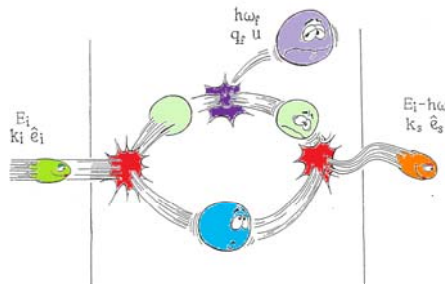


Introduction to Raman scattering



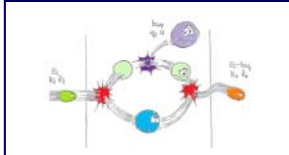
Jens KREISEL

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Outline



A. Introduction to Raman scattering

1. Interest of vibrational spectroscopy
2. Concept & Theory
3. Experimental issues

B. Illustrations **1** : Non-oxides

C. Illustrations **2** : Ferroic oxides

1. Octahedra tilts (ferroelasticity)
2. Cation displacements (ferroelectricity)
3. Strain in thin films

D. Illustrations **3** : Multiferroic oxides

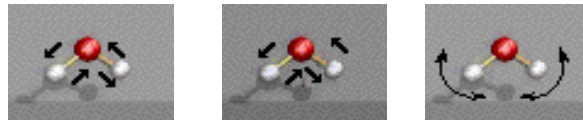
1. Thin films & Phase Transitions
2. Hetero-structures
3. Spin phonon-coupling
4. Electromagnons

E. Current trends & conclusions

Introduction: **Vibrational spectroscopy**

Chemical bonds between atoms in a molecule or a crystal are not rigid ...

↳ Atoms move around their centre of gravity !
(small amplitude, up to a fraction of the atomic size)

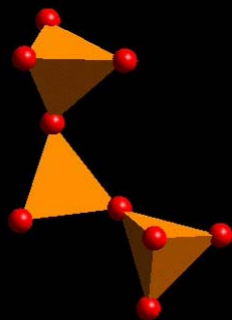


Vibrations are characteristic for a material → « *Fingerprint* »
(structure, chemistry, physics, state)

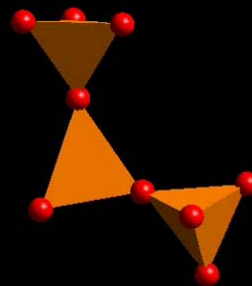
- Methods:
- Infrared spectroscopy
 - Raman spectroscopy
 - Inelastic neutron scattering
 - Ab-initio calculation

Atomic vibrations

Room temperature



High temperature



SiO₄ tetrahedra
in silicon

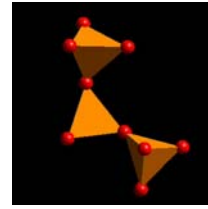
A vibration (Raman spectrum) is a unique **fingerprint**
for a given material, at a given external condition

Movies: M. Dove, Cambridge (UK)

Interest of vibrational spectroscopy (Raman scattering)

Vibrations are sensitive to changes of ...

- ... external parameter (strain, temperature, pressure, E, H)
- ... physical properties (ferroelectric, magnetic etc.)



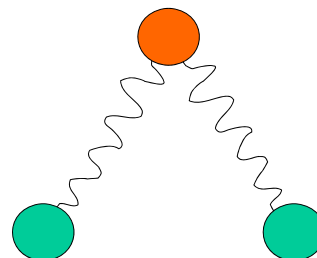
A probe for...

- ... identifying materials (solids, liquids, gas) or types of bonding (C-C \leftrightarrow C=C)
- ... structural phase transitions (or changes in lattice distortion)
- ... investigating coupling phenomena (spin-phonon, electromagnons etc.)
- ... investigating strain in thin films, nanocomposites etc.
- ... testing centro-symmetry etc.

Harmonic oscillator:

$$\omega = (k/\mu)^{1/2}$$

k: force constant
 μ : reduced mass



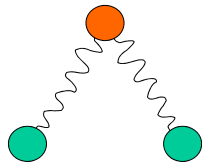
How many vibrational modes do exist ?

→ Degrees of freedom (DF)

- every atom: 3 degrees of freedom (x, y, z)
- crystal/molecule: $3N$ degrees of freedom
(N : atoms in the unit cell/of a molecule)
- among those $3N$:
 - 3 DF for a translation
 - 3 DF for a rotation (2 for a linear molecule)
 - The remaining: vibrational DF (**vibrational modes**)
 - $3N - 6$ for non-linear molecules
 - $3N - 5$ for linear molecules
 - $3N - 3$ for crystals (no free rotation !)

Degrees of freedom (DF), examples

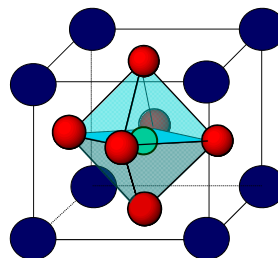
H₂O



$N = 3$ atoms → $3N = 9$ DF
minus 3 DL (translation)
minus 3 DL (rotation)

→ $3N - 6 = 3$ vibrational modes

Perovskite ABO₃

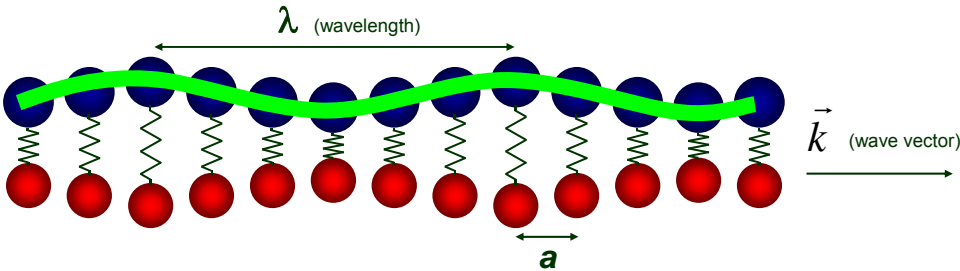


$N = 5$ at./uc. → $3N = 15$ DF
minus 3 DF (translation)

→ $3N - 3 = 12$ vibrational DF

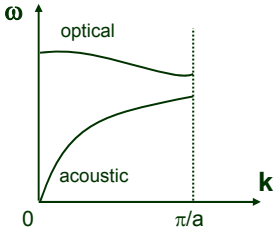
here $a=b=c$ → 4 triply generated modes

Vibrations and phonons ...



A vibrational wave can be described by a *quasi*-particle: **A phonon**
 (in analogy with a photon for an electromagnetic wave)

$\omega = \omega(k)$
 (Phonon dispersion)



Phonons and Raman spectroscopy

- Optical photons: small wave-vector
- Wave-vector conservation
- Raman phonons: very small momentum transfer

$k \approx 0$ (zone center)
 $\lambda \approx \infty$

Raman spectroscopy

all unit cell vibrate *in phase*

$k \approx \pi/a$ (zone boundary)

all unit cells vibrate *in anti-phase*

Raman scattering, a bit of history ...

1923 Theoretical prediction by the Austrian physicist A. Smekal

"The quantum theory of dispersion" (*Naturwissenschaften* 11, p. 873, 1923)

1928 Experimental discovery

- by the Indians C.V. Raman and K.S. Krishnan in Kalkutta

"The optical analog of the Compton effect" (*Nature* 121, p.711, 1928)

- by the Russians G. Landsberg et L. Mandelstam à Moscou

"A novel effect of light scattering in crystals" (*Naturwissenschaften* 16, p.557, 1928)



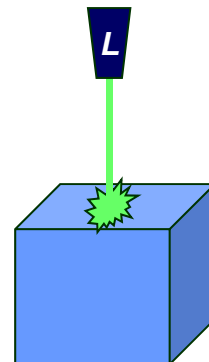
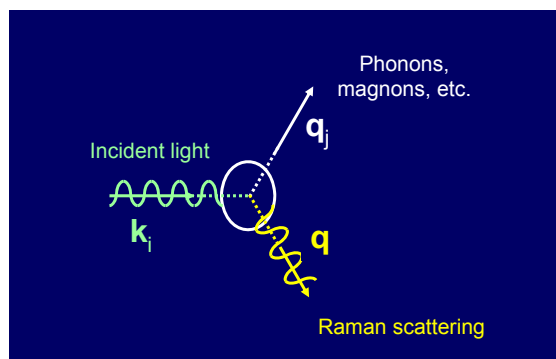
1930 Nobel price: Sir C.V. Raman (* 1888, † 1970)

"... for is work on light scattering and the discovery of the later called Raman effect ..."

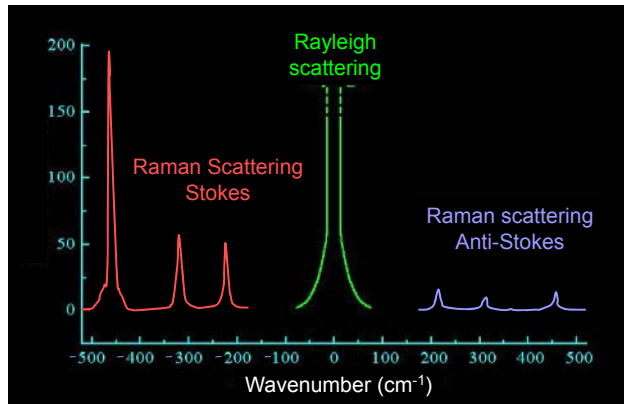
≈ 10.000 published articles using Raman scattering in the year 2011 [source WoS]

A.2 Concept & Theory: What is the Raman effect ?

Inelastic scattering of light with a material



Example of a Raman spectrum



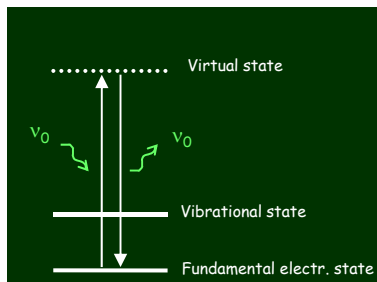
The unit of « spectroscopists », the wavenumber (cm^{-1}):

$$\tilde{\nu} = \frac{1}{\lambda} = \frac{\nu}{c}$$

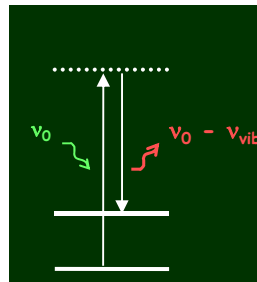
Conversions: 1 meV = 8.051 cm^{-1} 1 THz = 33 cm^{-1} 1 THz = 4.136 meV

Energy transfer model ...

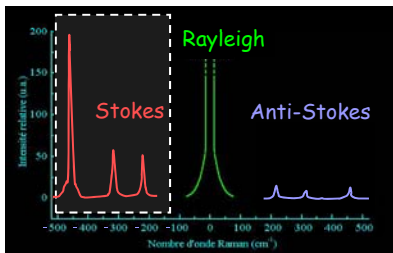
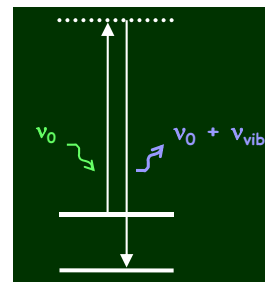
Raleigh scattering (elastic)



Stokes Scattering



Anti-Stokes scattering

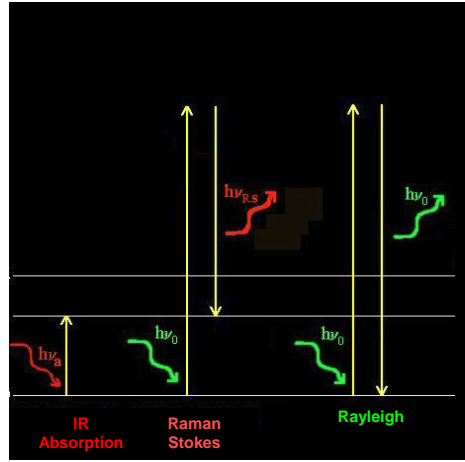
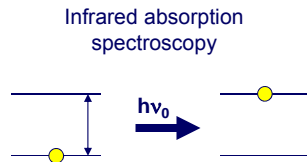


optical mode → Raman scattering
acoustic mode → Brillouin scattering

In principle, we can also study:

- rotational states
- magnetic states (→ magnons)
- electronic states (→ polarons)
- magneto-electric states (→ electromagnons)
- etc ...

Raman scattering ↔ Infrared absorption



IR absorption and Raman scattering are both vibrational spectroscopies
but involve different interactions (and thus selection rules)

Raman scattering- Classical treatment

Source of the scattered light (Rayleigh and Raman):

Induced dipole of the molecule by the incident electric field

Laser

$$\vec{E} = \vec{E}_0 \cos(\omega_0 t)$$

Molecule

$$x = x_0 \cos(\omega_M t)$$

- Induced electric dipole

$$\vec{\mu} = \alpha \vec{E} + \frac{1}{2} \beta \vec{E} \vec{E} + \frac{1}{6} \gamma \vec{E} \vec{E} \vec{E} + \dots$$

Raman scattering

Hyper-Raman scattering

a : polarisability (**tensor!**)
b : hyper-polarisability
g : 2° hyper-polarisability

- $\alpha \gg \beta \gg \gamma$

$$\vec{\mu} \cong \alpha \vec{E}$$

Limitation to linear effects

Classical treatment (induced dipole)

$$\vec{\mu} \cong \alpha \vec{E}$$



Taylor development of the polarisability around x_0

$$\alpha(x) = \alpha_0 + \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} x + \dots$$

$$\vec{\mu} = \left(\alpha_0 + \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} x \right) \vec{E} \quad \text{(induced electric dipole)}$$

Incident field

$$\vec{E} = \vec{E}_0 \cos(\omega_0 t) \Rightarrow \left(\alpha_0 + \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} x \right) \vec{E}_0 \cos(\omega_0 t)$$

Eigen-vibration of the molecule

$$x = x_0 \cos(\omega_M t) \Rightarrow \alpha_0 \vec{E}_0 \cos(\omega_0 t) + \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} \vec{E}_0 \cos(\omega_0 t) x_0 \cos(\omega_M t)$$

Classical treatment (result)



$$\vec{\mu} = \alpha_0 \vec{E}_0 \cos(\omega_0 t) + \frac{1}{2} \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} \vec{E}_0 x_0 [\cos(\omega_0 + \omega_M)t + \cos(\omega_0 - \omega_M)t]$$

$$\vec{\mu} = \vec{\mu}(\omega_0) + \vec{\mu}(\omega_0 + \omega_M) + \vec{\mu}(\omega_0 - \omega_M)$$

Raman scattering results from a modulation of the incident electric field by the vibrating molecule

... leads to two new frequencies
 $(\omega_0 + \omega_M$ and $\omega_0 - \omega_M)$

Classical treatment (Raman activity)

$$\vec{\mu} = \alpha_0 \vec{E}_0 \cos(\omega_0 t) + \frac{1}{2} \left. \frac{\partial \alpha}{\partial x} \right|_{x_0} \vec{E}_0 x [\cos(\omega_0 + \omega_M)t + \cos(\omega_0 - \omega_M)t]$$

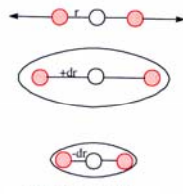
Selection rule

A mode is only active in
Raman spectroscopy if

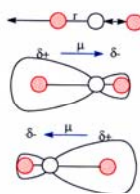
$$\left. \frac{\partial \alpha}{\partial x} \right|_{x_0} \neq 0$$

Illustration of the Raman activity & symmetry

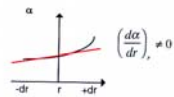
Symmetric mode



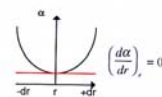
Asymmetric mode



$$\left. \frac{\partial \alpha}{\partial x} \right|_{x_0} \neq 0$$

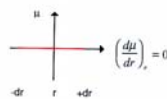


Raman **active**

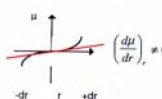


Raman **inactive**

$$\left. \frac{\partial \mu}{\partial x} \right|_{x_0} \neq 0$$



IR **inactive**



IR **active**

Raman and IR spectroscopy are **complementary**!

Exclusion rule

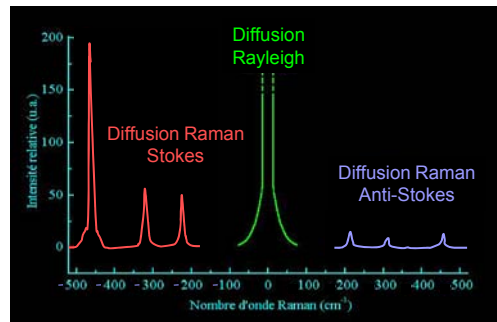
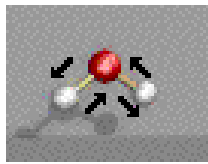
In a centro-symmetric molecule or crystal none of the Raman active modes is IR-active and vice versa.

The change in the molecular dipole moment when the atoms vibrate determines whether the vibration is or is not IR active.

Conclusive remarks on the theoretical part

Raman scattering: Inelastic scattering of light with a material

Harmonic oscillator: $\omega = (k/\mu)^{1/2}$
k: force constant
 μ : reduced mass



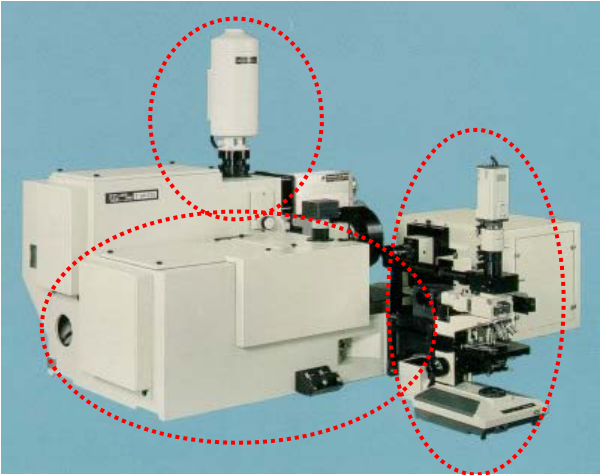
A Raman spectrum is a unique (vibrational) fingerprint for a given material

2.

Instrumental & experimental aspects



How does a Raman spectrometer look like ?

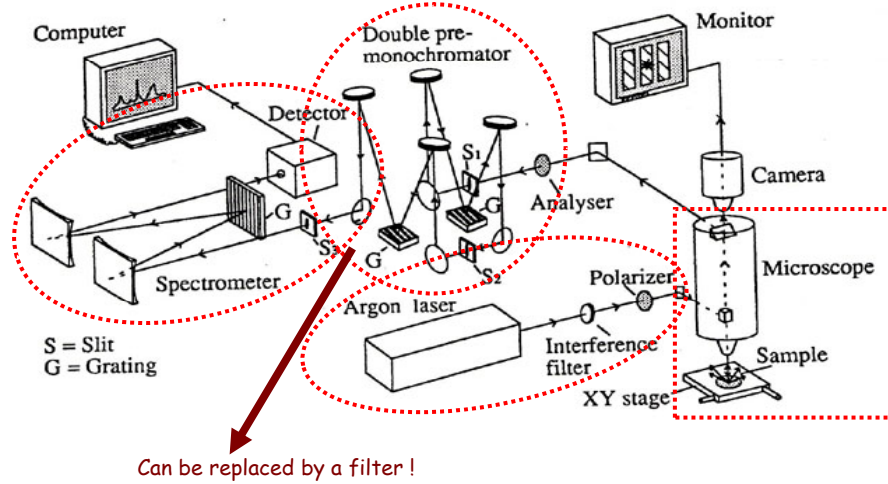


Raman Spectrometer T64000 (Jobin-Yvon)

Or more compact spectrometers



Instrumentation



Sample preparation ?

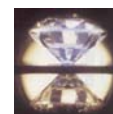
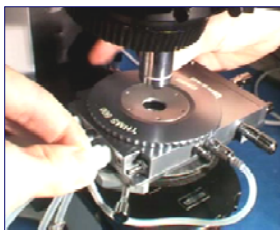
In most cases no preparation necessary

External parameters ?

Temperature (80 K to 1800 K)

- under atmosphere (Ar, O₂, N₂ or vacuum)
- simultaneous transport measurements
- simultaneous *E*-field

Pressure (↗ 100 GPa)



etc...

Which materials have a “nice” Raman signature ?

Difficult to say ..., but there are indications:



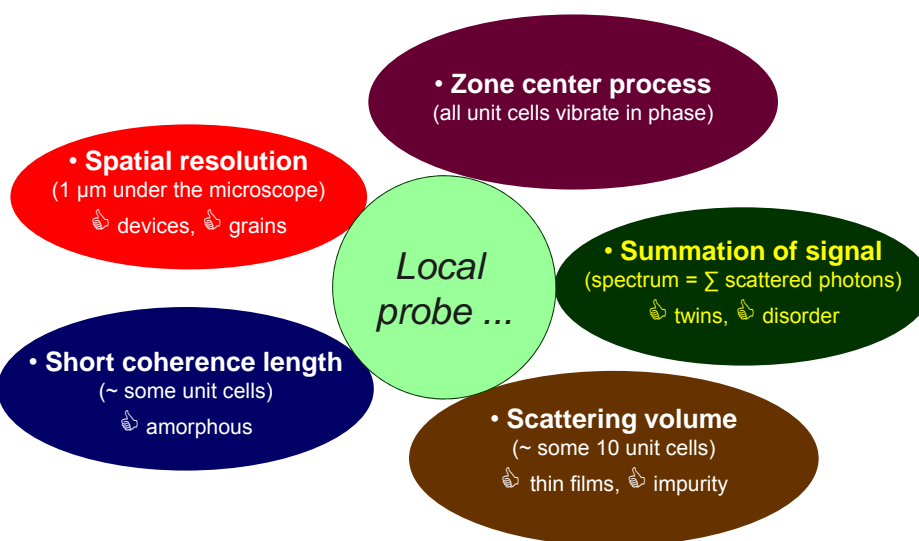
- oxide, fluoride, diamond, SiC etc. (transparent materials)



- cubic ($Pm-3m$) materials have no Raman signature
- disorder (chemical, structural, ...)
- strong metallic character
- strong absorption in the visible range
- strong reflectivity in the visible range
- bad crystalline quality

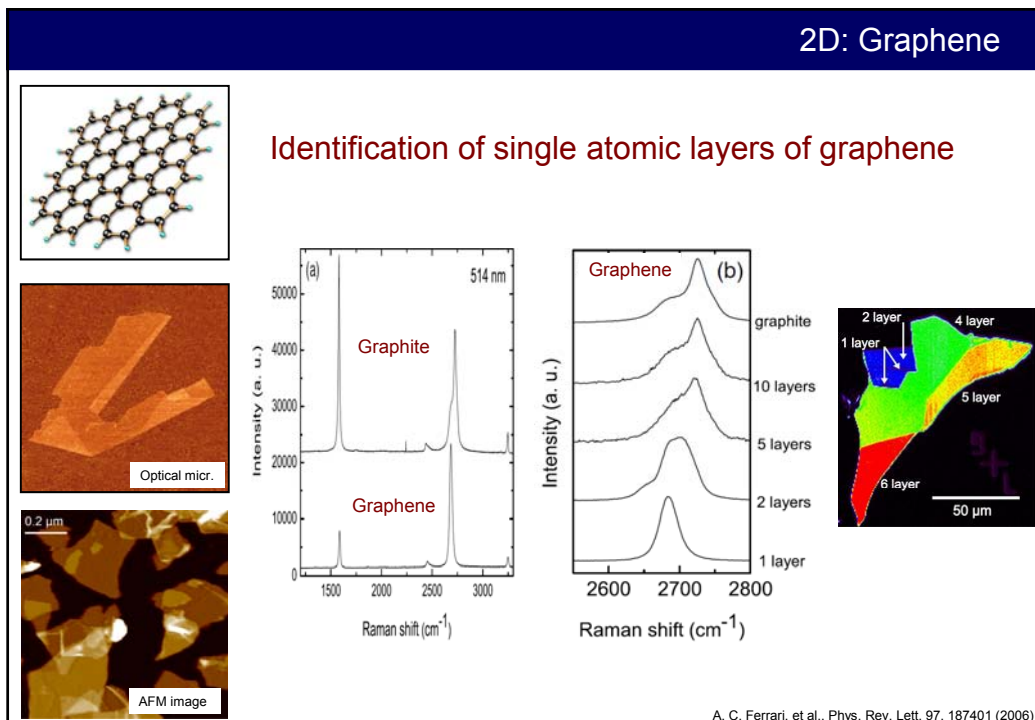
however ... silicon, graphite etc ... have a strong Raman signature

Why is Raman spectroscopy a local probe ?

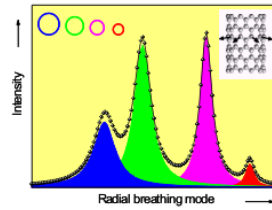
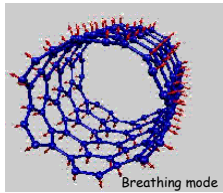
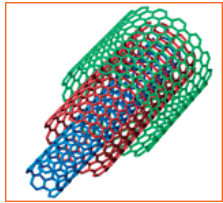
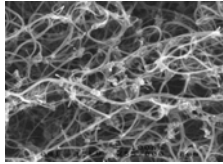


B. Illustrations 1

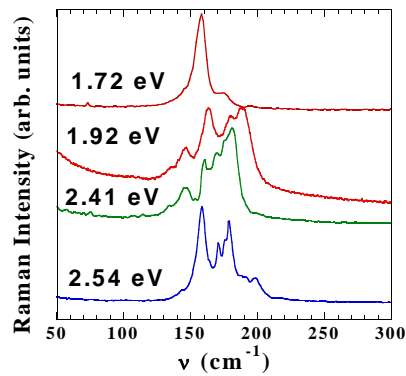
B.1 Raman scattering of non-oxide materials



1D: Carbon nanotubes



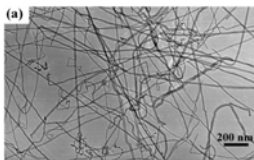
Determination of nanotube diameter !



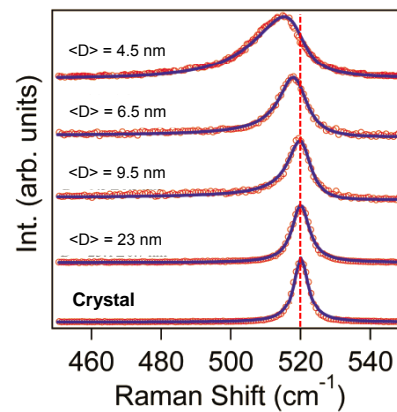
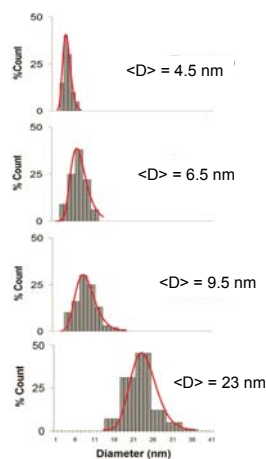
Nano-Size effects in Si nanowires

K. W. Adu et al., Nanolett. 5, 409 (2005)

TEM image of Si nanowires



Distribution of diameters



→ Identification and characterization of nano-size effects

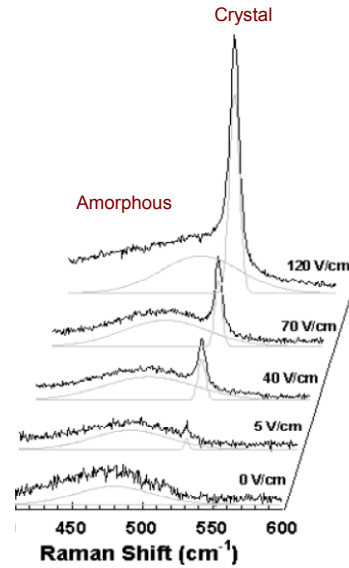
Amorphous samples

Do amorphous samples have a Raman signature ?

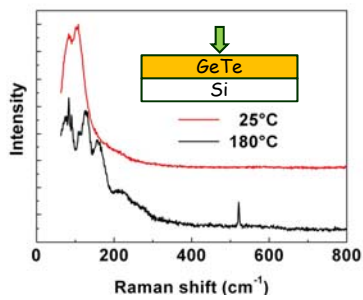
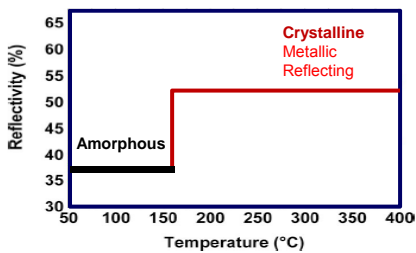
Example

Amorphous vs. nano-crystalline Si

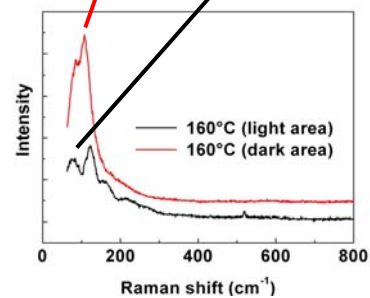
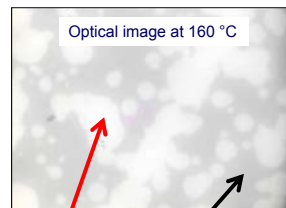
S. Jin Park et al., J. Korean Phys. Soc. 42, S466 (2005)



Phase Change Materials/Memories (PCM's), e.g. GeTe



→ Probing of phase transition

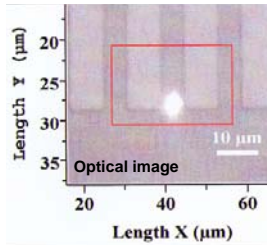


→ Probing transition region

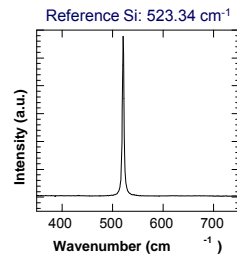
E. Gourvest, J. Kreisel, M. Armand, S. Maitrejean, A. Roule, S. Lhostis, C. Vallée, Appl. Phys. Lett. 95, 031908 (2009).

Raman imaging in micro- and nano-technology

Contacts on a Si wafer



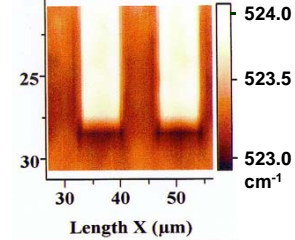
Do the contacts induce strain ?



Change in band position

↓
Strain !

Raman (strain) image



Strain underneath & at corner of contacts

Potential effect on dopants ...

Michel Mermoux, Grenoble, unpublished

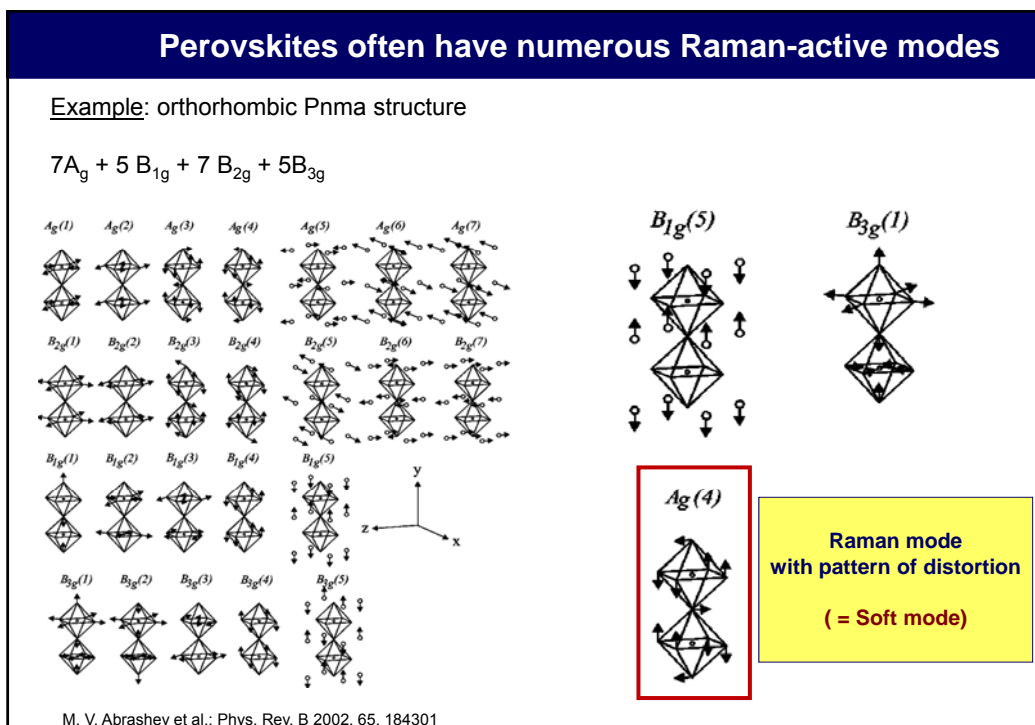
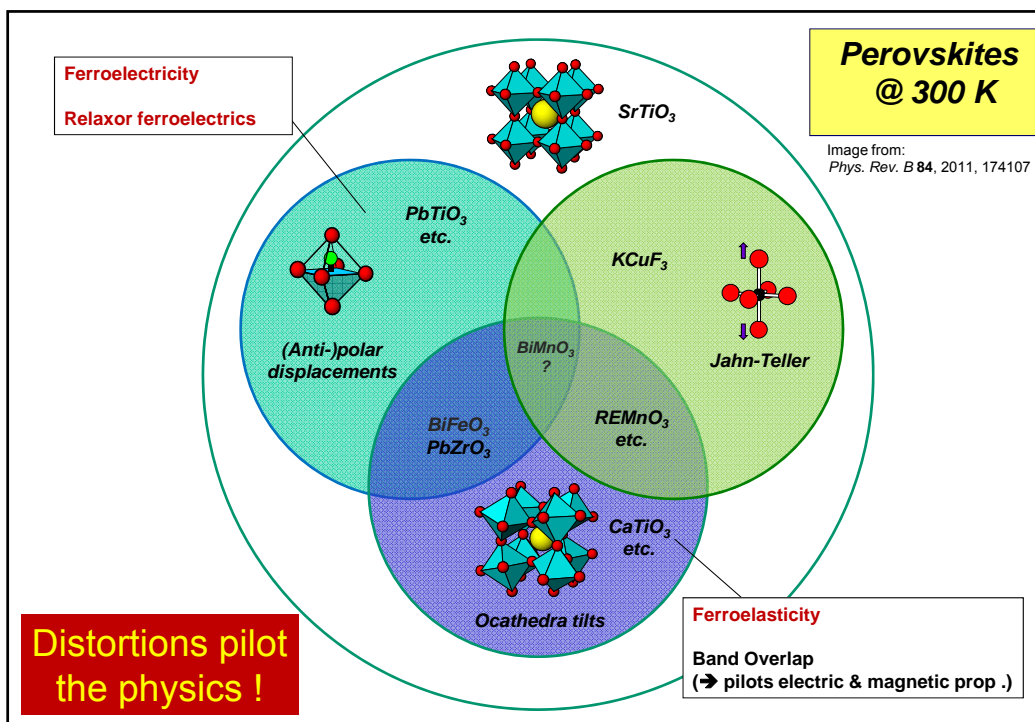
C. Illustrations 2

Raman scattering of ferroic oxides

(or ... Treating individual ferroic orders before looking at multiferroics)

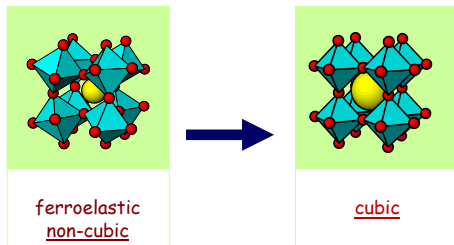
1. Octahedra tilts (ferroelasticity)
2. Cation displacements (ferroelectricity)

(The notion of “soft modes” & “hard modes”)



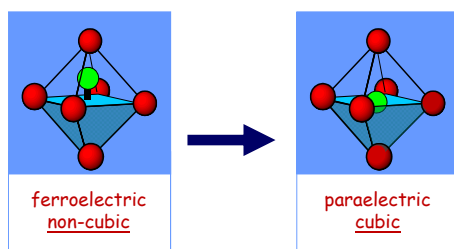
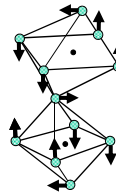
Probing the structural distortion & phase transition of perovskites

Structural distortion

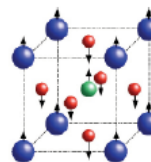


Following rotation angle of octahedra
(→ orbital overlap)

Raman mode with pattern of distortion
(= Soft mode = Instability)

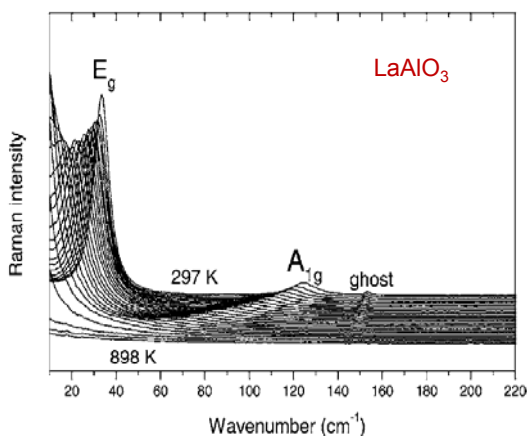


Following polar displacements
(→ ferroelectricity)

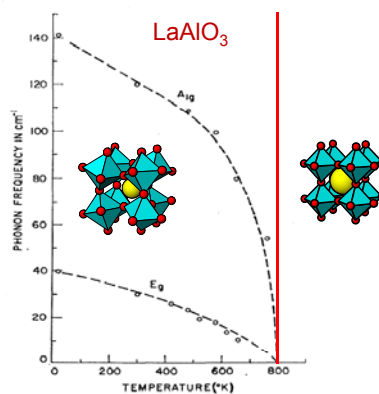


Prototype exemple for octahedra rotations: LaAlO₃

S. A. Hayward et al., Physical Review B 72, 054110 (2005).



J. F. Scott, Physical Review 183, 823 (1969).



Landau theory:

$$\omega^2(T) = \omega_0^2 (T_c - T) = \theta (T)^2$$

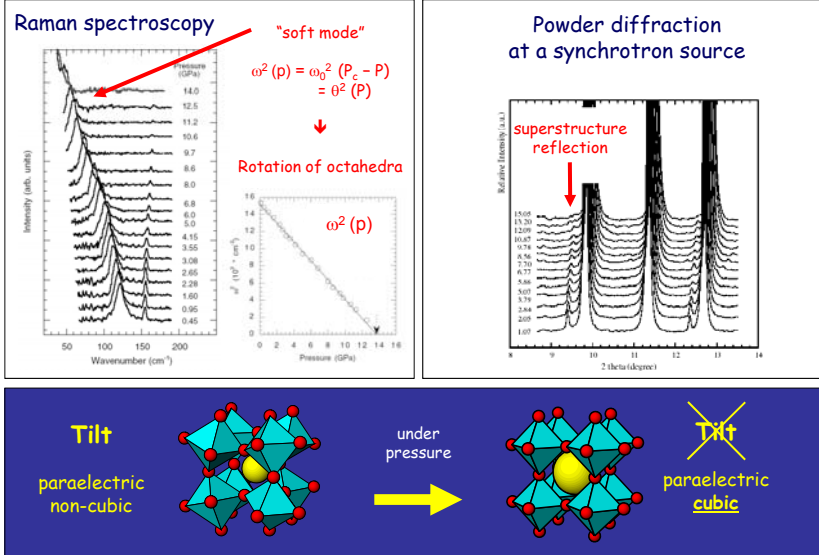
Position of soft mode → Tilt angle θ

See also the textbook example: SrTiO₃

[P. A. Fleury, J. F. Scott, and J. M. Worlock, Physical Review Letters 21, 16 (1968).]S

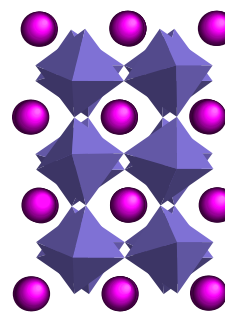
Effect of high-pressure on octahedra tilts: LaAlO_3

P. Bouvier & J. Kreisel J. Phys.: Condens. Matter **14**, 3981 (2002)



Octahedra tilts in "stable" perovskites

- Orthorhombic space group $Pnma$ ($a \neq b \neq c$, $\alpha = \beta = \gamma = 90^\circ$)
- Most common structure of perovskites
- Examples:
 - orthomanganites ($R\text{MnO}_3$)
 - orthoferrites ($R\text{FeO}_3$)
 - orthoscandates ($R\text{ScO}_3$)
 - orthochromites ($R\text{CrO}_3$)
- Tilt system: $a^- a^+ c^+$
 → can be described by two octahedra rotations

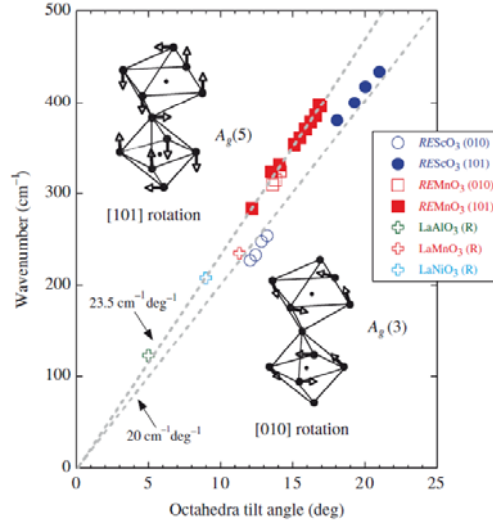
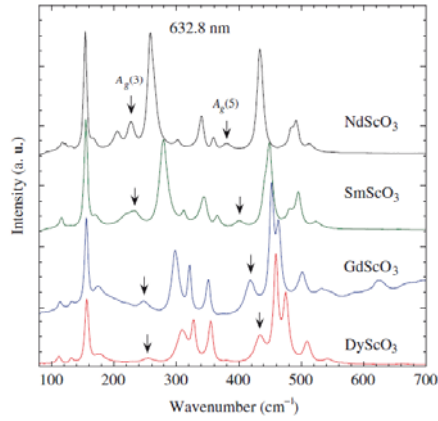


$A_g(5)$
[101] rotation

$A_g(3)$
[010] rotation

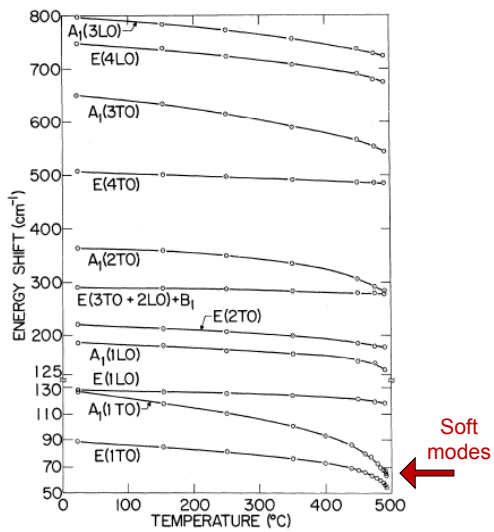
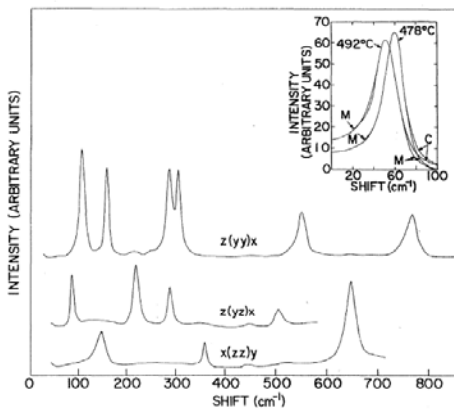


Position of Raman phonons scale with tilting angle



ReMnO₃: M. N. Iliev et al., Physical Review B 73, 064302 (2006).
 ReScO₃: O. Chaix-Pluchery, & J. Kreisel, Phase Transitions 48, 542 (2011).
 ReCrO₃: M. Weber, J. Kreisel et al., arXiv:1112.3618v1 (2012)

C.2 Cation displacements (ferroelectricity): BaTiO₃



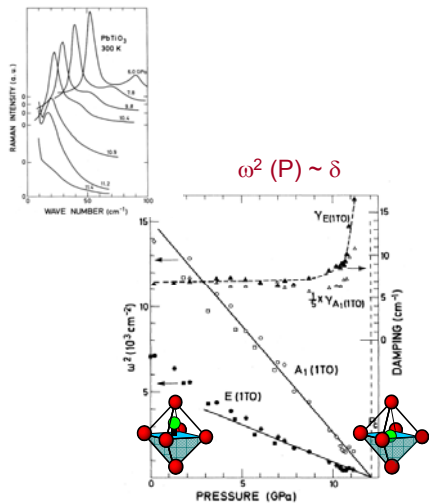
C. H. Perry, and D. B. Hall, Physical Review Letters 15, 700 (1965).

High-pressure studies of PbTiO_3

High-Pressure Raman data

J.A. Sanjurjo, E. Lopez-Cruz, G. Burns

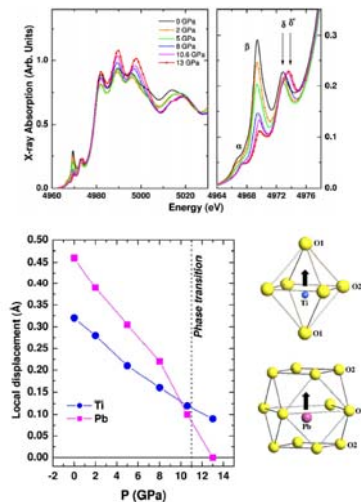
Phys. Rev. B **28**, (1983), p. 7260



High-pressure X-ray absorption data

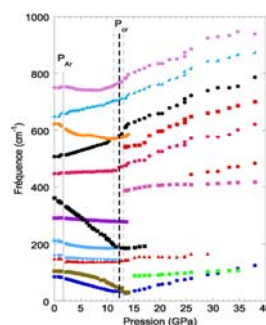
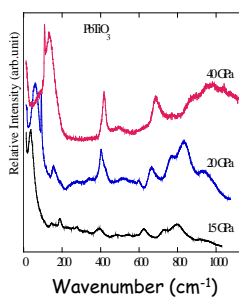
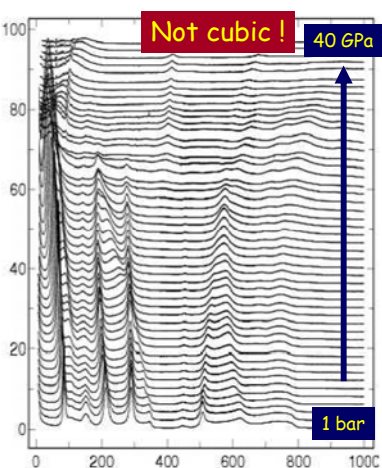
N. Jaouen, A.C.Dhaussy, J.P.Itié, A.Rogalev, S.Marinel, Y.Joly

Phys. Rev. B **75** (2007) p. 224115

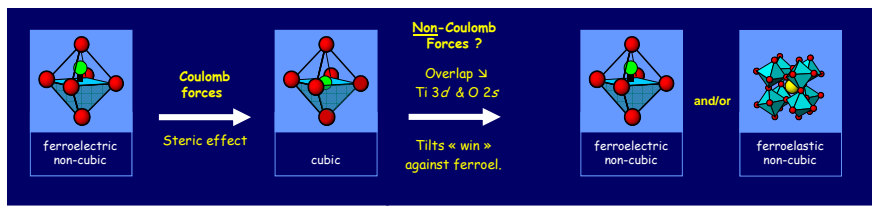


The ferroelectric PbTiO_3

P. Bouvier, B. Dkhil, J.Kreisel et al. Phys. Rev. Lett. **95** (2005) & Phys. Rev. Lett. **101** (2008)

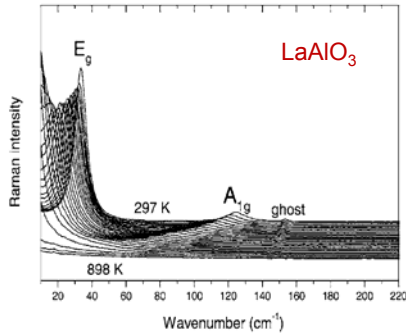


Not cubic at high pressure! → New mechanisms

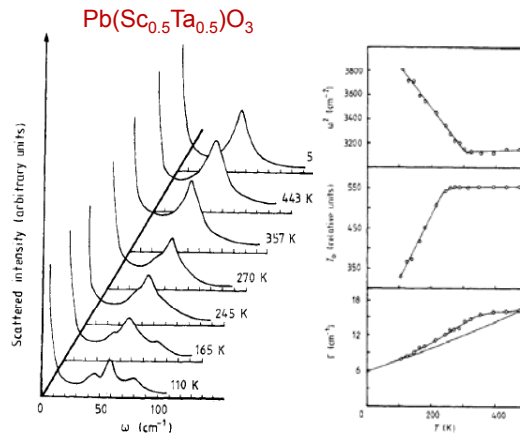


Soft ↔ Hard mode spectroscopy

S. A. Hayward et al., Physical Review B 72, 054110 (2005).



U. Bismayer, V. Devarajan, and P. Groves, Journal of Physics: Condensed Matter 1, 6977 (1989).



See also:

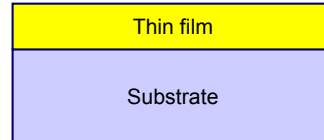
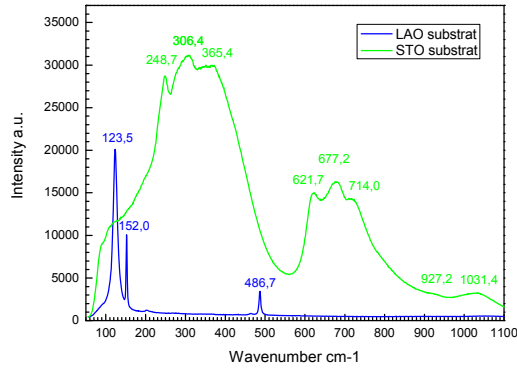
U. Bismayer, Hard Mode Raman Spectroscopy and Its Application to Ferroelastic and Ferroelectric Transitions, *Phase Transitions* 27 (1990) pp. 211
E. K. H. Salje and U. Bismayer, Hard Mode Spectroscopy: The Concept and Applications, *Phase Transitions* 63 (1997) pp. 1

D. Illustrations 3

Raman scattering of multiferroic oxides

1. Thin films & Phase Transitions
2. Hetero-structures
3. Spin phonon-coupling
4. Electromagnons

D.1. Thin films & their substrate ...



Strongly scattering substrate

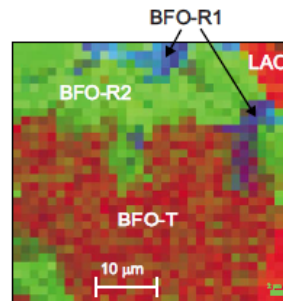
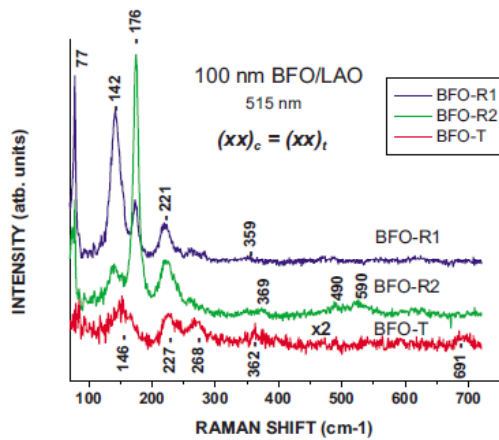
→ a potential problem for investigating very thin films (can be overcome by UV-Raman)

Raman spectra & imaging of inhomogeneous films

Example: Highly-strained BiFeO₃ films on LAO with phase coexistence

Potential lead-free piezoelectric

[J. X. Zhang et al., Nat Nano 6, 98 (2011)]

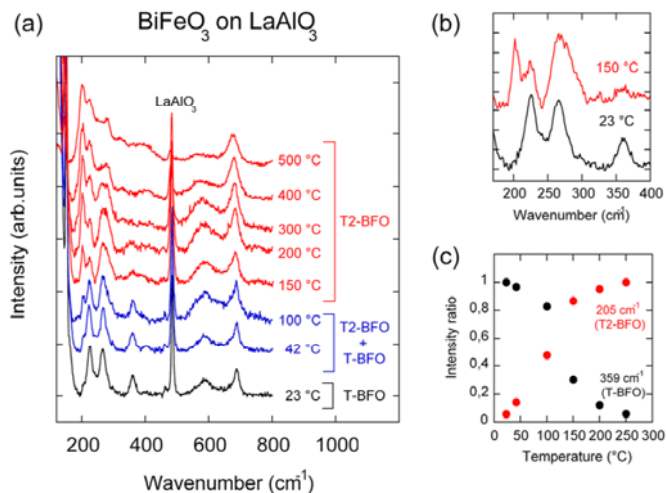


Raman image

M. N. Iliev, M. V. Abrashev, D. Mazumdar, V. Shelke, and A. Gupta, Physical Review B 82, 014107 (2010)

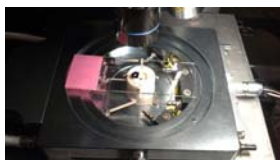
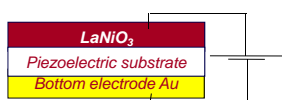
Probing a phase transition in tetragonal-like BFO by Raman scattering

J. Kreisel, P. Jadhav, O. Chaix-Pluchery, M. Varela, N. Dix, F. Sánchez, and J. Fontcuberta, Journal of Physics: Condensed Matter 23, 342202 (2011).

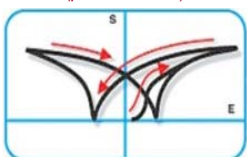


Structural transition close to 300 K in multiferroic BiFeO₃ thin films

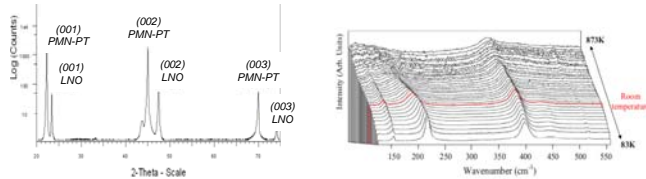
Following the strain engineering of films on a piezoelectric substrate



Strain as a fct. of E
(piezo substrate)

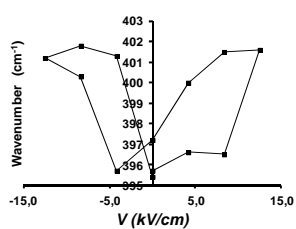


Good quality films on piezoelectric substrate (XRD & Raman)



N. Chaban, M. Weber, J. Kreisel, S. Pignard Appl. Phys. Lett. 97, 031915 (2010)

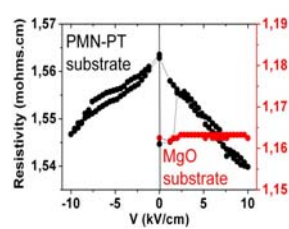
Raman phonon frequency
as a fct. of E
(LaNiO₃ thin film)



Transmission of strain to thin film !

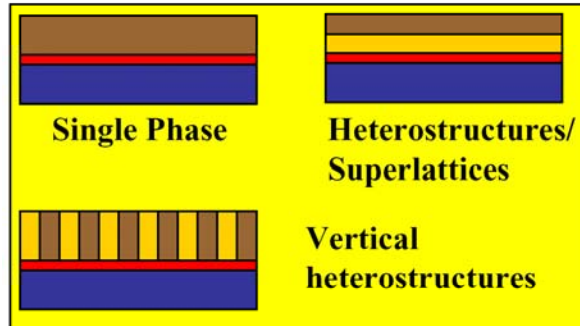
N. Chaban, J. Kreisel, S. Pignard, unpublished

Resistivity
as a fct. of E
(LaNiO₃ thin film)



→ 2% change in resistivity

D.2 Heterostructures



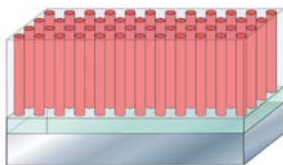
Raman scattering of self-organized Multiferroic Nano-composites

H. Zheng, J. Kreisel, Y.-H. Chu, R. Ramesh, and L. Salamanca-Riba, Appl. Phys. Lett. 90, 113113 (2007).

O. Chaix-Pluchery, C. Cochard, P. Jadhav, J. Kreisel, N. Dix, F. Sánchez, and J. Fontcuberta, Appl. Phys. Lett. 99, 072901 (2011).

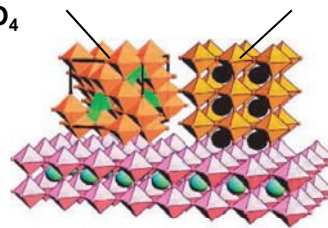
Exploiting strain coupling

- Magneto-electric memories
- Energy harvesting



Ferromagnetic
 CoFe_2O_4
matrix

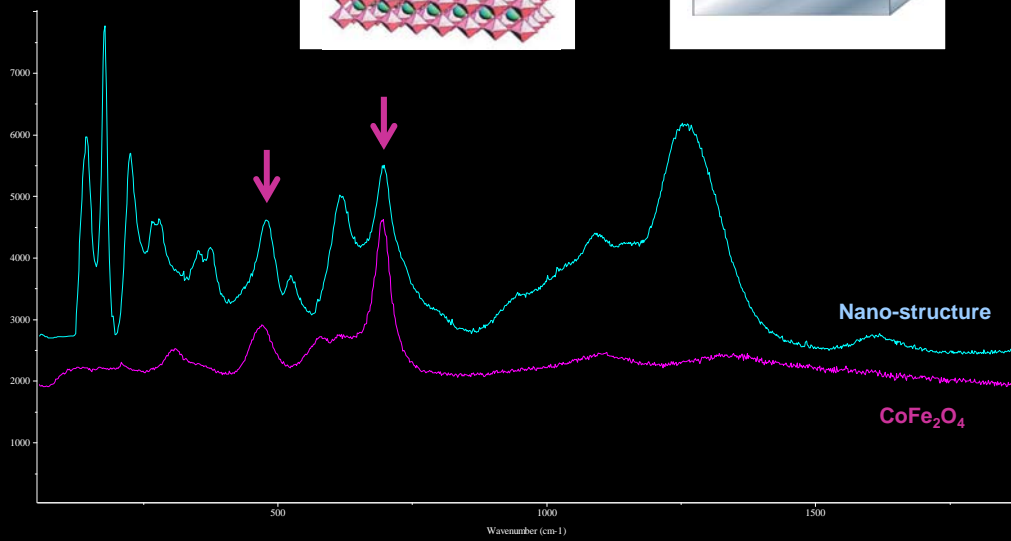
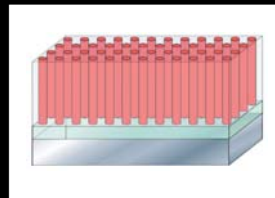
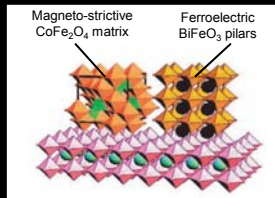
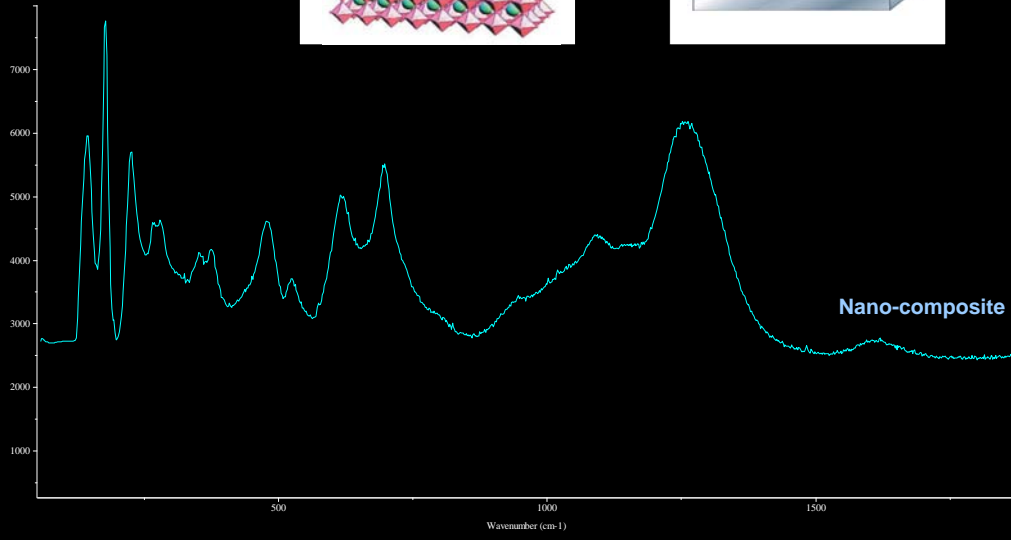
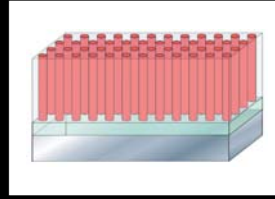
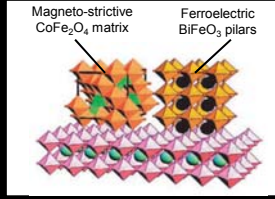
Ferroelectric
 BiFeO_3 pillars

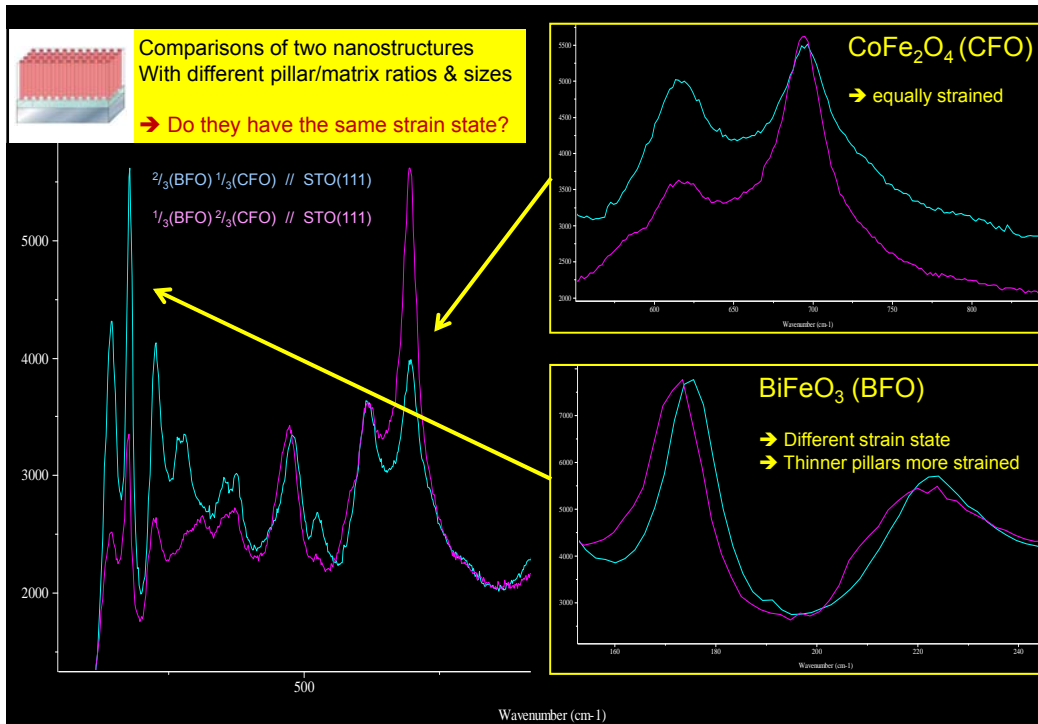
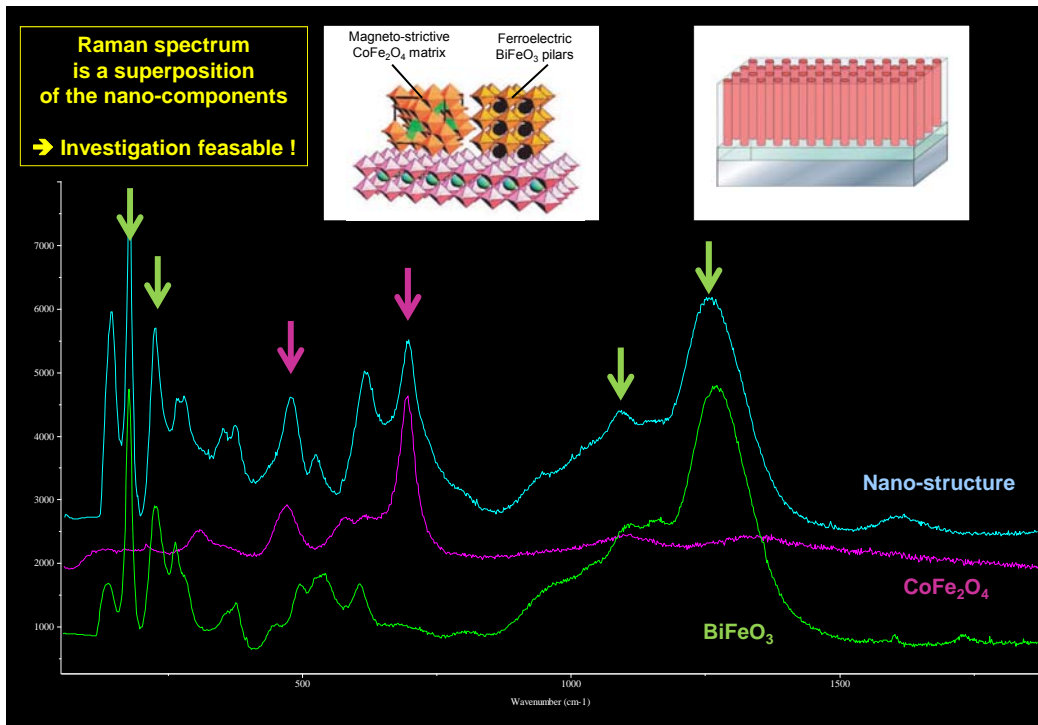


SrTiO_3 substrate

Strain-state and strain-coupling in multiferroic perovskite/spinel nano-composite ?

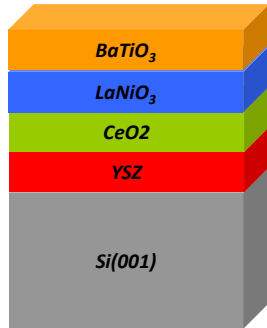
**Raman spectrum
of the nano-composite**





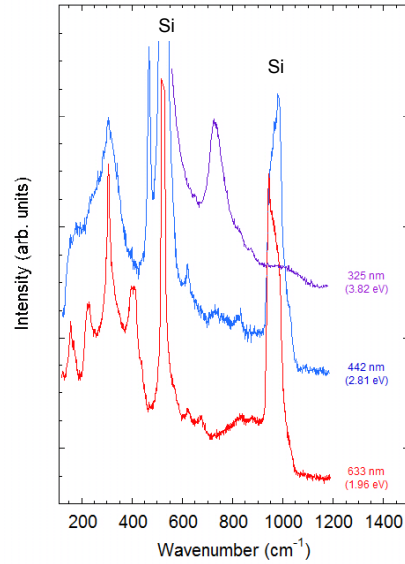
Raman scattering of complex heterostructures

J. Kreisel, M. Weber, J. Fontcuberta (Barcelona), unpublished



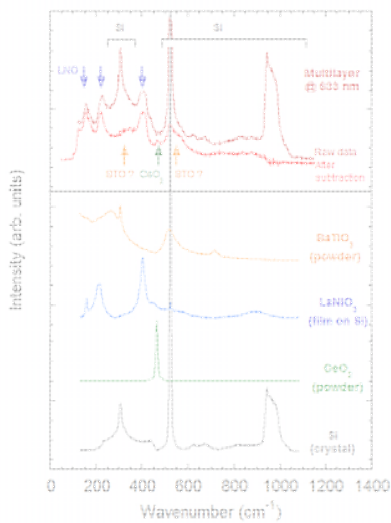
Use of different wavelengths

- Different optical depths
- Different absorption
- Different Raman cross sections

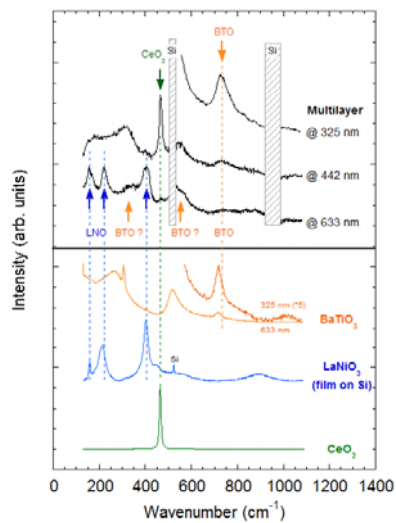


Raman scattering of complex heterostructures

Reference spectra & Si-subtraction

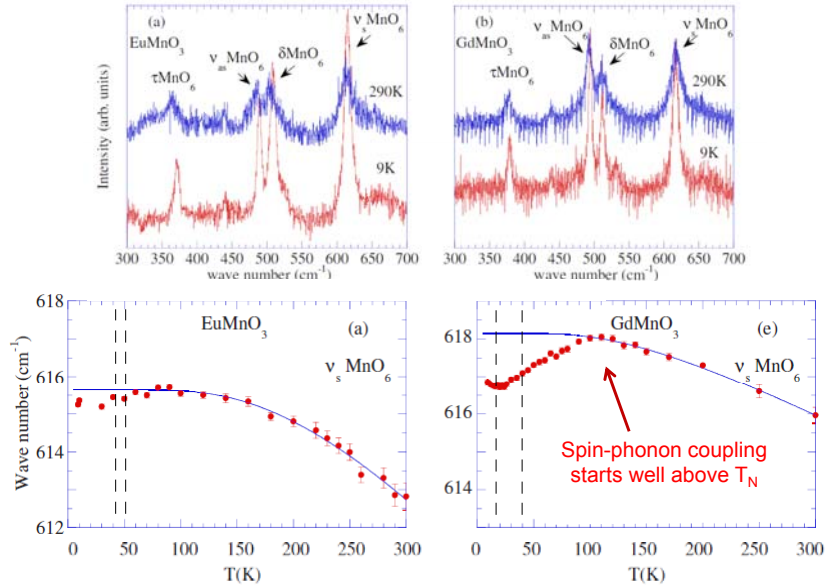


Final mode assignment → Evidence for strain



D.3 Spin-Phonon coupling (always present, but usually small)

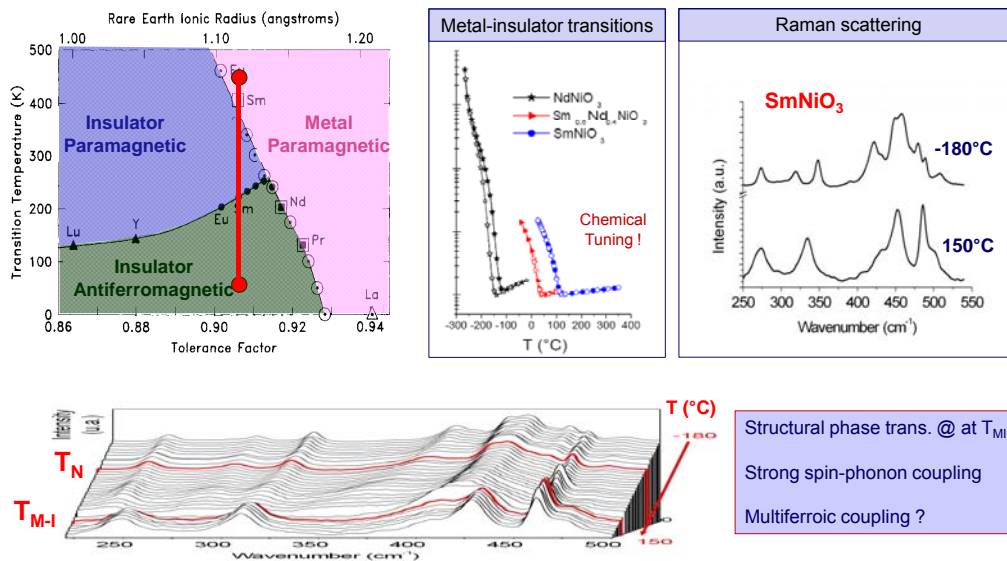
J. A. Moreira, A. Almeida, J. Kreisel et al. *Phys. Rev. B* **79**, 054303 (2009), *Phys. Rev. B* **81**, 054447 (2010), *Phys. Rev. B* **82**, 094418 (2010).



Look at: J. Laverdière, S. Jandl, A. A. Mukhin, V. Y. Ivanov, V. G. Ivanov, and M. N. Iliev, *Physical Review B* **73** (2006) pp. 214301

Phase transitions in ReNiO_3

MI & magnetic phase transition \rightarrow Structural transition ?



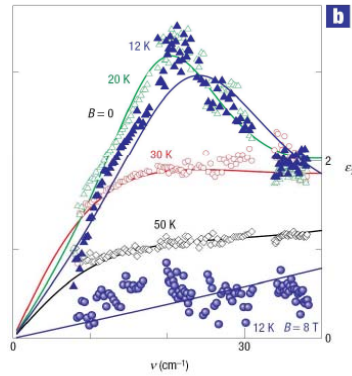
Structural phase trans. @ at T_{M-I}
Strong spin-phonon coupling
Multiferroic coupling ?

C. Girardot, J. Kreisel, S. Pignard et al. *Phys. Rev. B* **78**, 104101 (2008)

D.4 Electromagnons

Spin waves excited by ac E-fields [Pimenov]

New excitations of mixed magnetic (magnons) and lattice (phonons) character ?



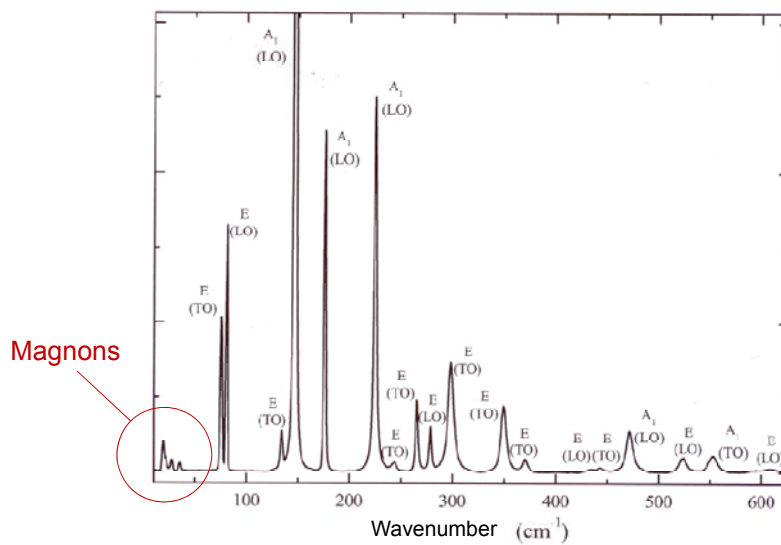
Optical conductivity
New peaks with dipolar activity



Electromagnon

Pimenov et al. Nature Phys 2, 97 (2006)
A. B. Sushkov, PRL 98, 027202 (2007)

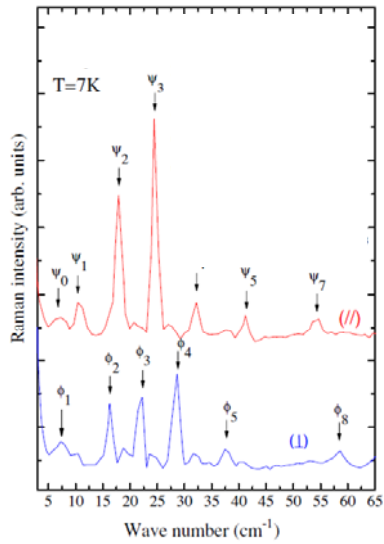
Raman signature of BiFeO₃



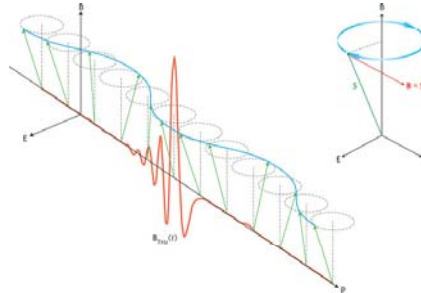
Taken from PhD thesis P. Rovillain, Paris (F)

Beyond phonons → Magnons & Electromagnons

M. Cazayous, et al. Physical Review Letters 101, 037601 (2008).



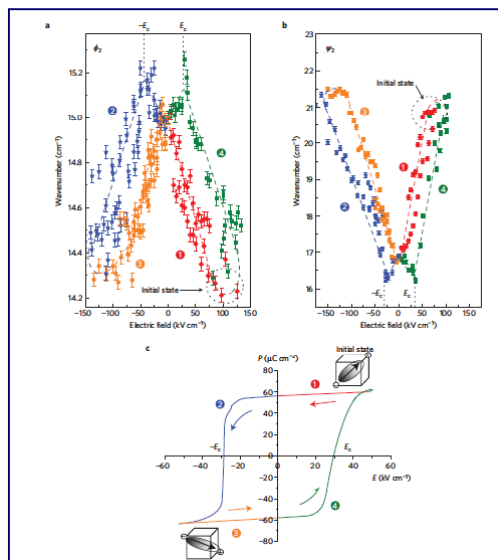
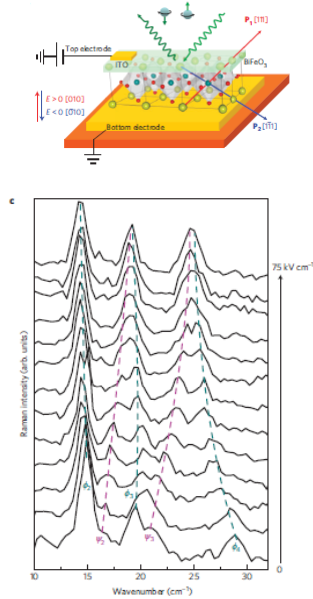
Magnetic excitations (magnons)

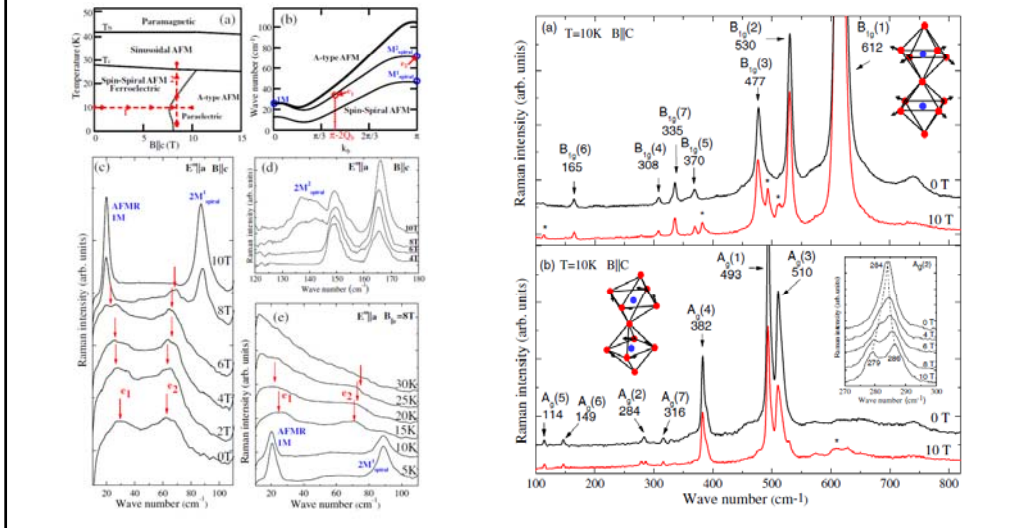


Possible electromagnons ?!

Electric-field control of spin waves in multiferroic BiFeO_3

P. Rovillain et al., Nat Mater 9, 975 (2010).



Magnetic Field Induced Dehybridization of the Electromagnons in Multiferroic TbMnO_3 P. Rovillain,¹ M. Cazayous,¹ Y. Gallais,¹ M-A. Measson,¹ A. Sacuto,¹ H. Sakata,² and M. Mochizuki³

D.

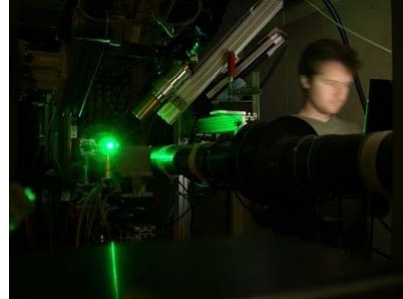
Emerging techniques & fields

Simultaneous use of Raman spectroscopie & synchrotron radiation

Now at almost all synchrotrons sources

3 beamlines @ ESRF

+ mobile spectrometers



See proceedings of the 2008 & 2011 international workshops:

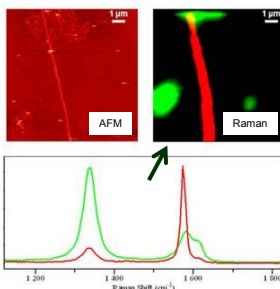
“ Workshop on Simultaneous studies of Raman spectroscopy with Synchrotron X-ray Absorption, Scattering and Diffraction ”

Emerging 1 ... Imaging & Enhancing the Raman signal

2 emerging techniques with sub- μ resolution

Coupled Raman-AFM

Co-localisation
&
analysis of sub- μ objects



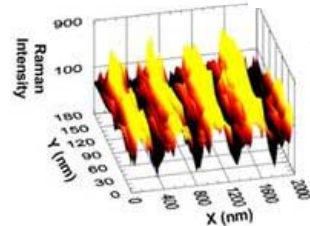
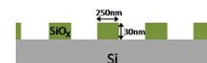
Carbon nanotubes
(AFM & Raman imaging)

Raman spectra of
different regions

Tip-enhanced Raman scattering (TERS)

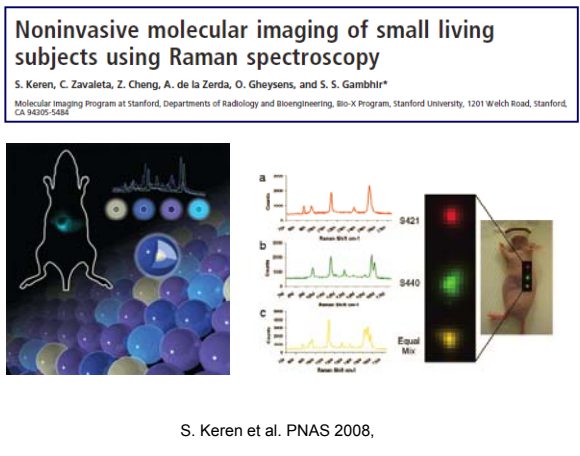
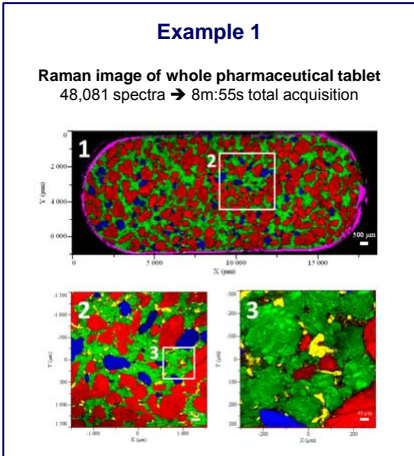
NanoRaman:
Spatial resolution <100nm
(mechanism not yet understood)

TERS Imaging of Nano-structured Silicon



SiO_x
on a Si substrate
imaged by TERS

Raman Spectroscopy, the Sleeping Giant in Structural Biology, Awakes*
 Paul R. Carey‡
 From the Department of Biochemistry, Case Western Reserve University, Cleveland, Ohio 44106



Concluding remarks ...

Raman spectroscopy ...

- ... is a versatile technique for the study of various materials
- ... is versatile for characterization and fundamental research
- ... complimentary to other techniques (diffraction etc.)
- ... versatile for investigating phase transitions and coupling mechanism

