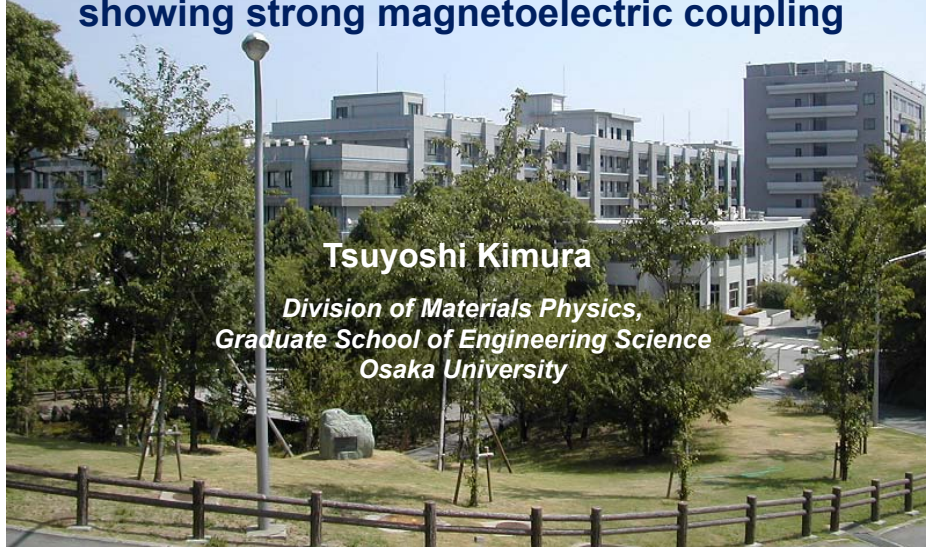


How to find and synthesize new multiferroics showing strong magnetoelectric coupling



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Session C21. DMP: Multiferroics II.
Monday morning, 11:00, 12 March 2001, Room 604, Washington State Convention Center

C21.001 Materials being simultaneously ferroelectric, ferromagnetic, ferrotoroidic and ferroelastic
Hans Schmid (University of Geneva, CH-1211 Geneva 4, Switzerland)

C21.002 Magnetism and ferroelectricity; why do they so seldom coexist?
Daniel Khomskii (Groningen University, The Netherlands)

C21.003 Biferroic (ferroelectric-ferroelastic) Characteristics of Oriented Piezoelectric Crystals
Dwight Viehland (Dept. of the Navy)

C21.004 Study of stress induced polarization switching in ferroelectrics using 2-D simulation
Rajeev Ahluwalia, Wenwu Cao (Pennsylvania State University)

C21.005 Piezoelectric characterization of Ferrite/Ferroelectric magnetoelectric composite system.
Srinivas Kuchipudi, Prasad Goduru, S.V Suryanarayana (Osmania University, Hyderabad-7, INDIA)

C21.006 Prediction of coupling magnetoelectric effect in ferromagnetic rare-earth-iron alloys
Ce-Wen Nan (Tsinghua University, Beijing 100084, China)

C21.007 Why are there so few magnetic ferroelectrics?
Nicola Hill (University of California at Santa Barbara)

C21.008 A Thermodynamic Theory for a Multiferroic
Avadh Saxena (Los Alamos National Laboratory), Pradeep Kumar (University of Florida)

Outline of this lecture

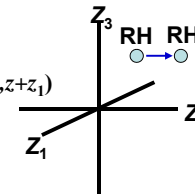
- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetoelectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites $RMnO_3$
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- ME effect in magnetically-disordered system

Symmetry operations

There are 4 kinds of geometric symmetry operations.

Translation

$$(x,y,z) \rightarrow (x+x_1, y+y_1, z+z_1)$$



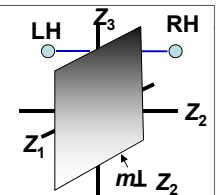
Mirror m

$$(x,y,z) \rightarrow (x,-y,z)$$

Direction cosine matrix

$$m \perp Z_2 \quad (a) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$|a| = -1$ A mirror plane is a 2D symmetry element that reverses the sign of one coordinate.



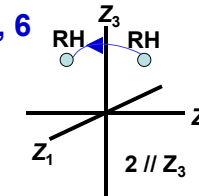
Rotation 2, 3, 4, 6

$$(x,y,z) \rightarrow (-x,-y,z)$$

Direction cosine matrix

$$2 \parallel Z_3 \quad (a) = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$|a| = +1$ Rotation axes are 1D symmetry elements that change two coordinates.



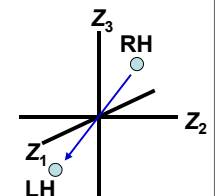
Inversion $\bar{1}$

$$(x,y,z) \rightarrow (-x,-y,-z)$$

Direction cosine matrix

$$\bar{1} \quad (a) = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

$|a| = -1$ Inversion center is a zero-D point that change all three coordinates.

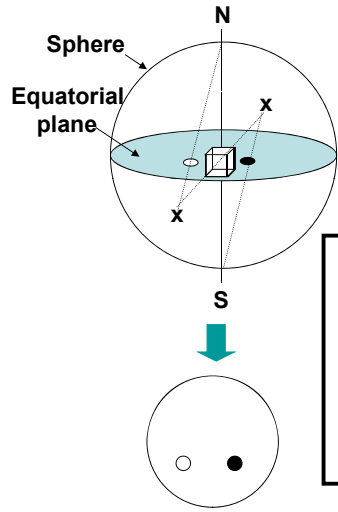


Mirror & Inversion transformations are accompanied by a handedness change, while rotation & translation are not.

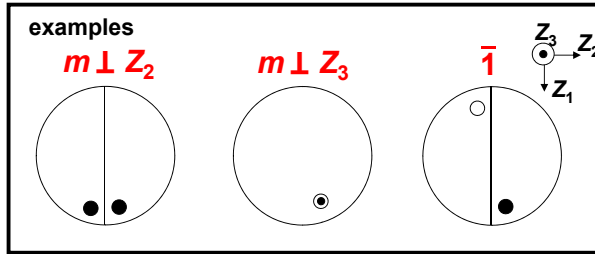
Stereographic projections

To visualize point groups, we make use of stereographic projections.

→ Easy way of representing 3D objects in 2D



1. An object located at the center of sphere
2. Any point of interest is then projected to the surface.
3. If the point ends in the northern hemisphere, then connecting it to the South Pole.
4. Where this line intersects the equatorial plane is the point on the stereographic projection.
5. Closed (open) circles identify points originating from the northern (southern) hemispheres.



32 point groups illustrated by stereograms

<p>triclinic</p>	<p>tetragonal</p>
<p>monoclinic</p>	<p>hexagonal</p>
<p>orthorhombic</p>	<p>cubic</p>
<p>trigonal</p>	

Transformation operators for symmetry elements

The 14 symmetry elements generate the 32 point group

Identity operator	$1 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	Threefold rotation (3) parallel to $[111]$	$3 // [111] \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$
Inversion center	$\bar{1} \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	Threefold inversion axis ($\bar{3}$) parallel to Z_3	$\bar{3} // Z_3 \begin{pmatrix} 1/2 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & 1/2 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Twofold rotation (2) parallel to Z_1	$2 // Z_1 \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	Threefold inversion axis ($\bar{3}$) parallel to $[111]$ in cubic crystals	$\bar{3} // [111] \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix}$
Twofold rotation (2) parallel to Z_2	$2 // Z_2 \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	Fourfold rotation (4) parallel to Z_3	$4 // Z_3 \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Mirror (m) perpendicular to Z_1	$m \perp Z_1 \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	Fourfold inversion ($\bar{4}$) parallel to Z_3	$\bar{4} // Z_3 \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Mirror (m) perpendicular to Z_2	$m \perp Z_2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	Sixfold rotation (6) parallel to Z_3	$6 // Z_3 \begin{pmatrix} 1/2 & \sqrt{3}/2 & 0 \\ -\sqrt{3}/2 & 1/2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Mirror (m) perpendicular to Z_3	$m \perp Z_3 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	Sixfold inversion ($\bar{6}$) parallel to Z_3	$\bar{6} // Z_3 \begin{pmatrix} -1/2 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & -1/2 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Threefold rotation (3) parallel to Z_3	$3 // Z_3 \begin{pmatrix} -1/2 & \sqrt{3}/2 & 0 \\ \sqrt{3}/2 & -1/2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$		

Minimum symmetry elements for the 32 point groups

Point group	Symmetry elements
1	1
1̄	1̄
2	2 // Z ₂
m	m ⊥ Z ₂
2/m	2 // Z ₂ , m ⊥ Z ₂
222	2 // Z ₁ , 2 // Z ₂
mm2	m ⊥ Z ₁ , m ⊥ Z ₂
mmm	m ⊥ Z ₁ , m ⊥ Z ₂ , m ⊥ Z ₃
3	3 // Z ₃
3̄	3̄ // Z ₃
32	3 // Z ₃ , 2 // Z ₁
3m	3 // Z ₃ , m ⊥ Z ₁
3̄m	3̄ // Z ₃ , m ⊥ Z ₁
4	4 // Z ₃
4̄	4̄ // Z ₃
4/m	4 // Z ₃ , m ⊥ Z ₃
422	4 // Z ₃ , 2 // Z ₁
4mm	4 // Z ₃ , m ⊥ Z ₁
4̄2m	4̄ // Z ₃ , 2 // Z ₁
4/mmm	4 // Z ₃ , m ⊥ Z ₃ , m ⊥ Z ₁
6	6 // Z ₃
6̄	6̄ // Z ₃
6/m	6 // Z ₃ , m ⊥ Z ₃
622	6 // Z ₃ , 2 // Z ₁
6mm	6 // Z ₃ , m ⊥ Z ₁
6̄m2	6̄ // Z ₃ , m ⊥ Z ₁
6/mmm	6 // Z ₃ , m ⊥ Z ₃ , m ⊥ Z ₁
23	2 // Z ₁ , 3 // [111]
m3	m ⊥ Z ₁ , 3 // [111]
432	4 // Z ₃ , 3 // [111]
4̄3m	4̄ // Z ₃ , 3 // [111]
m3m	m ⊥ Z ₁ , 3 // [111], m ⊥ [110]



Tensors and physical properties

We introduce the tensor description of physical properties relating symmetry to physical properties.

Tensors are defined by the way in which they transform from one coordinate system to another.

Measured quantities such as **STRESS** & **STRAIN** can be represented by tensors.

elastic compliance

Tensors are useful in describing anisotropy of physical properties.

Polar tensors & Axial tensors

→ Their transformation laws are slightly different.

Polar tensors

For a polar tensor, the general transformation law for a tensor of rank N is

$$T'_{ijk\dots} = a_{il}a_{jm}a_{kn}\dots T_{lmn\dots},$$

$$\left(\begin{array}{l} T'_{ijk\dots}; \text{ tensor component in new axial system,} \\ a_{il}a_{jm}a_{kn}\dots; \text{ direction cosines,} \\ T_{lmn\dots}, \text{ tensor component in old system} \end{array} \right)$$

$$\begin{aligned} T' &= T \\ T'_i &= a_{ij}T_j \\ T'_{ij} &= a_{ik}a_{jl}T_{kl} \\ T'_{ijk} &= a_{il}a_{jm}a_{kn}T_{lmn} \end{aligned}$$

Each tensor component has N subscripts and there are N direction cosines involved in the product $a_{il}a_{jm}a_{kn}\dots$

Meaning of the tensor rank N

→ Number of directions involved in measuring the properties

Example; (Thermal conductivity k relates heat flow h to T -gradient dT/dZ)

$$h_i = -k_{ij} (dT/dZ_j) \quad (2 \text{ directions in measuring } k)$$



h_i and dT/dZ_j are first rank polar tensor quantities, while the thermal conductivity k is a second rank tensor property.

belongs to materials

k depends on the symmetry of the material, whereas the heat flow and temperature gradient do not.

Tensor rank of other physical properties

Pyroelectricity p ; a relationship between thermal & electric variables



A change in temperature ΔT creates a change in electric polarization P .

Polarization → vector (= first rank tensor)

Temperature → scalar (= zero rank tensor)

$$P_i = p_i \Delta T \quad (\text{pyroelectric coefficient } p_i; \text{ first rank tensor property})$$

Rank	Polar tensor property	
Zero	Specific heat	$C = (\Delta Q/\Delta T)$
First	Pyroelectricity	$P_i = p_i \Delta T$
Second	Thermal expansion	$x_{ij} = \alpha_{ij} \Delta T$
Third	Piezoelectricity	$P_j = d_{jki} x_{ki}$

The symmetry of any physical property of a crystal must include the symmetry elements of the point group of the crystal.



The measurements made in symmetry-related directions will give the same property coefficient.

Pyroelectricity

The name is derived from the Greek *pyr*, fire, and electricity.

Pyroelectricity p is a first rank tensor property relating a change electric polarization P to a change in temperature δT . The defining relation can also be written in terms of the electric displacement D since no field is applied.

$$P_i = D_i = p_i \delta T \quad [C/m^2]$$

$$p_i = a_{ij} p_j$$

Symmetry limitations for pyroelectricity (rank 1)

Pyroelectricity disappears in all centrosymmetric materials.

For a first rank tensor there are 3 nonzero coefficients, p_1 , p_2 , & p_3 .

Tensor coefficients are often written in matrix form:

$$\begin{matrix} 3 \times 1 & 3 \times 3 & 3 \times 1 \\ (p') & = & (a) (p) \end{matrix}$$

$(p') = (p)$ If the direction cosine matrix (a) is a symmetry element of material.

For the **inversion** symmetry operation we have

$$(p') = \begin{pmatrix} p_1' \\ p_2' \\ p_3' \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix} = \begin{pmatrix} -p_1 \\ -p_2 \\ -p_3 \end{pmatrix} = -(p)$$

$$\begin{pmatrix} -p_1 \\ -p_2 \\ -p_3 \end{pmatrix} = \begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix}$$

which is only satisfied if all 3 pyroelectric coefficients are zero: $p_1 = p_2 = p_3 = 0$

Pyroelectricity disappears in all point groups containing inversion symmetry.

Example

Is LiNbO_3 (point group $3m$) pyroelectric or not?

If yes, which pyroelectric coefficient p_i can be finite?

Symmetry elements for $3m$

$$3 \parallel Z_3 \begin{pmatrix} -1/2 & \sqrt{3}/2 & 0 \\ -\sqrt{3}/2 & -1/2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad m \perp Z_1 \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$(p') = (a) (p)$

$$p_1' = -1/2 p_1 + \sqrt{3}/2 p_2$$

$$p_2' = -\sqrt{3}/2 p_1 - 1/2 p_2$$

$$p_3' = p_3$$

$$p_1' = -p_1 \rightarrow p_1 = 0$$

$$p_2' = p_2$$

$$p_3' = p_3$$

$$p_2' = -1/2 p_2$$

$$p_2 = 0$$

p_3 can be finite.

by Neumann's Principle,
If the transformation matrix is
for symmetry operation,
 $(p') = (p)$.

3m is pyroelectric

with $\begin{pmatrix} 0 \\ 0 \\ p_3 \end{pmatrix}$

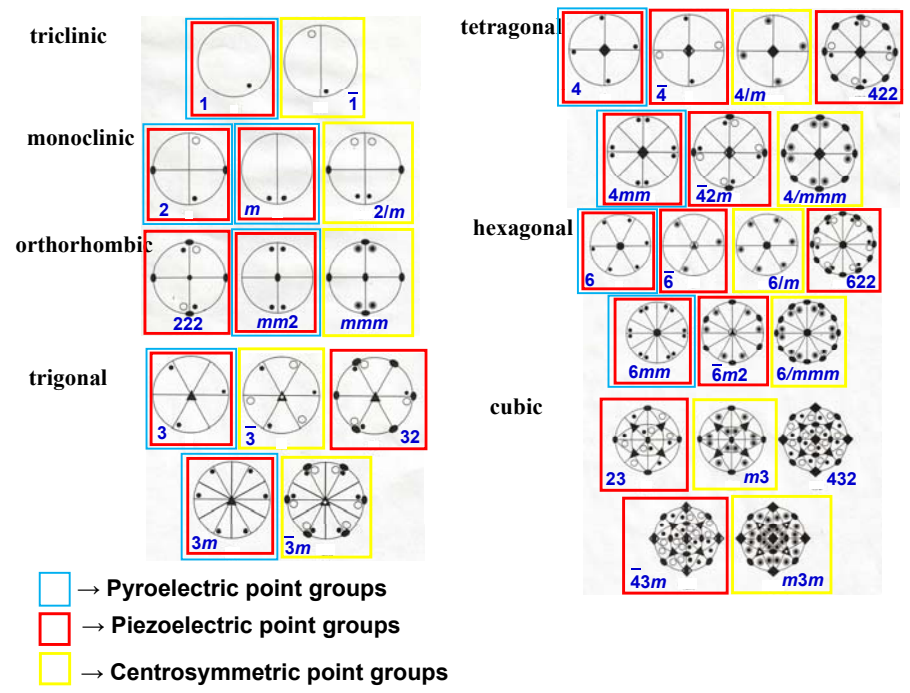
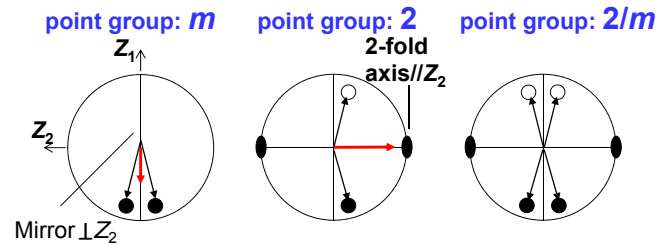
Polar axes

Pyroelectric matrices for 10 pyroelectric point groups

The direction of the polar axis is fixed by symmetry.

It is easy to visualize the polar axis directions by examining stereographic projections.

Point group	$\begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix}$
1	$\begin{pmatrix} p_1 \\ p_2 \\ p_3 \end{pmatrix}$
2	$\begin{pmatrix} 0 \\ p_2 \\ 0 \end{pmatrix}$
m	$\begin{pmatrix} p_1 \\ 0 \\ p_3 \end{pmatrix}$
mm2, 3, 3m	$\begin{pmatrix} 0 \\ 0 \\ p_3 \end{pmatrix}$
4, 4mm, 6	$\begin{pmatrix} 0 \\ 0 \\ p_3 \end{pmatrix}$
6mm	$\begin{pmatrix} p_3 \end{pmatrix}$



 → Pyroelectric point groups
 → Piezoelectric point groups
 → Centrosymmetric point groups

Axial tensor

Several properties change sign when the axial system changes from right-handed to left-handed.

(e.g. pyromagnetism, Hall effect ...)



Axial tensors → depends on handedness

Axial tensors transform in the following manner,

$$T'_{ijk\dots} = |a| a_{il} a_{jm} a_{kn} \dots T_{lmn\dots},$$

Determinant of the direction cosines matrix

$|a| = +1$ or -1 depending on whether or not the handedness of the axial system changes during transformation

(For mirror or inversion symmetry operations, $|a| = -1$ i.e. the sign of the tensor coefficient changes.)

Magnetolectricity → a second rank axial tensor properties

A most familiar examples of tensors : vectors (the 1st rank tensors)

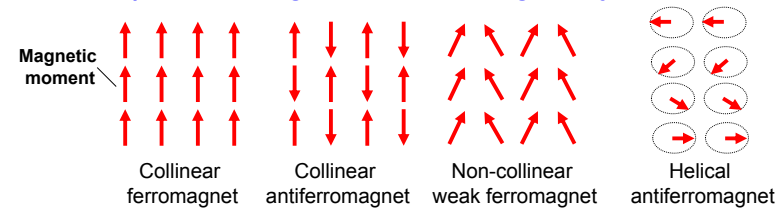
	Polar vectors	Axial vectors
characteristics	Displacement (directed segment of length, that is, arrow)	Vector product of two polar tensors (the directional properties of element of area, rather than arrow)
examples	electric polarization P electric field E	magnetic moment M magnetic field H
The direction which arrow points (i.e. sign) under handedness change	change	Not change
Effect of inversion operation	Vector which breaks inversion symmetry	Vector which preserves inversion symmetry

Outline of this lecture

- Symmetry in crystals
- **Magnetic symmetry**
- Conventional magnetoelectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites $RMnO_3$
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- ME effect in magnetically-disordered system

Symmetries & tensors related to magnetic phenomena

Representative magnetic structures in magnetically ordered materials

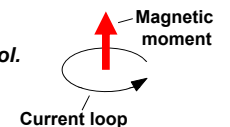


Geometric representations are helpful in determining the effect of symmetry on physical properties.

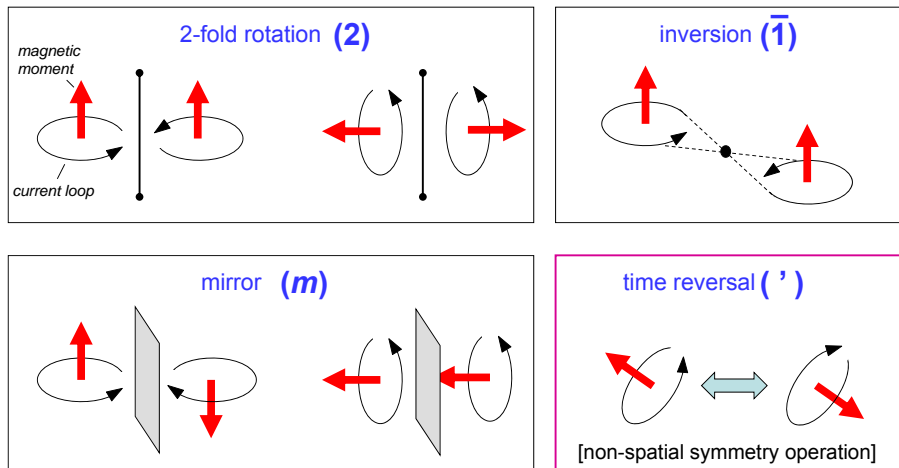
Magnetic moments are often visualized as arrows, but this is somewhat misleading.



Magnetization arises from moving electric charge so that a current loop is more meaningful symbol.

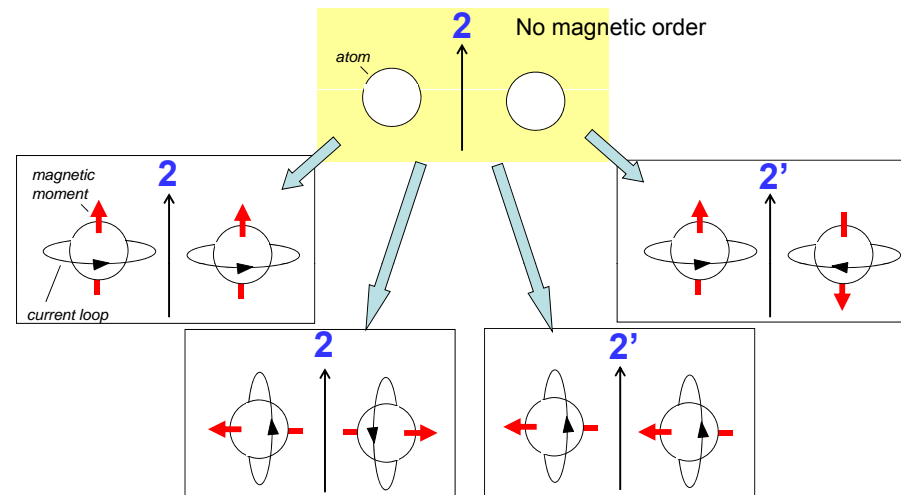


Transformations of a current loop (magnetic moment) under 4 symmetry operations



In addition to rotation, mirror inversion operations, **time reversal operation** can be a symmetry operation in magnetically ordered materials.

Simple examples of magnetic point groups



Introduction of the time reversal operator increases the number of classes by adding 90 additional **magnetic point groups**.

Discussing magnetic symmetry

When discussing magnetic symmetry, it is necessary to distinguish the crystallographic point groups from the magnetic point groups.

2/m1' : crystallographic group

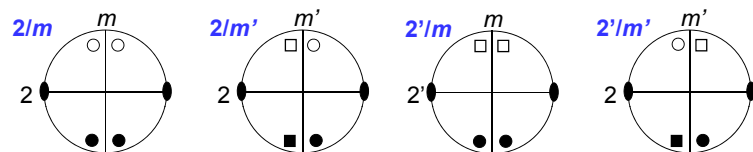
(containing both the regular & time-reversed symmetry elements)

4 magnetic point groups associated with crystallographic group 2/m1'

- 2/m** : containing 2, m, & $\bar{1}$, but not 2', m', and $\bar{1}'$
- 2/m'** : containing 2, m', & $\bar{1}'$
- 2'/m** : containing 2', m, & $\bar{1}$
- 2'/m'** : containing 2', m', & $\bar{1}'$

Stereograms of the 4 magnetic point groups

Square & circular symbols represent points related by time reversal.



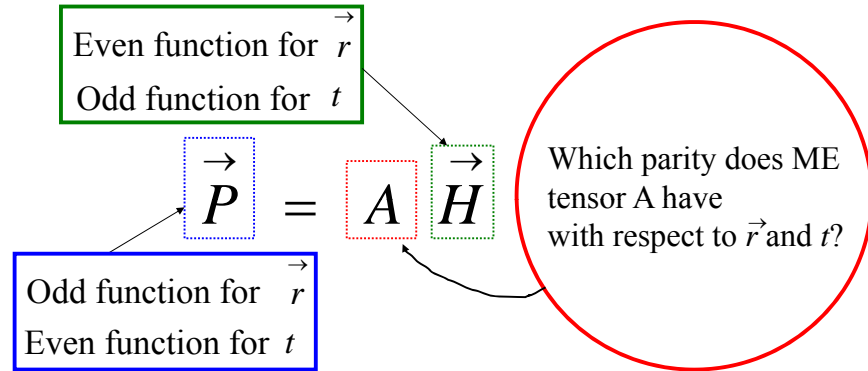
List of magnetic point groups

Generating elements		Tetragonal		Hexagonal	
Triclinic	4(9) 1	5(3) 4 Z ₃	6(5) 6 Z ₃	6(5) 6 Z ₃	6(5) 6 Z ₃
	0 $\bar{1}$	4(2) 4' Z ₃	6(6) 6' Z ₃	6(6) 6' Z ₃	6(6) 6' Z ₃
	0 $\bar{1}'$	4(2) 4 Z ₃	6(6) 6 Z ₃	6(6) 6 Z ₃	6(6) 6 Z ₃
	9(9) $\bar{1}'$	5(3) 4' Z ₃	6(6) 6' Z ₃	6(6) 6' Z ₃	6(6) 6' Z ₃
Monoclinic	2 5(5) 2 Z ₂	4/m 0 m ⊥ Z ₃ , 4 Z ₃	6/m 0 m ⊥ Z ₃ , 6 Z ₃	6/m 0 m ⊥ Z ₃ , 6 Z ₃	6/m 0 m ⊥ Z ₃ , 6 Z ₃
	2' 4(4) 2' Z ₂	4'/m 0 m' ⊥ Z ₃ , 4' Z ₃	6'/m 0 m' ⊥ Z ₃ , 6' Z ₃	6'/m 0 m' ⊥ Z ₃ , 6' Z ₃	6'/m 0 m' ⊥ Z ₃ , 6' Z ₃
	m 4(4) m ⊥ Z ₂	4/m' 5(3) m' ⊥ Z ₃ , 4 Z ₃	6/m' 5(3) m' ⊥ Z ₃ , 6 Z ₃	6/m' 5(3) m' ⊥ Z ₃ , 6 Z ₃	6/m' 5(3) m' ⊥ Z ₃ , 6 Z ₃
	m' 5(5) m' ⊥ Z ₂	4/m' 4(2) m' ⊥ Z ₃ , 4' Z ₃	6/m' 4(2) m' ⊥ Z ₃ , 6' Z ₃	6/m' 4(2) m' ⊥ Z ₃ , 6' Z ₃	6/m' 4(2) m' ⊥ Z ₃ , 6' Z ₃
	2/m 0 2 Z ₂ , m ⊥ Z ₂	422 3(2) 2 Z ₁ , 4 Z ₃	622 3(2) 2 Z ₁ , 6 Z ₃	622 3(2) 2 Z ₁ , 6 Z ₃	622 3(2) 2 Z ₁ , 6 Z ₃
	2'/m' 0 2' Z ₂ , m' ⊥ Z ₂	4'22 2(1) 2' Z ₁ , 4' Z ₃	6'22' 2(1) 2' Z ₁ , 6' Z ₃	6'22' 2(1) 2' Z ₁ , 6' Z ₃	6'22' 2(1) 2' Z ₁ , 6' Z ₃
	2/m' 5(5) 2 Z ₂ , m' ⊥ Z ₂	42'2' 2(1) 2' Z ₁ , 4' Z ₃	62'2' 2(1) 2' Z ₁ , 6' Z ₃	62'2' 2(1) 2' Z ₁ , 6' Z ₃	62'2' 2(1) 2' Z ₁ , 6' Z ₃
	2'/m 4(4) 2' Z ₂ , m ⊥ Z ₂	4mm 2(1) m ⊥ Z ₁ , 4 Z ₃	6mm 2(1) m ⊥ Z ₁ , 6 Z ₃	6mm 2(1) m ⊥ Z ₁ , 6 Z ₃	6mm 2(1) m ⊥ Z ₁ , 6 Z ₃
		4mm' 2(1) m' ⊥ Z ₁ , 4' Z ₃	6mm' 2(1) m' ⊥ Z ₁ , 6' Z ₃	6mm' 2(1) m' ⊥ Z ₁ , 6' Z ₃	6mm' 2(1) m' ⊥ Z ₁ , 6' Z ₃
Orthorhombic	222 3(3) 2 Z ₂ , 2 Z ₃	4m' m' 3(2) m' ⊥ Z ₁ , 4' Z ₃	6m' m' 3(2) m' ⊥ Z ₁ , 6' Z ₃	6m' m' 3(2) m' ⊥ Z ₁ , 6' Z ₃	6m' m' 3(2) m' ⊥ Z ₁ , 6' Z ₃
	2'2'2 2(2) 2' Z ₂ , 2' Z ₃	42m 2(1) 2' Z ₁ , 4' Z ₃	62m 2(1) 2' Z ₁ , 6' Z ₃	62m 2(1) 2' Z ₁ , 6' Z ₃	62m 2(1) 2' Z ₁ , 6' Z ₃
	mm2 2(2) m ⊥ Z ₂ , 2 Z ₃	4'2m' 2(1) 2' Z ₁ , 4' Z ₃	6'2m' 2(1) 2' Z ₁ , 6' Z ₃	6'2m' 2(1) 2' Z ₁ , 6' Z ₃	6'2m' 2(1) 2' Z ₁ , 6' Z ₃
	m' m' 2 3(3) m' ⊥ Z ₂ , 2 Z ₃	42m' 2(1) 2' Z ₁ , 4' Z ₃	62m' 2(1) 2' Z ₁ , 6' Z ₃	62m' 2(1) 2' Z ₁ , 6' Z ₃	62m' 2(1) 2' Z ₁ , 6' Z ₃
	m' m' 2' 2(2) m' ⊥ Z ₂ , 2' Z ₃	4/mmm 0 m ⊥ Z ₁ , m ⊥ Z ₂ , 4 Z ₃	6/mmm 0 m ⊥ Z ₁ , m ⊥ Z ₂ , 6 Z ₃	6/mmm 0 m ⊥ Z ₁ , m ⊥ Z ₂ , 6 Z ₃	6/mmm 0 m ⊥ Z ₁ , m ⊥ Z ₂ , 6 Z ₃
	mmm 0 m' ⊥ Z ₁ , m' ⊥ Z ₂ , m ⊥ Z ₃	4'/mmm' 0 m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/mmm' 0 m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/mmm' 0 m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/mmm' 0 m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	m' m' m' 3(3) m' ⊥ Z ₁ , m' ⊥ Z ₂ , m' ⊥ Z ₃	4/m' m' m' 3(2) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6/m' m' m' 3(2) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6/m' m' m' 3(2) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6/m' m' m' 3(2) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	m' m' m' 2(2) m' ⊥ Z ₁ , m' ⊥ Z ₂ , m' ⊥ Z ₃	4/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
Trigonal	3 5(3) 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3 0 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3' 5(3) 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	32 3(2) 2 Z ₁ , 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	32' 2(1) 2' Z ₁ , 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3m 2(1) m ⊥ Z ₁ , 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3m' 3(2) m' ⊥ Z ₁ , 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3m 2(1) m ⊥ Z ₁ , 3 Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3m' 0 m' ⊥ Z ₁ , 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3'm' 3(2) m' ⊥ Z ₁ , 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3'm 0 m' ⊥ Z ₁ , 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃
	3'm 0 m' ⊥ Z ₁ , 3' Z ₃	4'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 4' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃	6'/m' m' m' 2(1) m' ⊥ Z ₁ , m' ⊥ Z ₂ , 6' Z ₃



Number of nonzero magnetoelectric coefficient

Why both I and R must be broken for 1st order ME effect?



$$\vec{P} = A \vec{H} \dots \textcircled{1}$$

System which I is preserved
i.e. which have I in symmetry
operation $IA \rightarrow A$

System which R is preserved
i.e. which have R in
symmetry operation $RA \rightarrow A$

By applying I to both sides in $\textcircled{1}$

$$I \vec{P} = I (A \vec{H})$$

$$\Leftrightarrow I \vec{P} = (IA) (I \vec{H})$$

$$\Leftrightarrow -\vec{P} = A \vec{H} \dots \textcircled{2}$$

From $\textcircled{1}$ & $\textcircled{2}$ $A \equiv 0$

By applying R to both sides in $\textcircled{1}$

$$R \vec{P} = R (A \vec{H})$$

$$\Leftrightarrow R \vec{P} = (RA) (R \vec{H})$$

$$\Leftrightarrow \vec{P} = A (-\vec{H}) \dots \textcircled{3}$$

From $\textcircled{1}$ & $\textcircled{3}$ $A \equiv 0$

Thus, both I & R must be broken to have a finite A .

Axial tensor properties

Several properties change sign
when the axial system changes from right-handed to left-handed.

(e.g. pyromagnetism, Hall effect ...)



Axial tensors \longrightarrow depends on handedness

Axial tensors transform in the following manner,

$$T'_{ijk\dots} = |a| a_{il} a_{jm} a_{kn} \dots T_{lmn\dots}$$

Determinant of the direction cosines matrix

$|a| = +1$ or -1 depending on whether or not the handedness of
the axial system changes during transformation

(For mirror or inversion symmetry operations, $|a| = -1$
i.e. the sign of the tensor coefficient changes.)

Magnetolectricity \longrightarrow a second rank axial tensor properties

$$M_i = \alpha_{ij} E_j$$

M_i is linearly proportional to the applied electric field E_j
through the magnetolectric coefficients Q_{ij} .

Since E is a polar first rank tensor & M is an axial first rank tensor,
the magnetolectric effect is an axial second rank tensor which transforms as follows.

$$M'_i = \pm |a| a_{ij} M_j = \pm |a| a_{ij} \alpha_{jk} E_k$$

$$= \pm |a| a_{ij} \alpha_{jk} a_{lk} E'_l = \alpha'_{il} E'_l \quad \Rightarrow \quad \alpha'_{il} = \pm |a| a_{ij} \alpha_{jk} a_{lk}$$

In matrix form, the linear magnetolectric effect transforms in a similar way
in going from the old system to the new system.

$$(M') = \pm |a| (a) (M) = \pm |a| (a) (\alpha) (E)$$

$$= \pm |a| (a) (\alpha) (a)_t (E') = (\alpha') (E')$$

The ME effect vanishes for all symmetry groups containing time reversal symmetry ($\bar{1}$).

$$(\alpha') = (-1)(+1)(+1)(\alpha)(+1) = (-\alpha) = (\alpha) = 0$$

The ME effect also disappears for ordinary inversion symmetry ($\bar{1}$) operations.

$$(\alpha') = (+1)(-1)(-1)(\alpha)(-1) = (-\alpha) = (\alpha) = 0$$

For space inversion accompanied by time inversion ($\bar{1}$), the ME effect is permitted.

$$(\alpha') = (-1)(-1)(-1)(\alpha)(-1) = (\alpha) = (\alpha)$$

First magnetoelectric material: Cr₂O₃

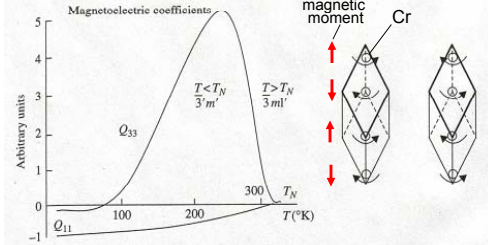
Crystal structure: corundum (=Al₂O₃)

Antiferromagnet with T_N = 307 K

Magnetic point group: $\bar{3}'m'$

Generating elements

$m' \perp Z_1, \bar{3}' \parallel Z_3$



$\bar{3}' \parallel Z_3$

Time reversal

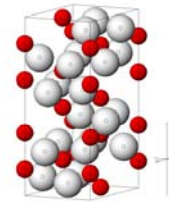
Handedness change by inversion

$$\begin{pmatrix} Q'_{11} & Q'_{12} & Q'_{13} \\ Q'_{21} & Q'_{22} & Q'_{23} \\ Q'_{31} & Q'_{32} & Q'_{33} \end{pmatrix} = (-1)(-1) \begin{pmatrix} 1/2 & -\sqrt{3}/2 & 0 \\ \sqrt{3}/2 & 1/2 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{22} & Q_{23} \\ 0 & Q_{32} & Q_{33} \end{pmatrix} \begin{pmatrix} 1/2 & \sqrt{3}/2 & 0 \\ -\sqrt{3}/2 & 1/2 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

$$= \begin{pmatrix} (1/4 Q_{11} + 3/4 Q_{22}) & (-\sqrt{3}/4 Q_{11} + \sqrt{3}/4 Q_{22}) & (\sqrt{3}/2 Q_{23}) \\ (\sqrt{3}/4 Q_{11} - \sqrt{3}/4 Q_{22}) & (3/4 Q_{11} + 1/4 Q_{22}) & (-1/2 Q_{23}) \\ (\sqrt{3}/2 Q_{32}) & (-1/2 Q_{32}) & (Q_{33}) \end{pmatrix}$$

$$= \begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{22} & Q_{23} \\ 0 & Q_{32} & Q_{33} \end{pmatrix}$$

This equality can be satisfied if $Q_{11} = Q_{22}$ & $Q_{23} = Q_{32} = 0$



Therefore the magnetoelectric matrix for point group $\bar{3}'m'$ is

$$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{11} & 0 \\ 0 & 0 & Q_{33} \end{pmatrix}$$

$m' \perp Z_1$

Time reversal

Handedness change by mirror

$$\begin{pmatrix} Q'_{11} & Q'_{12} & Q'_{13} \\ Q'_{21} & Q'_{22} & Q'_{23} \\ Q'_{31} & Q'_{32} & Q'_{33} \end{pmatrix} = (-1)(-1) \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} Q_{11} & Q_{12} & Q_{13} \\ Q_{21} & Q_{22} & Q_{23} \\ Q_{31} & Q_{32} & Q_{33} \end{pmatrix} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} Q_{11} & -Q_{12} & -Q_{13} \\ -Q_{21} & Q_{22} & Q_{23} \\ -Q_{31} & Q_{32} & Q_{33} \end{pmatrix} = \begin{pmatrix} Q_{11} & Q_{12} & Q_{13} \\ Q_{21} & Q_{22} & Q_{23} \\ Q_{31} & Q_{32} & Q_{33} \end{pmatrix}$$

This equality can be satisfied if $Q_{12} = Q_{13} = Q_{21} = Q_{31} = 0$

$$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{22} & Q_{23} \\ 0 & Q_{32} & Q_{33} \end{pmatrix}$$

Magnetoelectric matrices for the magnetic point groups

1, $\bar{1}'$	$\begin{pmatrix} Q_{11} & Q_{12} & Q_{13} \\ Q_{21} & Q_{22} & Q_{23} \\ Q_{31} & Q_{32} & Q_{33} \end{pmatrix}$	4', $\bar{4}, 4'/m'$	$\begin{pmatrix} Q_{11} & Q_{12} & 0 \\ Q_{12} & -Q_{11} & 0 \\ 0 & 0 & 0 \end{pmatrix}$
2, $m', 2/m'$	$\begin{pmatrix} Q_{11} & 0 & Q_{13} \\ 0 & Q_{22} & 0 \\ Q_{31} & 0 & Q_{33} \end{pmatrix}$	32, $3m', \bar{3}'m', 422, 4m'm', \bar{4}'2m', 4/m'm'm', 622, 6m'm', \bar{6}'m'2, 6/m'm'm'$	$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{11} & 0 \\ 0 & 0 & Q_{33} \end{pmatrix}$
2', $m, 2'/m$	$\begin{pmatrix} 0 & Q_{12} & 0 \\ Q_{21} & 0 & Q_{23} \\ 0 & Q_{32} & 0 \end{pmatrix}$	4'22, $4'mm', \bar{4}2m, \bar{4}'2m', 4'/m'mm'$	$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & -Q_{11} & 0 \\ 0 & 0 & 0 \end{pmatrix}$
222, $m'm'2, m'm'm'$	$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{22} & 0 \\ 0 & 0 & Q_{33} \end{pmatrix}$	32', $3m, \bar{3}'m, 42'2', 4mm, \bar{4}'2'm, 4/m'mm, 62'2', 6mm, \bar{6}'m2', 6/m'mm$	$\begin{pmatrix} 0 & Q_{12} & 0 \\ -Q_{12} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$
22'2', $2mm, m'm2', m'mm'$	$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & Q_{23} \\ 0 & Q_{32} & 0 \end{pmatrix}$	23, $m'3, 432, \bar{4}'3m', m'3m'$	$\begin{pmatrix} Q_{11} & 0 & 0 \\ 0 & Q_{11} & 0 \\ 0 & 0 & Q_{11} \end{pmatrix}$
3, $\bar{3}', 4, \bar{4}', 4/m', 6, \bar{6}', 6/m',$	$\begin{pmatrix} Q_{11} & Q_{12} & 0 \\ -Q_{12} & Q_{11} & 0 \\ 0 & 0 & Q_{33} \end{pmatrix}$	Other magnetic groups	$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$

Only 58 magnetic point groups are magnetoelectric.

Polarization (Magnetization) induced by Magnetic (Electric) fields is restricted to magnetic symmetry.

Example; Magnetic symmetry and ME tensor in GaFeO₃ (Remeikite)

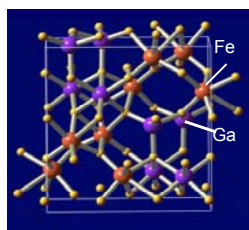
- Characteristic of crystal structure
- 4 sub-cells in a unit cell
- In each sub-cell,
 - 3 (Fe,Ga)O₆ octahedra (Ga₂,Fe₁,Fe₂)
 - 1 GaO₄ tetrahedron (Ga₁)
 - breaking space inversion sym. I
- space group: $Pc2_1n$
- ferrimagnetic (spontaneous polarization //c)
 - breaking time reversal sym. R

$$m'2'm \rightarrow \{1, RIC_{2a}, RC_{2b}, IC_{2c}\}$$

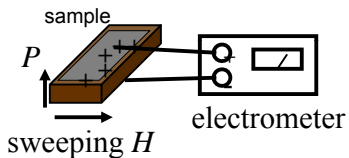
by applying these symmetry operations $\rightarrow A = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \alpha_{23} \\ 0 & \alpha_{32} & 0 \end{pmatrix}$

to $\vec{P} = A \vec{H}$

ME_H effect in conventional magnetoelectrics



GaFeO₃
pyroelectric
ferrimagnetic
m'2'm

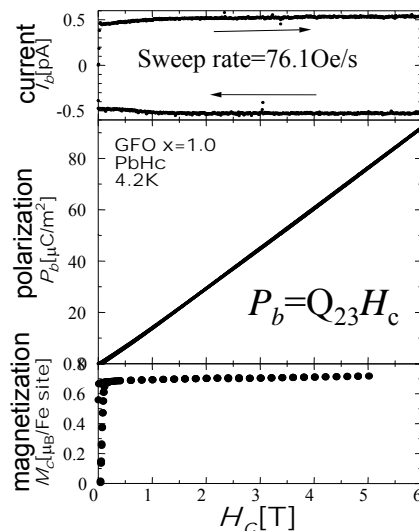


$$P = Q H$$

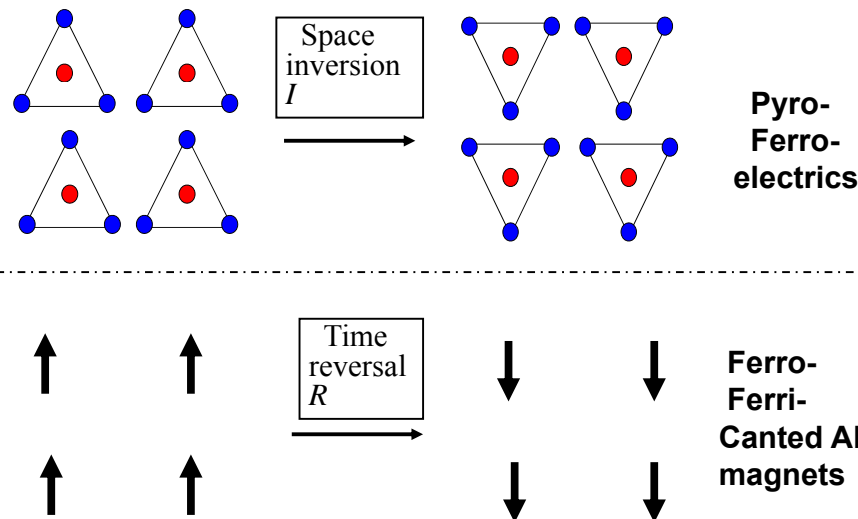
Charge
↓ t differential

$$\frac{I}{S} = \frac{1}{S} \frac{dQ}{dt} = \frac{dP}{dt} = Q \frac{dH}{dt}$$

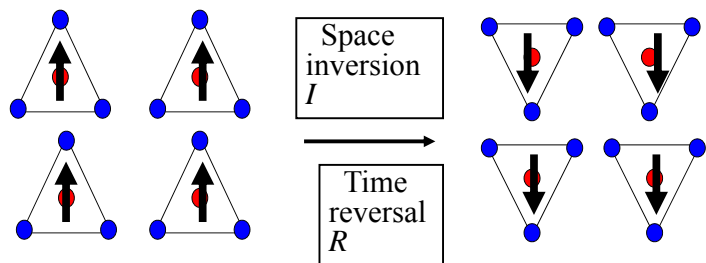
current Electrode area



System with breaking of either I & R



System with breaking of both I & R

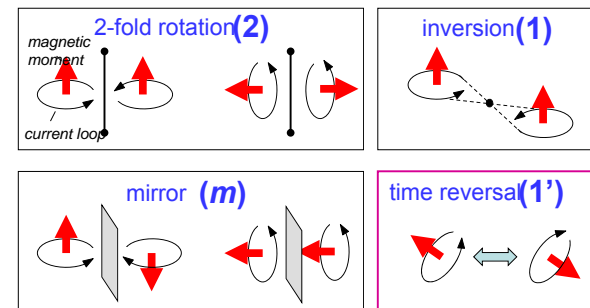


Magnetolectric Multiferroics

Important remarks by former studies

In a magnetically ordered compound,
magnetic symmetry (not fundamental crystal symmetry)
determines its **ferroelectric property**.

In noncollinear spiral spin structure,
magnetic symmetry operations are quite different from crystallographic one.



reference **Properties of Materials: Anisotropy, Symmetry, Structure**
by Robert E. Newnham, Oxford University Press (2005).

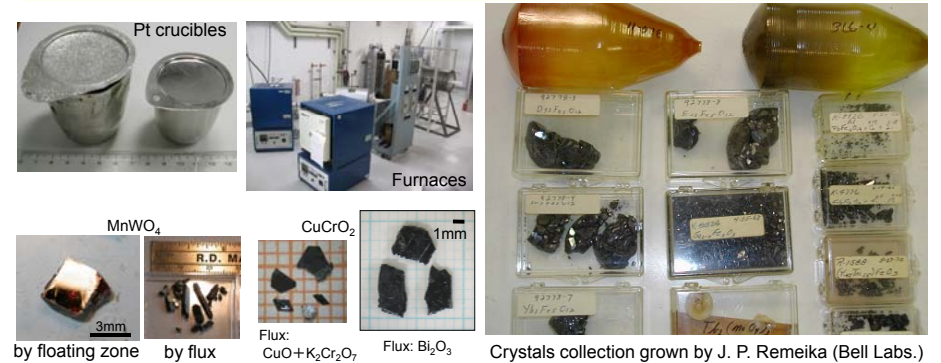
Outline of this lecture

- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetoelectric effect
- **Single crystal growth**
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites $RMnO_3$
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- ME effect in magnetically-disordered system

Single crystal growth for inorganic materials

- Directional Solidification/Bridgman Method
- Flux Method
- Czochralski growth
- Floating Zone Method
- Chemical vapor transport method

They enable growth of materials which **melt congruently**, and those that do not, and require a flux.

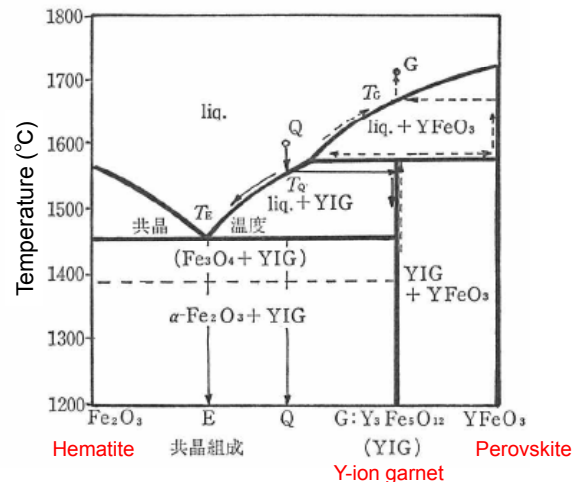


Crystals collection grown by J. P. Remeika (Bell Labs.)

Importance of phase diagram to grow single crystals

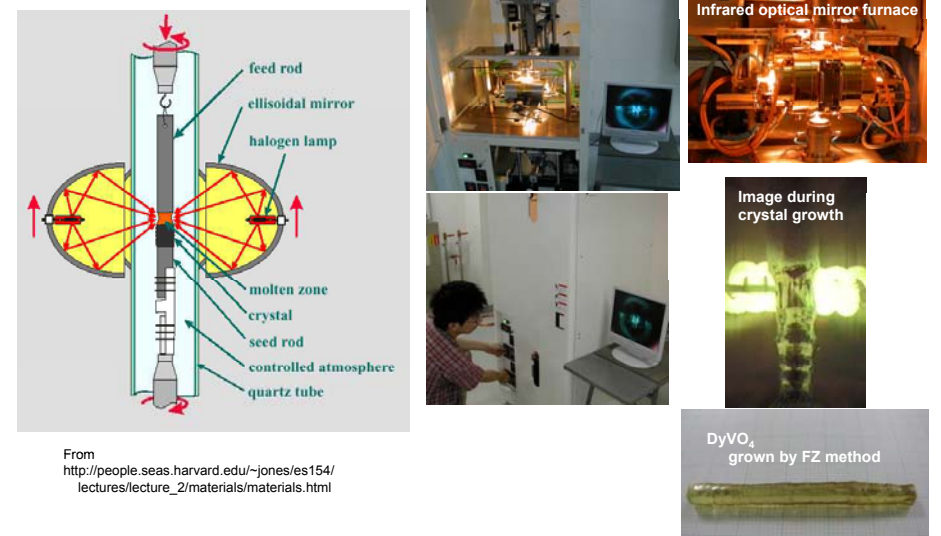
“Phase Diagrams for Ceramists” American Chemical Society

Example: Phase diagram of Fe_2O_3 - $YFeO_3$



Floating zone (FZ) method

The basic idea in float zone (FZ) crystal growth is to move a liquid zone through the material. If properly seeded, a single crystal may result.

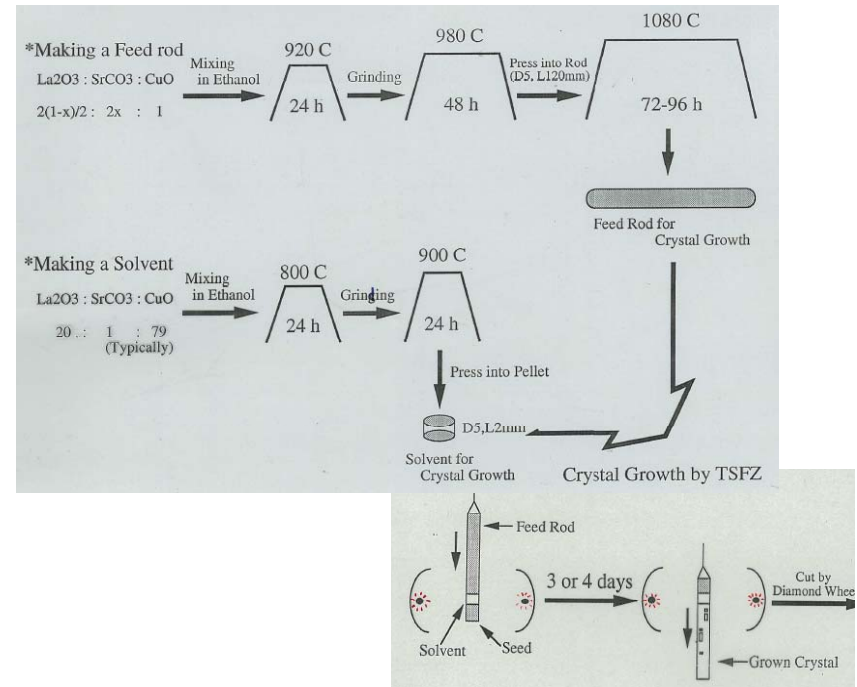
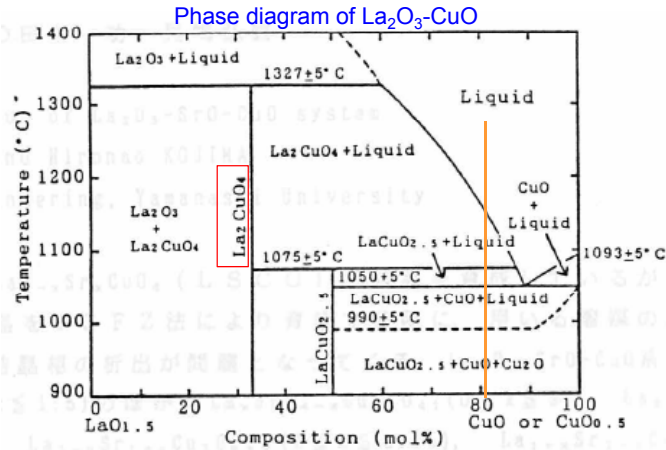


From http://people.seas.harvard.edu/~jones/es154/lectures/lecture_2/materials/materials.html

Traveling solvent floating zone (FZ) method

An effective method to grow compounds which melt incongruently.

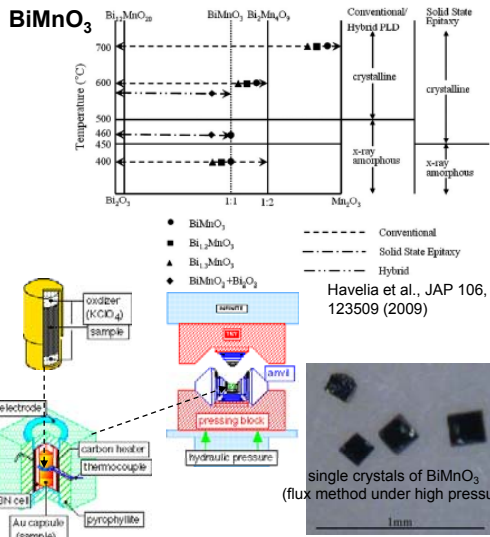
Growth of a high- T_c cuprate, $(La,Sr)_2CuO_4$



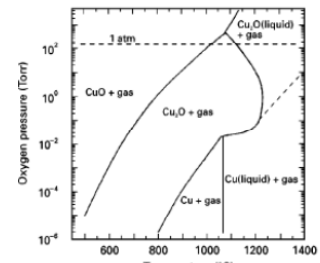
When the solid state reaction could not stabilize the formation of the focused phase,

* change the pressure.

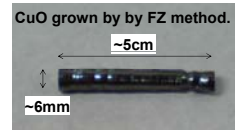
* change the oxygen partial pressure.



CuO Phase diagram of Cu-O system



Applying ~10 atm O₂ pressure makes the growth of CuO crystal.



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Classification of magnetoelectric multiferroics

Origins to induce polar structure in multiferroics

***6s² lone pair of Bi or Pb** (Seshadri & Hill Chem. Mat. 2001)

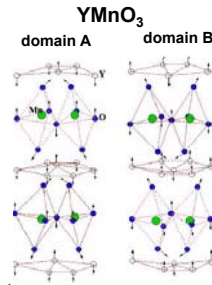
Bi³⁺ or Pb²⁺ ion with two electrons on the 6s lone pair ([Xe]4f¹⁴5d¹⁰6s²) that moves away from the centrosymmetric position in its oxygen surrounding (as in PbTiO₃).

Pb(A,B)O₃ (A=Fe, Mn, Co...; B=W, Nb...) [T_c(FE)~300~400K T_N(M)~100~200K]
BiFeO₃ [T_c(FE)~1123K T_N(M)~650K], BiMnO₃ [T_c(FE)~773K T_c(M)~110K]

***Geometric ferroelectrics** (van Aken et al. Nature Mat. 2004)

An electric dipole moment is induced by a nonlinear coupling to nonpolar lattice distortions, such as the buckling of Y-O planes and tilts of manganese-oxygen bipyramids

Hexagonal RMnO₃ (R=Y, Ho, etc.) [T_c(FE)~900K T_N(M)~100K]



***Charge ordering** (Efremov et al, Nat. Mater. 2004, Ikeda et al. Nature 2005, Tokunaga et al. Nature Mat. 2006)

LuFe₂O₄, (Pr,Ca)₃Mn₂O₇

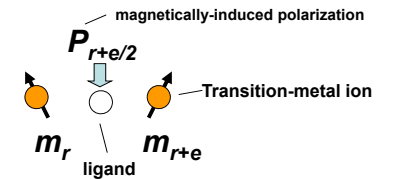
***Origins of magnetic and ferroelectric ordering are independent. (Their ferroelectric order often appears at higher temperature than magnetic one.)**

***Ferroelectricity induced by magnetic order**

Classification of magnetically-induced polarization

Cluster model composed of two transition metal ions link by ligand ion

C. Jia et al., PRB 74, 224444 (2006); PRB 76, 144424 (2007).



$$P_{r+e/2} = PMS(m_r \cdot m_{r+e})e + P^{SP}e \times (m_r \times m_{r+e}) + P^{ORB}[(e \cdot m_r)m_r - (e \cdot m_{r+e})m_{r+e}]$$

1. term from exchange striction

(Chapon et al. PRL 2006, Sergenko et al. PRL 2006)

RMn₂O₅ (R=Tb, Dy, Y, Ho, ...)

Ca₃CoMnO₆
GdFeO₃

2. term from spin current

(Katsura et al. PRL 2005, Harris PRL 2005, Mostovoy PRL 2006)

TbMnO₃
Ni₃V₂O₈
MnWO₄

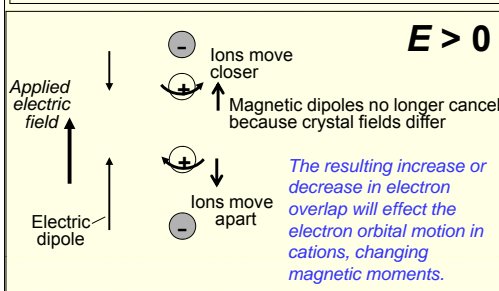
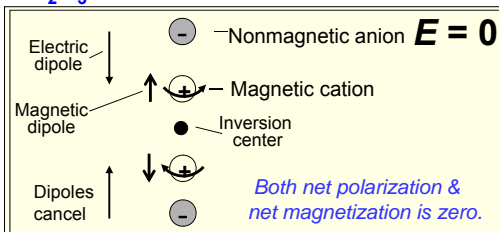
3. term from variation of p-d hybridization

(Jia et al. PRB 2006, Arima JPSJ 2007)

Cu(Fe,Al)O₂, CuCrO₂

Ferroelectricity induced by exchange striction (~J S_i · S_j)

Cr₂O₃

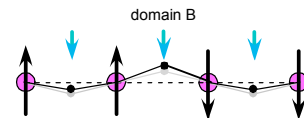


J. PHYS. SOC. JAPAN **16** (1961) 2589
Origin of Magnetoelectric Effect in Cr₂O₃

By Muneyuki DATE, Junjiro KANAMORI, and Masashi TACHIKI

Department of Physics, Osaka University, Nakanoshima, Osaka

(Received September 26, 1961)



Gray and black circles represent oxygen ions in paramagnetic and magnetically ordered phases.

Ca₃CoMnO₆ Choi et al. PRL 100, 047601 (2008)

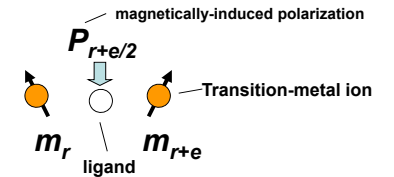
DyFeO₃, GdFeO₃

Tokunaga et al. PRL 100, 047601 (2008)
Tokunaga et al. Nat. Mat. 8, 558 (2009).

Classification of magnetically-induced polarization

Cluster model composed of two transition metal ions link by ligand ion

C. Jia et al., PRB 74, 224444 (2006); PRB 76, 144424 (2007).



$$P_{r+e/2} = PMS(m_r \cdot m_{r+e})e + P^{SP}e \times (m_r \times m_{r+e}) + P^{ORB}[(e \cdot m_r)m_r - (e \cdot m_{r+e})m_{r+e}]$$

1. term from exchange striction

(Chapon et al. PRL 2006, Sergenko et al. PRL 2006)

RMn₂O₅ (R=Tb, Dy, Y, Ho, ...)

Ca₃CoMnO₆
GdFeO₃

2. term from spin current

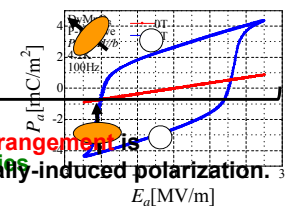
(Katsura et al. PRL 2005, Harris PRL 2005, Mostovoy PRL 2006)

TbMnO₃
Ni₃V₂O₈
MnWO₄

3. term from variation of p-d hybridization

(Jia et al. PRB 2006, Arima JPSJ 2007)

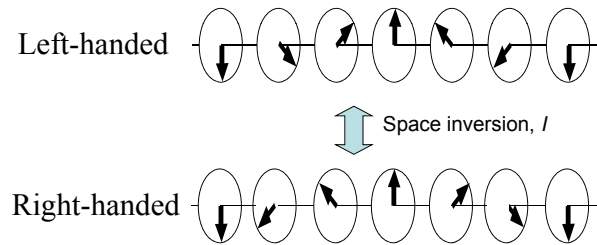
Cu(Fe,Al)O₂, CuCrO₂



Remarkable magnetic field effects on electric properties are a key for magnetically-induced polarization.

Spin spiral mechanism for multiferroics

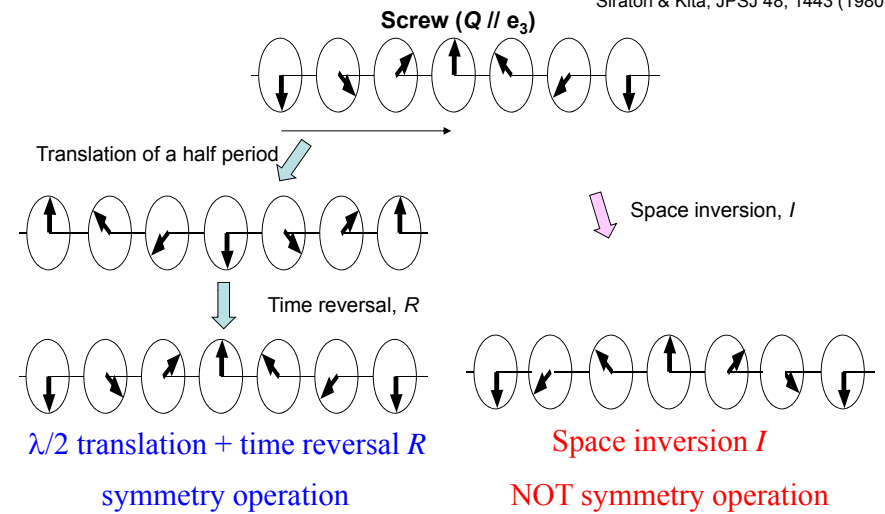
Ferroelectricity induced by a spiral magnetic order that breaks the inversion symmetry.



The origin of such ferroelectricity is driven by magnetism.

Magnetolectric effect in Screw Spiral

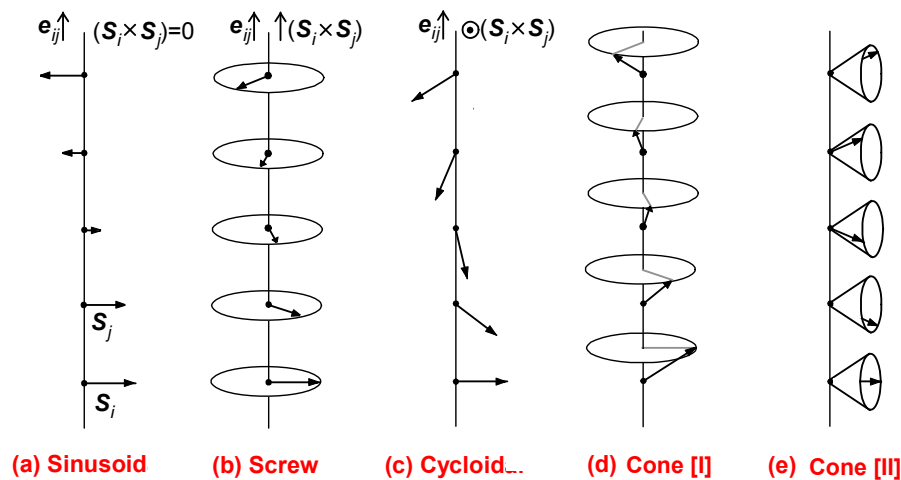
Siratori & Kita, JPSJ 48, 1443 (1980)



In screw structure, only I is broken. \Rightarrow 1st order ME tensor vanishes, But 2nd order ME tensor does exist.
 $M_i = \gamma_{ijk} H_j E_k$

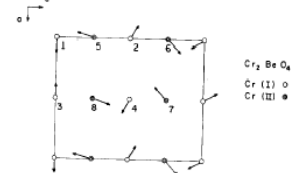
Classification of modulated spin structures

Cox, Takei, & Shirane, J. Phys. Chem. Solids 24, 405 (1963).

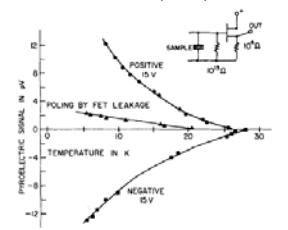


Former works studying the magnetolectric coupling in systems with spiral spin structures

$Cr_2BeO_4 [T_{C(FE)} \sim 27K]$

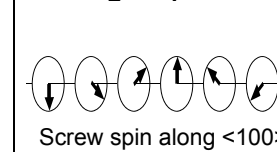


D. E. Cox et al.
 JAP 40, 1124 (1969)

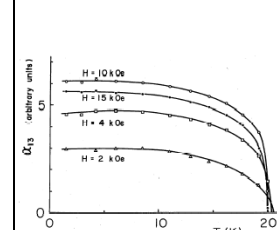


R. E. Newnham et al.
 JAP 49, 6088 (1979)

$ZnCr_2Se_4 [T_{C(FE)} \sim 20K]$

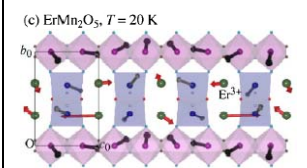


J. Akimitsu et al.
 JPSJ 44, 172 (1978)

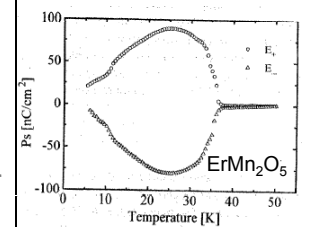


K. Shiratori & E. Kita
 JPSJ 48, 1443 (1980)

$Rm_2O_5 [T_{C(FE)} \sim 37K]$



H. Kimura, Y. Noda et al., JPSJ
 76, 074706 (2007).



Y. Koyata & K. Kohn,
 Ferroelectrics 204, 115 (1997)

Control of spin helicity by magnetoelectric cooling process & its detection by polarized neutron diffraction

JOURNAL OF THE PHYSICAL SOCIETY OF JAPAN, Vol. 48, No. 4, APRIL, 1980

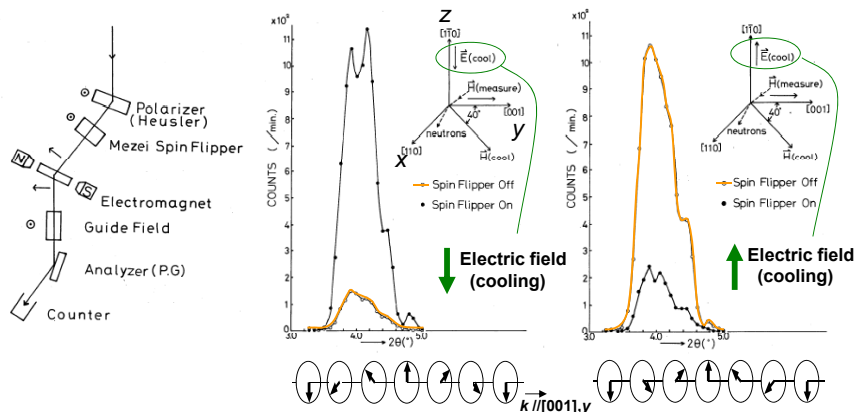


A Method of Controlling the Sense of the Screw Spin Structure

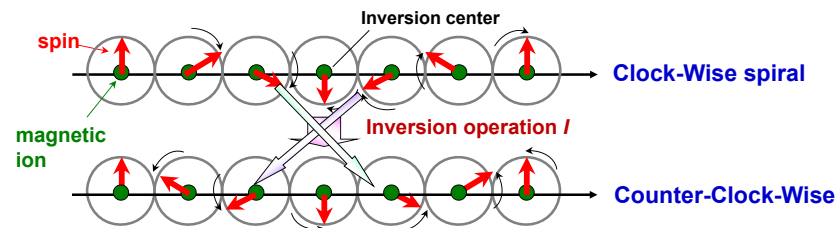
Kiiti SIRATORI, Jun AKIMITSU,† Eiji KITA and Masakazu NISHI††

Considering the magnetic symmetry of a screw spin structure, it was shown that the sense of the screw spin structure can be controlled by a magnetoelectric cooling. It was confirmed experimentally in ZnCr₂Se₄ by means of a polarized neutron diffraction.

Polarization dependence of 0,0,k₀ reflection after ME cooling



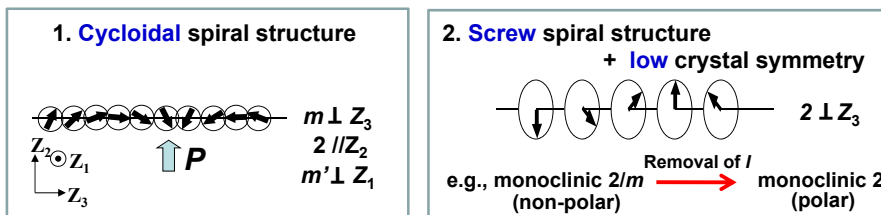
Breaking space inversion symmetry in spiral spin systems



The CW & CCW spiral structures are inverted by *I*. However, these two spiral structures are not identical.

Thus, the inversion symmetry is broken by a spiral spin order.

To make system ferroelectric,



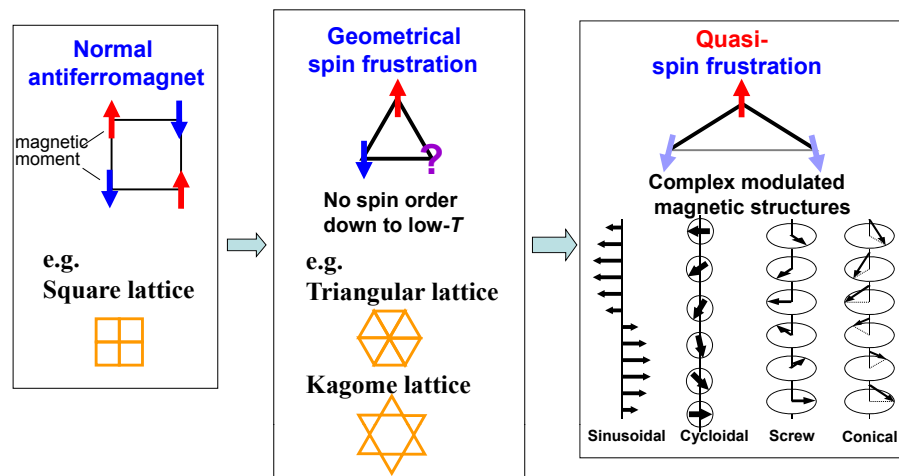
Materials design

How to produce the spiral magnetic structure

Competing magnetic interactions

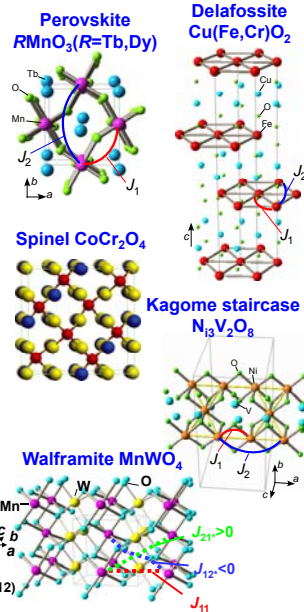
An approach to exploring new magnetoelectric multiferroics

We focus on magnetic insulators with competing magnetic interactions (spin frustration) as candidates of new multiferroics.



List of spin-spiral-driven ferroelectrics

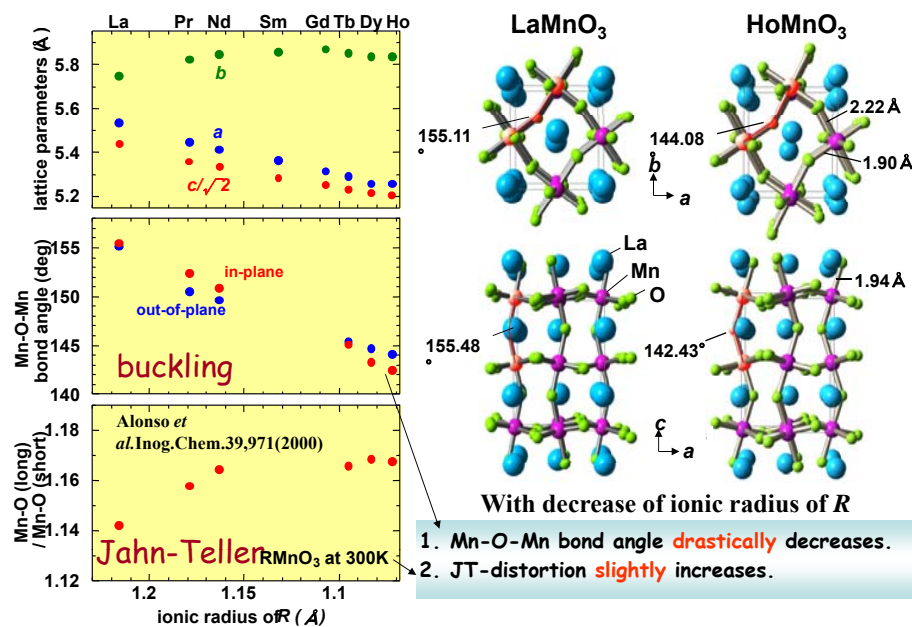
Compound	Crystal structure	Magnetic ion	Proposed spin structure	Temperature range (K)	Ref.
$RMnO_3$ ($R=Tb, \text{etc.}$)	O (mmm) [perovskite]	Mn^{2+} $S=2$	cycloidal	≤ 28	Kimura <i>et al.</i> (2003)
$Ni_3V_2O_8$	O (mmm)	Ni^{2+} $S=1$	cycloidal	3.9–6.3	Lawes <i>et al.</i> (2005)
$(Ba,Sr)_2M_2Fe_{12}O_{22}$	R ($-3m$) [haxaferrite]	Fe^{3+} $S=5/2$	screw, L-conical ($\beta=0$) T-conical ($\beta>0$)	≤ -110	Kimura <i>et al.</i> (2005)
$CuFeO_2$	R ($-3m$) [delafossite]	Fe^{3+} $S=5/2$	collinear ($\beta=0$) screw ($\beta>0$)	≤ 11	Kimura <i>et al.</i> (2005)
$CoCr_2O_4$	C ($m3m$) [spinel]	Co^{2+} Cr^{3+} $S=3/2$ $S=3/2$	T-conical	≤ 26	Yamasaki <i>et al.</i> (2006)
$MnWO_4$	M ($2/m$) [wolframite]	Mn^{2+} $S=5/2$	cycloidal	7–12.5	Taniguchi <i>et al.</i> (2006)
$RbFe(MoO_4)_2$	R ($-3m$)	Fe^{3+} $S=5/2$	screw	≤ 3.8	Kenzelmann <i>et al.</i> (2006)
$LiCu_2O_2$	O (mmm)	Cu^{2+} $S=1/2$	cycloidal	≤ 23	Park <i>et al.</i> (2007)
$LiCuVO_4$	O (mmm)	Cu^{2+} $S=1/2$	cycloidal	≤ 2.4	Naito <i>et al.</i> (2007)
CuO	M ($2/m$) [tenorite]	Cu^{2+} $S=1/2$	cycloidal + screw	212–230	Kimura <i>et al.</i> (2008)
$ACrO_2$ ($A=Ag, Cu$)	R ($-3m$) [delafossite]	Cr^{3+} $S=3/2$	screw	≤ 24	Seki <i>et al.</i> (2008)
$FeVO_4$	Tri (-1)	Fe^{3+} $S=5/2$	cycloidal	≤ 16	Daoud-Aladine <i>et al.</i> (2009)
$CuCl_2$	M ($2/m$) [distorted CdI ₂]	Mn^{2+} $S=5/2$	cycloidal	≤ 24	Seki <i>et al.</i> (2010)
Mn_2GeO_4	O (mmm) [olivine]	Mn^{2+}	cycloidal	< 5.5	White <i>et al.</i> (2012)



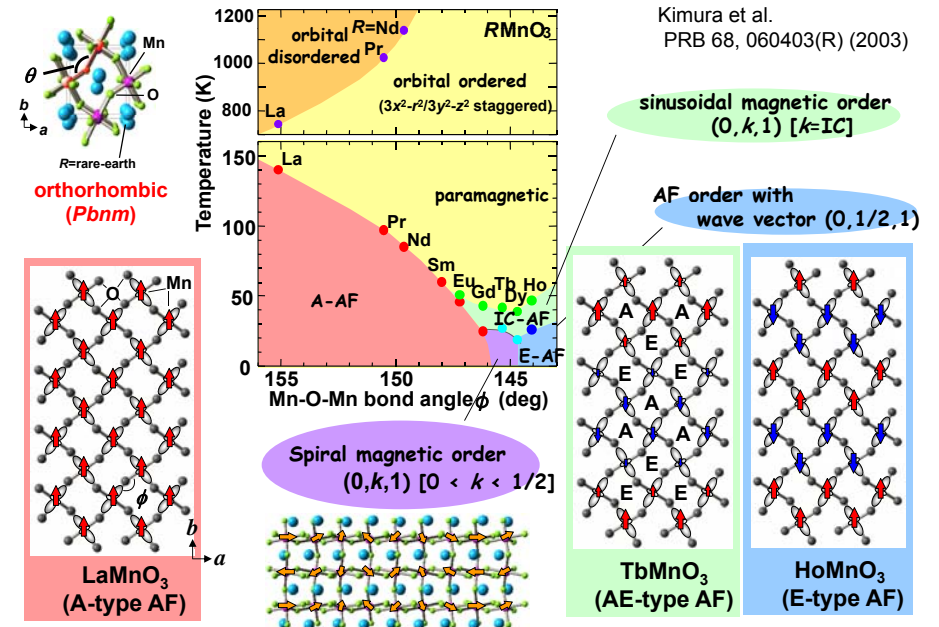
Outline of this lecture

- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetoelectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites $RMnO_3$
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- ME effect in magnetically-disordered system

Change in lattice distortion in $RMnO_3$ (all of them are $Pbnm$ orthorhombic)



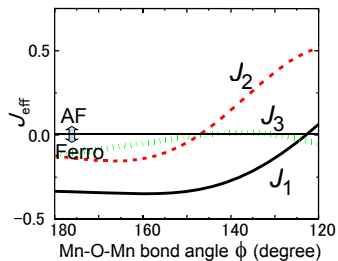
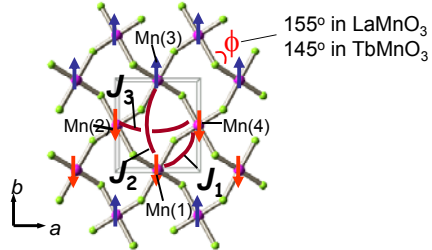
Complex phase diagram & variety of phases in perovskite manganites $RMnO_3$



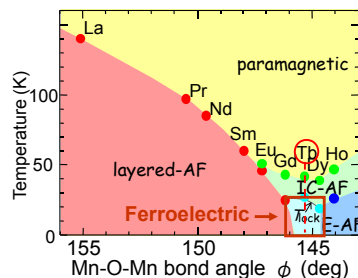
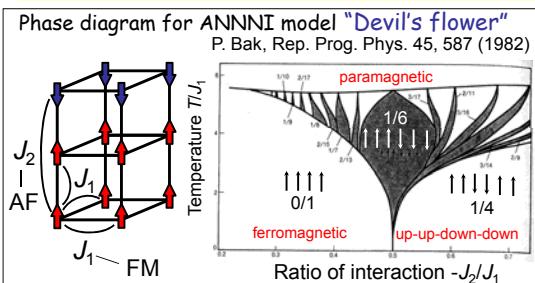
Competing magnetic interactions in RMnO_3

MnO₂ plane in perovskite manganite

Kimura, Ishihara et al. PRB 68, 060403(R) (2003)

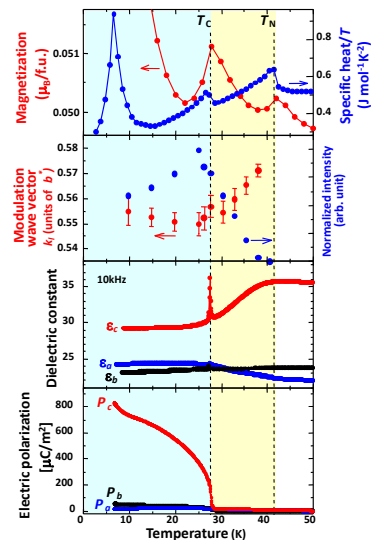


Competition between FM Nearest-Neighbor & AF Next-Nearest-Neighbor interactions



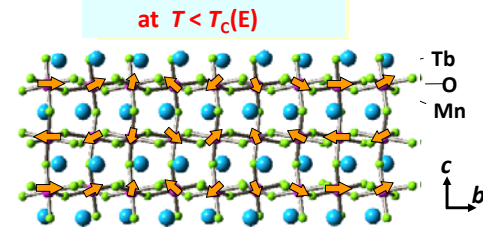
Ferroelectric order accompanied by spiral magnetic order in TbMnO_3

T. Kimura et al. Nature 426, 55 (2003).

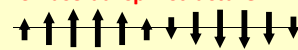


Spin structure model of TbMnO_3

M. Kenzelmann et al. PRL 95, 087206 (2005).
T. Arima et al., PRL 96, 097202 (2006).



Sinusoidal spin structure



Spiral spin structure

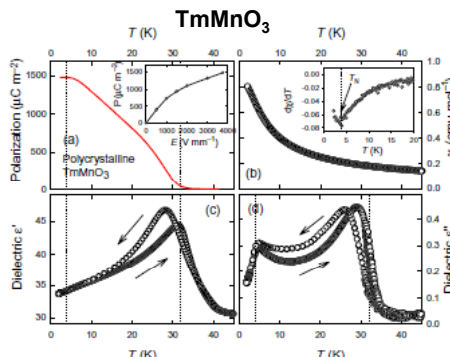


$m \perp z$
 $2 \parallel y$
 $m' \perp x$

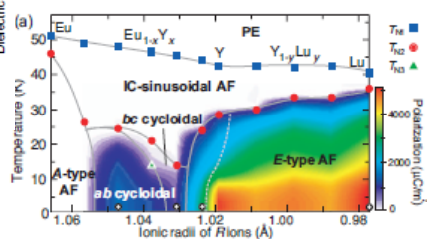
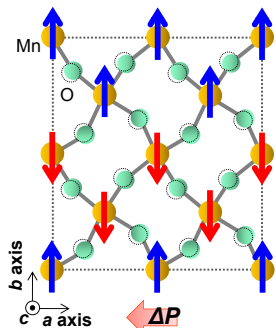
Ferroelectricity induced by exchange striction ($\sim J S_i \cdot S_j$)

Sergienko et al. PRL 97, 227204 (2006)

Picozzi et al., PRL 99, 227201 (2007).



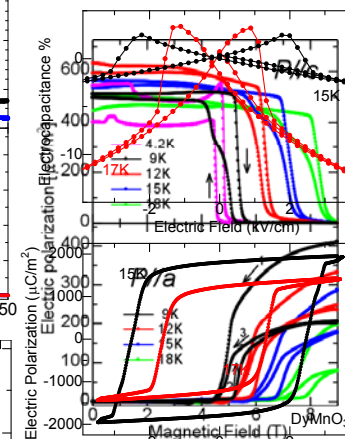
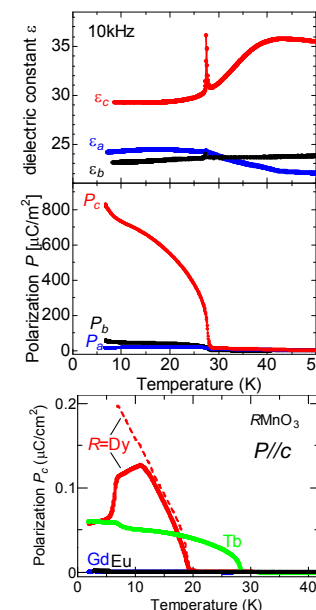
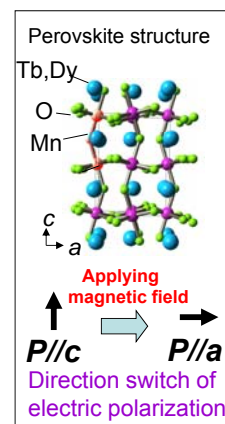
Pomjakushin et al.
New. J. Phys. PRB 11, 043019 (2010)



Ishiwata et al. PRB 81, 100411(R) (2010)

Large ME effects near the phase boundary in TbMnO_3 , DyMnO_3

T. Kimura et al. Nature 426, 55 (2003).



Magnetically controllable ferroelectric properties

Ferroelectricity with spontaneous polarization along the c-axis

Outline of this lecture

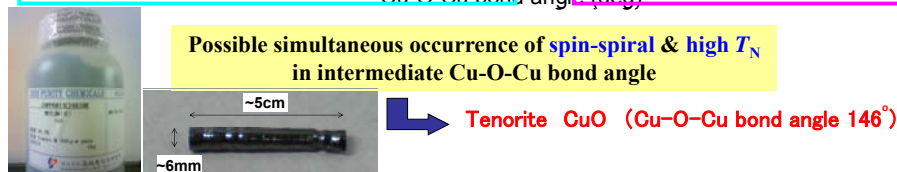
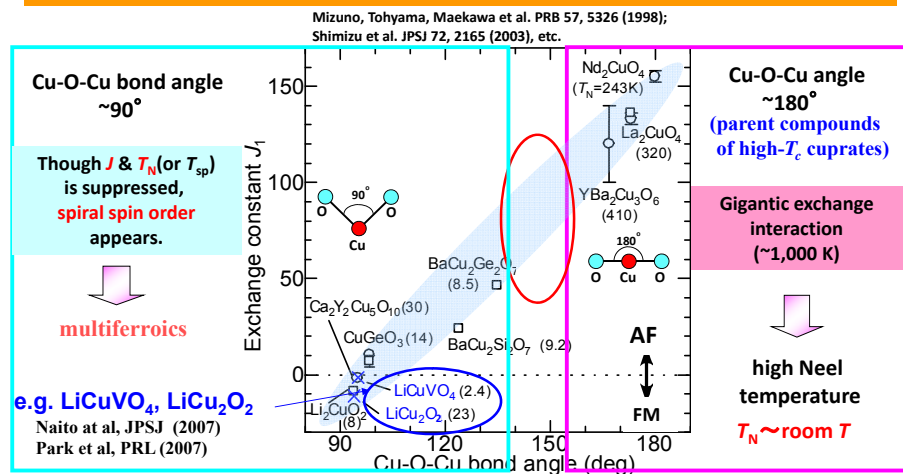
- Symmetry in crystals
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- ME effect in magnetically-disordered system

Spin frustration often suppresses magnetic ordering temperature.
Most of induced-multiferroics only operate below ~ 40 K.

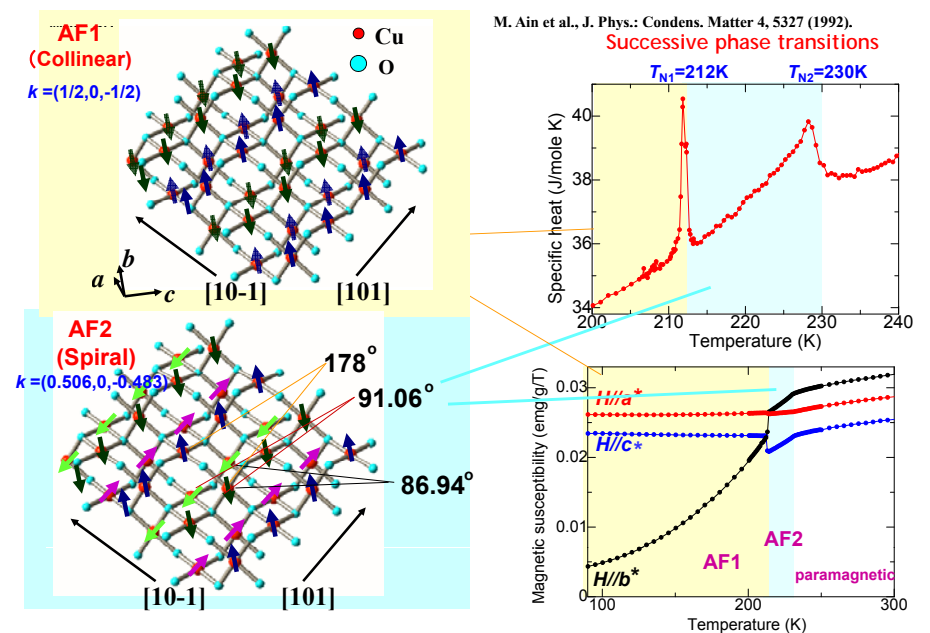
How to obtain induced-ferroelectrics with high- T_C ?

1. Low dimensional cuprates with Cu^{2+}

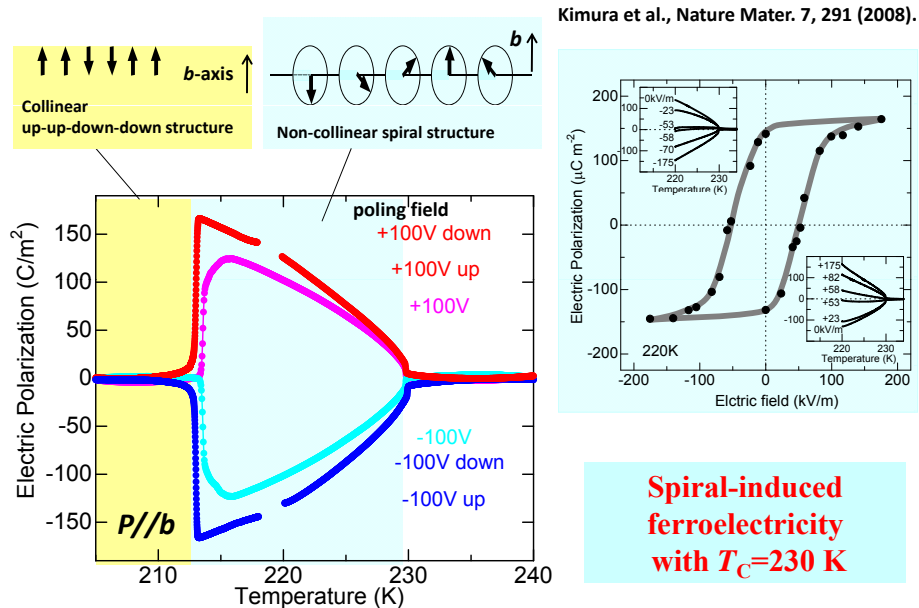
Variation of superexchange interaction J in several undoped cuprates



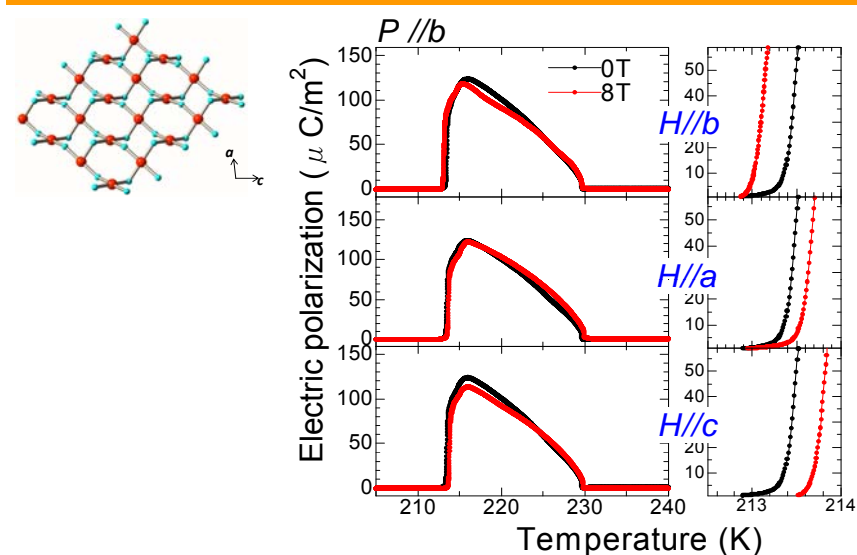
Crystal & magnetic structures of CuO



Ferroelectricity with $P//b$ -axis in spin spiral phase of CuO



Magnetic-field effect on ferroelectricity in CuO



Unfortunately, the effect of H on ferroelectricity was quite small in CuO.

Spin frustration often suppresses magnetic ordering temperature.
Most of induced-multiferroics only operate below $\sim 40\text{ K}$.

How to obtain induced-ferroelectrics with high- T_c ?

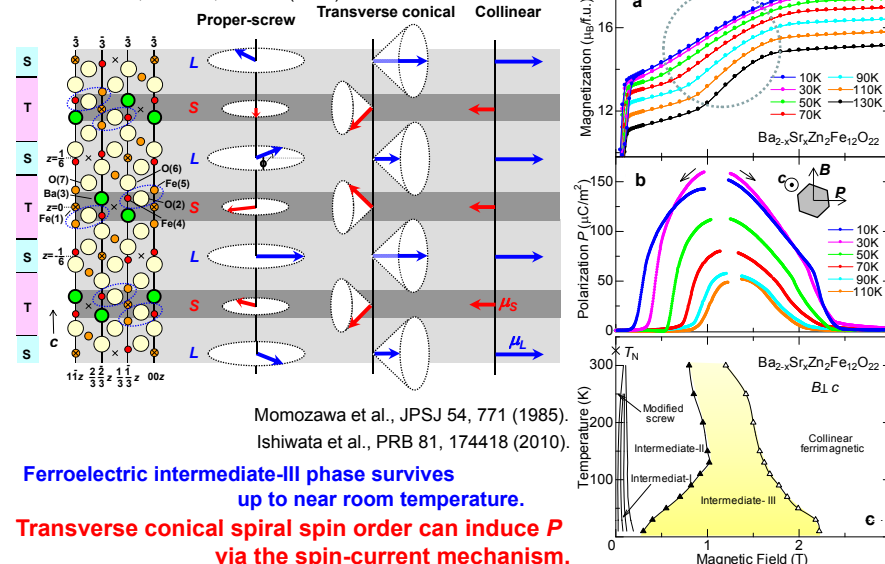
1. Low dimensional cuprates with Cu^{2+}
2. Iron oxides with hexagonal structure (hexaferrites)

Refrigerator magnet



Magnetolectric Y-type hexaferrite $(\text{Ba,Sr})_2\text{Me}_2\text{Fe}_{12}\text{O}_{22}$ ($\text{Me}=\text{Zn, Mg, etc.}$)

Kimura et al., PRL. 94, 137201 (2005)



Momozawa et al., JPSJ 54, 771 (1985).

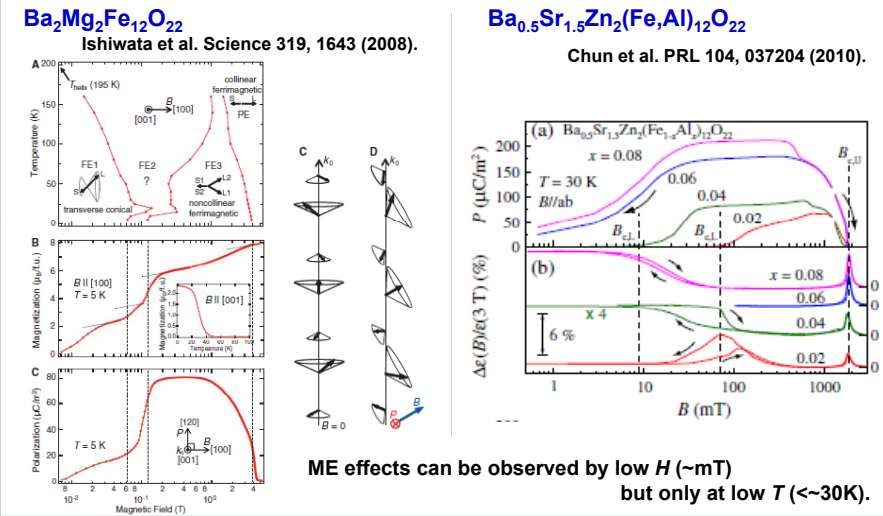
Ishiwata et al., PRB 81, 174418 (2010).

Ferroelectric intermediate-III phase survives up to near room temperature.

Transverse conical spiral spin order can induce P via the spin-current mechanism.

However, suppression of resistivity does not allow experimental observation of polarization above $\sim 110\text{ K}$.

Low-Magnetic-Field Control of Electric Polarization in Y-type hexaferrites (Ba,Sr)₂Me₂Fe₁₂O₂₄

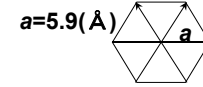


We pursue **room-temperature magnetoelectrics** in other types of hexaferrites.

- Hexaferrite showing
1. a spiral magnetic order above room temperature
 2. highly insulating electric property at room temperature

Classification of hexagonal ferrites (hexaferrites) - chemical formula -

J. Smit & H.P.J. Wijn, Ferrite (Philips' Technical Library, 1959)



M-type
(magnetoplumbite)
BaFe₁₂O₁₉
($c=23.19$ Å)

Refrigerator magnet



W-type : BaM₂Fe₁₆O₂₇ ($c=32.84$ Å)

Y-type : Ba₂M₂Fe₁₂O₂₂ ($c=43.56$ Å)

Z-type : Ba₃M₂Fe₂₄O₄₁ ($c=52.30$ Å)

X-type : Ba₂M₂Fe₂₈O₄₆ ($c=84.11$ Å)

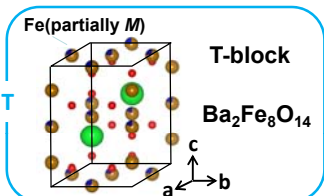
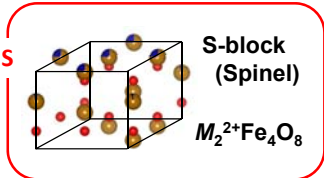
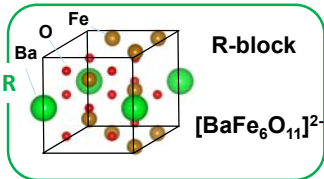
U-type : Ba₄M₂Fe₃₆O₆₀ ($c=113$ Å)

(M = divalent metal)

Classification of hexagonal ferrites

- Stacking sequence composed of 3 types of blocks-

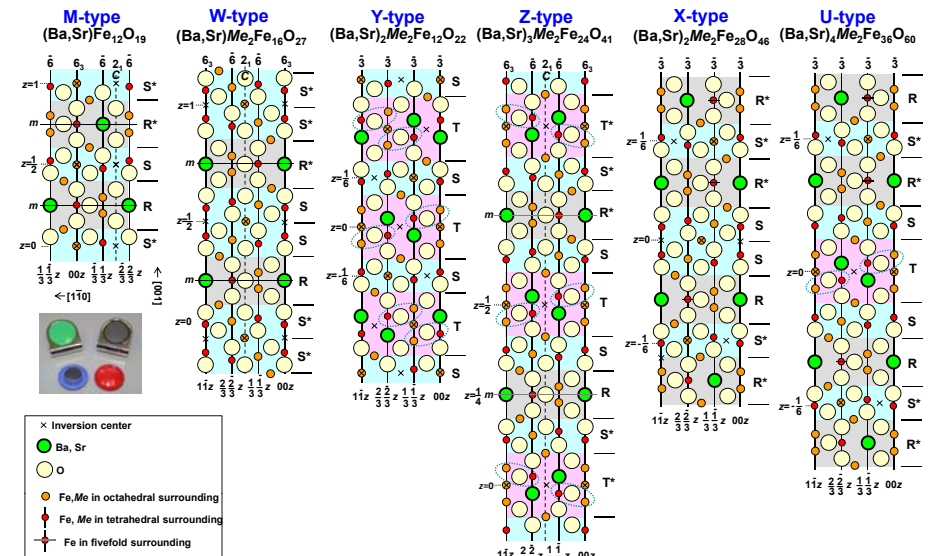
J. Smit & H.P.J. Wijn, Ferrite (Philips' Technical Library, 1959)



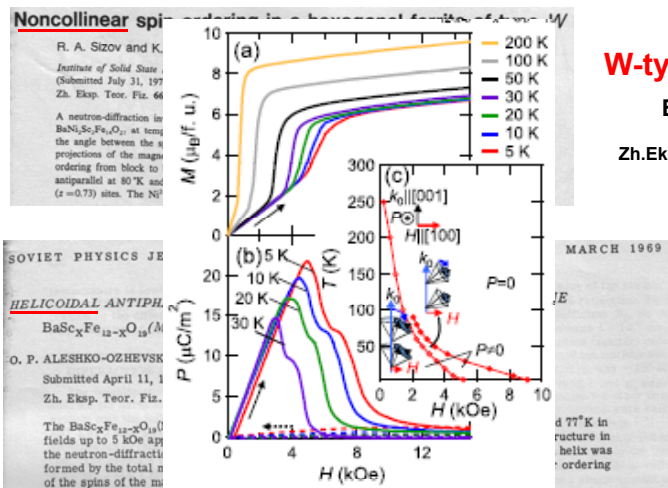
	Chem. form.	stacking	c (Å)	S.G.
M	BaFe ₁₂ O ₁₉	RSR'S*	23.19	P6 ₃ /mmc
W	BaM ₂ Fe ₁₆ O ₂₇	RS ₂ R'S ₂	32.84	P6 ₃ /mmc
Y	Ba ₂ M ₂ Fe ₁₂ O ₂₂	(TS) ₃	43.56	R-3/m
Z	Ba ₃ M ₂ Fe ₂₄ O ₄₁	RSTSR'S'T'S*	52.3	P6 ₃ /mmc
X	Ba ₂ M ₂ Fe ₂₈ O ₄₆	(RSR'S ₂) ₃	84.11	R-3/m
U	Ba ₄ M ₂ Fe ₃₆ O ₆₀	(RSR'S'TS*) ₃	113	R-3/m

The prime (') and asterisk (*) symbols indicates that the corresponding block is rotated 120° or 180° about the c axis, respectively.

Crystal structures of 6 main types of hexaferrites



Appearance of noncollinear spiral magnetic order in hexaferrites



W-type
 $BaNi_2Sc_2Fe_{14}O_{27}$
 Zh.Eksp. Teor. Fiz. 66, 368 (1974)

M-type
 $BaSc_xFe_{12-x}O_{19}$
 Zh.Eksp. Teor. Fiz. 55, 820 (1968)

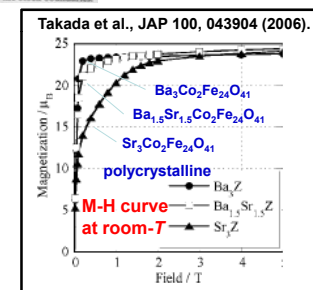
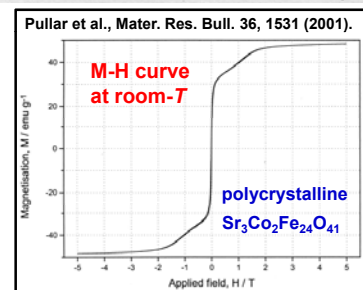
c.f. ME effect in M-type [Tokunaga et al., PRL 105, 257201 (2010).]

Former studies on magnetism of Z-type hexaferrites

Noncollinear Magnetic Structures in Hexagonal Ferrites of the $Ba_{3-x}Sr_{3-x}Zn_2Fe_{24}O_{41}$ (Z) System
 M. I. NAMTALISHVILI, O. P. ALESHKO-OZHEVSKII, AND I. L. YAMZIN
 Crystallography Institute, USSR Academy of Sciences
 Submitted July 26, 1971
 Zh. Eksp. Teor. Fiz. 62, 701-709 (February, 1972)

$(Ba,Sr)_3Zn_2Fe_{24}O_{41}$
 Zh.Eksp. Teor. Fiz. 62, 701 (1972)

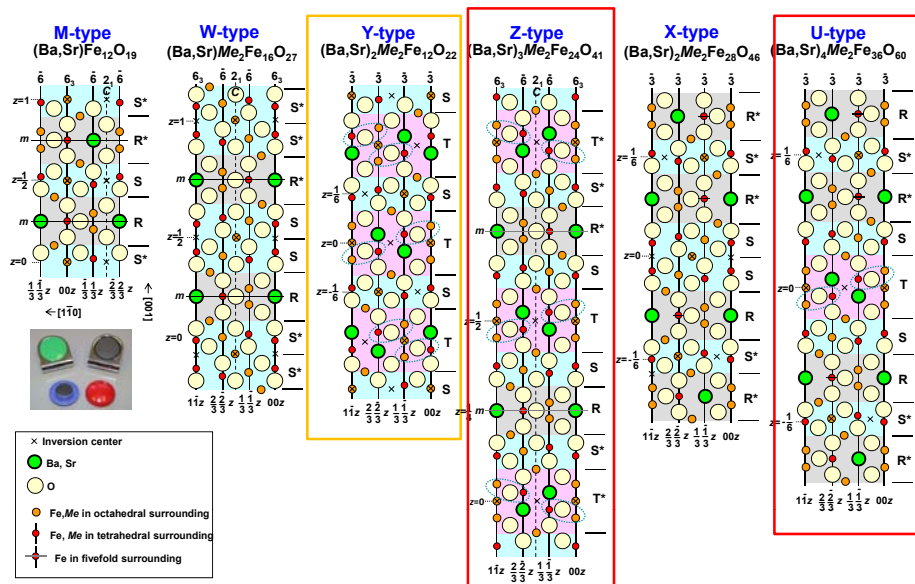
Noncollinear spin structure?



M of $Sr_3Co_2Fe_{24}O_{41}$ increases in a stepwise fashion.

→ Similar to magnetoelectric Y-type hexaferrites

Crystal structures of 6 main types of hexaferrites



Experimental procedures

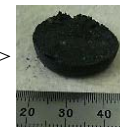
*Sample synthesis

Z-type $(Ba,Sr)_3Co_2Fe_{24}O_{41}$ & U-type $(Ba,Sr)_4Co_2Fe_{36}O_{60}$ studied here are polycrystalline samples prepared by the conventional solid-state reaction technique.

Starting chemicals

$BaCO_3$
 $SrCO_3$
 Fe_2O_3
 Co_3O_4

calcine
 800~1000°C
 16~20h
 in air



crush & sinter
 1150-1300°C
 5~50h
 in air or O₂ flow

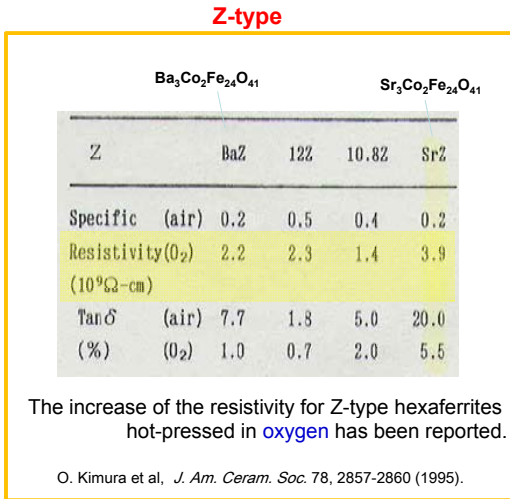
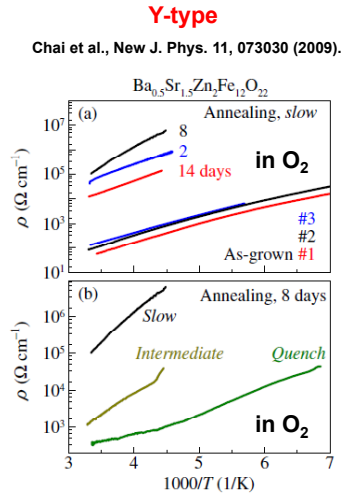


*Measurements

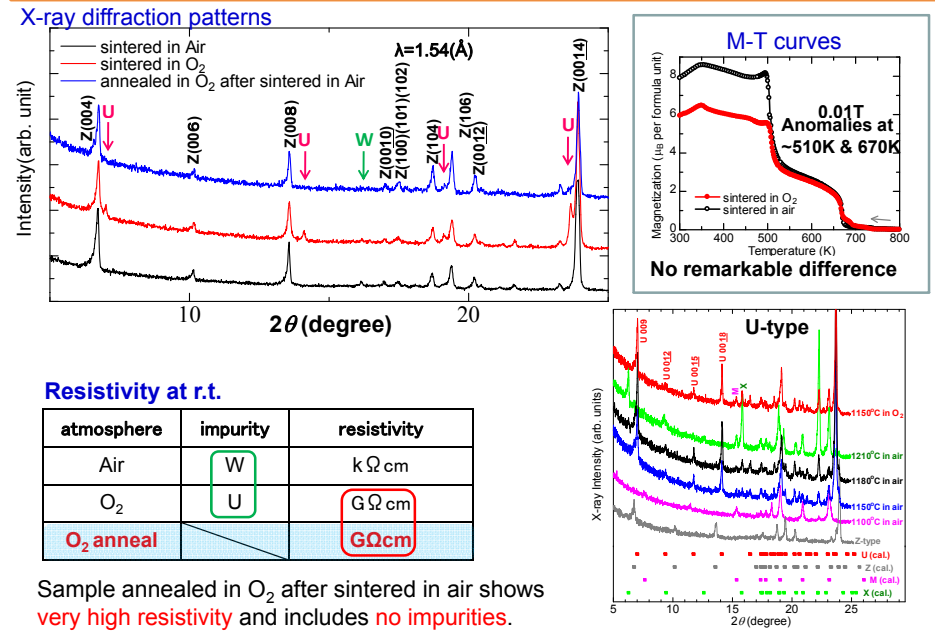
- Powder x-ray diffraction (room temperature)
- Resistivity (room temperature)
- Magnetization (~10K < T < ~800 K)
- Dielectric constant (~10K < T < ~400 K)
- Electric polarization (~10K < T < ~400K)
- Powder neutron diffraction (~10K < T < ~640K)

H
 E
 Magnetic fields were applied in a direction normal to electric fields.

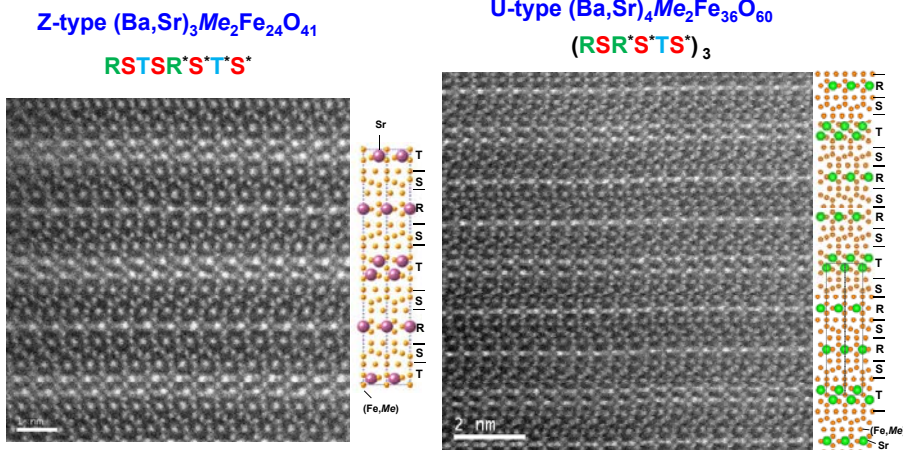
Enhancement of Resistivity in Hexaferrites



Evaluation of sample quality (purity, resistivity)



[100]-zone high-angle annular dark-field scanning TEM (HAADF-STEM) images for two hexaferrite samples



Low field ME effect of Z-type $Sr_3Co_2Fe_{24}O_{41}$ at room temperature

polycrystalline ceramics sintered in oxygen.

Kitagawa et al., Nature Mater. 9, 797 (2010).

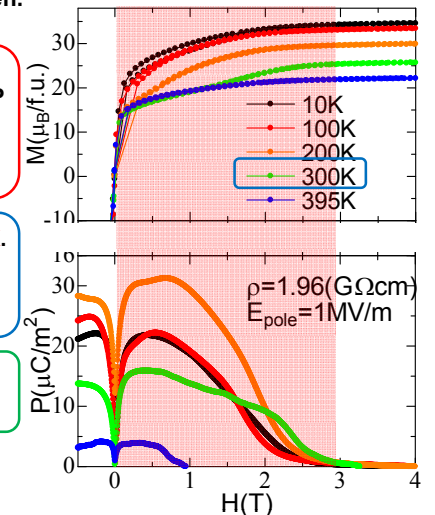
✓ In the region where magnetization M shows metamagnetic fashion, polarization P can be observed.

➡ **Z-type hexaferrite shows ME effect!!**

✓ In addition, P can be measured up to **395K**.

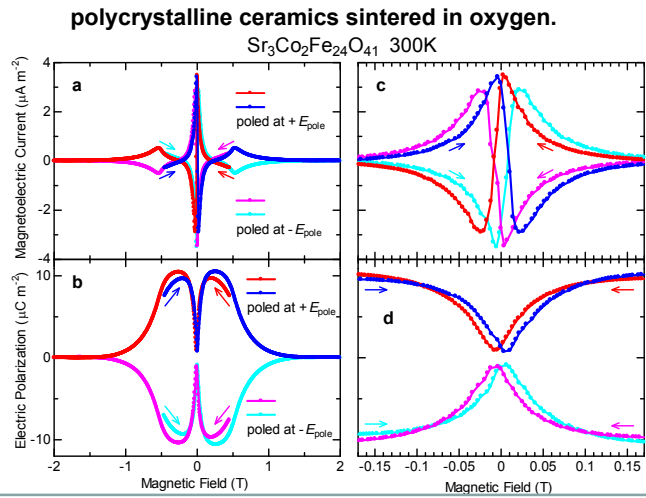
➡ **Ferroelectric transition temperature T_c is higher than room temperature!!**

✓ P appears by the application of **low magnetic field**.



Magnetolectric effects are observed at a wide temperature range including room temperature.

Room-temperature ME effect of $\text{Sr}_3\text{Co}_2\text{Fe}_{24}\text{O}_{41}$



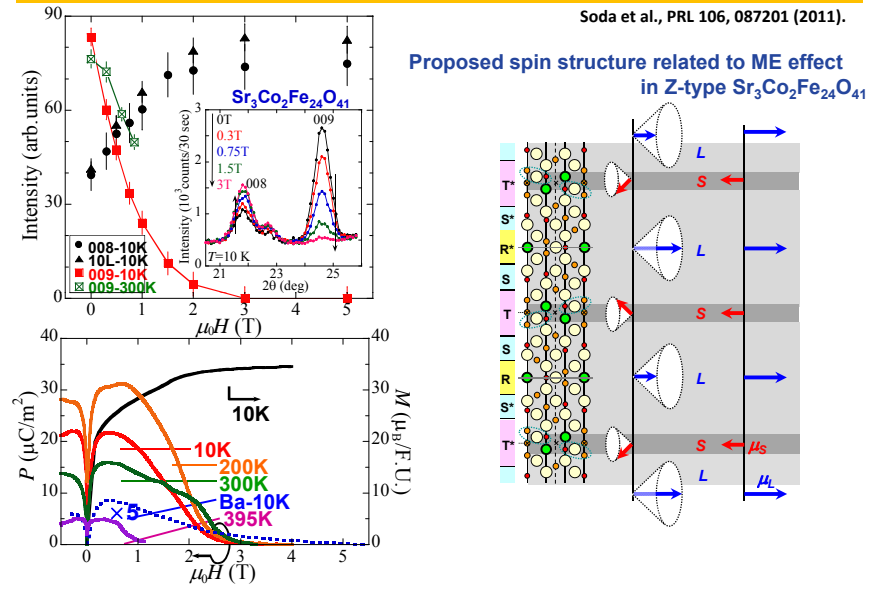
*ME coefficient defined as $\alpha = \mu_0 dP/dB$

The α exceeds 1×10^{-10} s/m below 0.04T and reached a maximum $\sim 2.5 \times 10^{-10}$ s/m at 0.003T.

(c.f. α in Cr_2O_3 : 4×10^{-12} s/m; α in Z-type single crystal: 3×10^{-9} s/m by Chun arXiv:1111.4525)

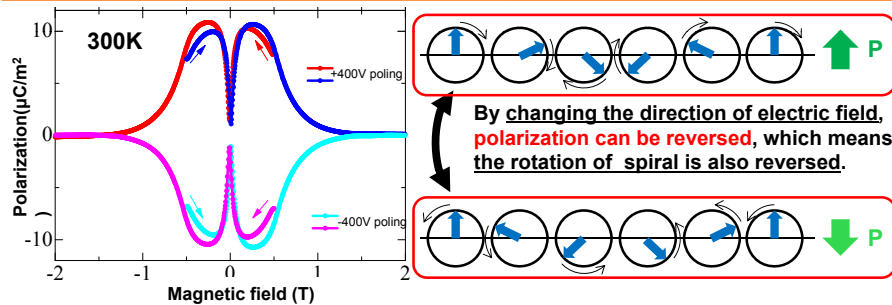
Origin of magnetolectric effect –Neutron diffraction–

Soda et al., PRL 106, 087201 (2011).



In analogy with Y-type hexaferrites, the r.t. ME effect can be understood in terms of P induced by a transverse conical spin structure through the spin-current mechanism.

Non-volatility of reversible polarization



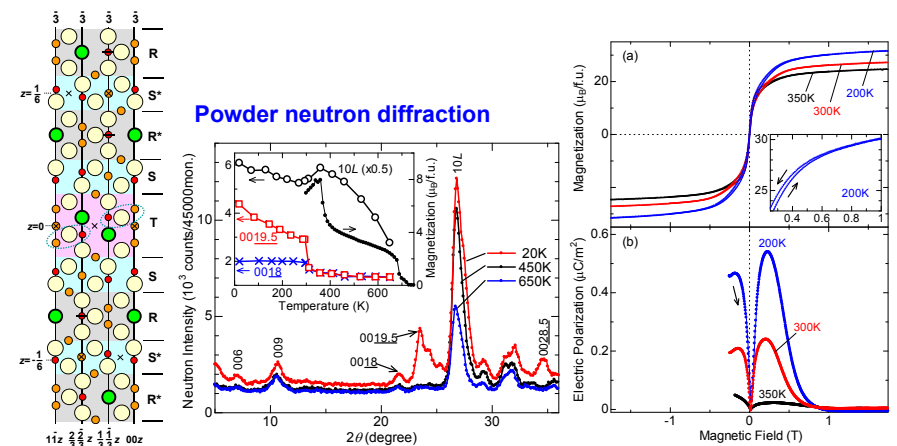
Ferroelectric domains are aligned by electric field (poling).



Once sample becomes ferroelectric, polarization is memoried unless sample becomes paraelectric

Magnetism and magnetolectricity of U-type $\text{Sr}_4\text{Co}_2\text{Fe}_{36}\text{O}_{60}$

K. Okumura et al., APL 98, 212504 (2011)



Corresponding to the appearance of the magnetic order with the propagation vector $(0,0,3/2)$, a small magnetolectric effect was observed below $T_{N2} \sim 350$ K.

Summary (magnetolectric hexaferrites)

Various hexaferrite compounds were highlighted in terms of their high-temperature and low-field magnetolectric operation.

M-type $(\text{Ba,Sr})\text{Fe}_{12}\text{O}_{19}$, Y-type $(\text{Ba,Sr})_2\text{Me}_2\text{Fe}_{12}\text{O}_{22}$,
Z-type $(\text{Ba,Sr})_3\text{Me}_2\text{Fe}_{24}\text{O}_{41}$, U-type $(\text{Ba,Sr})_4\text{Me}_2\text{Fe}_{36}\text{O}_{60}$

*The ME effect appears even below **several hundreds Oe** and persists up to **~400 K**.

*The ME effects can be originated from a **transverse conical spin structure**.

This result has the promise of ME device applications including non-volatile memory where information is stored as **electrically-detectable & -controllable spin-helicity**.



Outline of this lecture

- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetolectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites RMnO_3
 - Cuprates and ferrites working at room temperature

- **Observation of spin-spiral domain structure**
 - ME effect in magnetically-disordered system
- by scanning resonant x-ray microdiffraction**
with Y. Hiraoka (Osaka), Y. Tanaka (SPring8), S. Shin (SPring8)

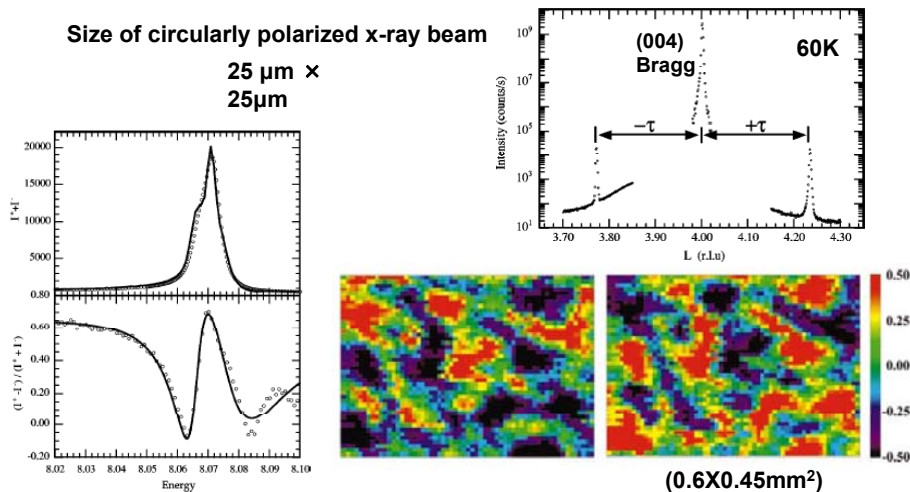
Imaging spiral magnetic domains in Ho by circularly polarized Bragg diffraction

J.C. Lang et al., J. Appl. Phys. 95, 6537 (2004)

Ho metal

[spiral magnetic order with $(0,0, L \pm \tau)$ below $T_N=133\text{K}$]

X-ray energy $E \sim 8.071 \text{ eV}$ ($\sim \text{Ho } L_3\text{-edge } 2p \rightarrow 5d$)

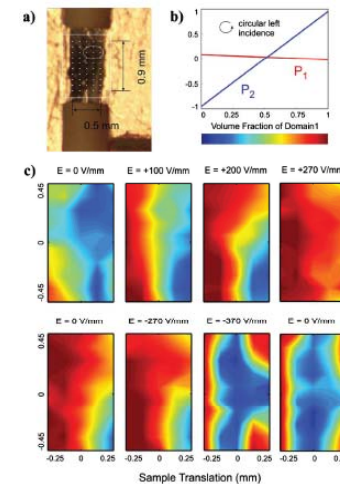


Imaging spiral magnetic domains in multiferroics by circularly polarized X-ray

$\text{Ni}_3\text{V}_2\text{O}_8$

Fabrizi, Phys. Rev. B **82**, 024434 (2010).

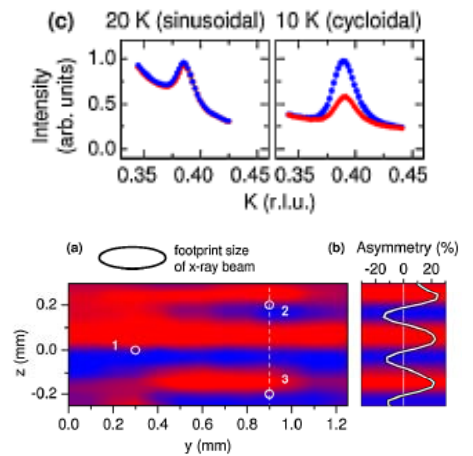
Nonresonant X-ray
Beam size $\approx 380 \times 250 \mu\text{m}^2$



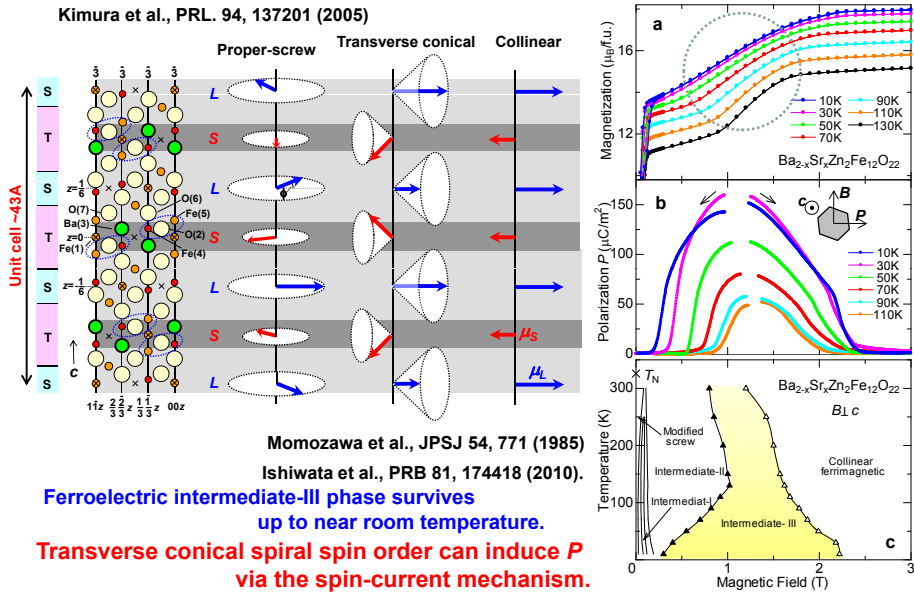
DyMnO_3

Schierle, Phys. Rev. Lett. **105**, 167207 (2010).

X-ray energy : Dy M_5 -edge
Beam size $\approx 300 \times 100 \mu\text{m}^2$



Magnetolectric Y-type hexaferrite (Ba,Sr)₂Me₂Fe₁₂O₂₂ (Me=Zn, Mg, etc.)



Circularly polarized x-ray diffraction study of Ba_{0.8}Sr_{1.2}Zn₂Fe₁₂O₂₂

Mulders et al., PRB 81, 092405 (2010).

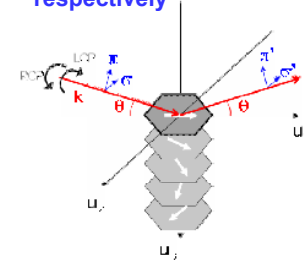
Magnetic diffraction intensity along c :

$$I_{\text{right}} \propto \left(\cos^2 \theta + \frac{1}{2} \sin^2 2\theta \mp \chi \cos \theta \sin 2\theta \right)$$

$$I_{\text{left}} \propto \left(\cos^2 \theta + \frac{1}{2} \sin^2 2\theta \pm \chi \cos \theta \sin 2\theta \right)$$

$F_{11}, F_{1,-1}$: atomic proper
 $q (= k_i - k_f)$, G : reciprocal

If the fractions of the right- and left-handed spin-chiral domains are a and $(1-a)$, respectively



$$\frac{I_a^{(-)}}{I_a^{(+)}} = \frac{\cos^2 \theta + \frac{1}{2} \sin^2 2\theta \mp (1-2a) \cos \theta \sin 2\theta}{\cos^2 \theta + \frac{1}{2} \sin^2 2\theta \pm (1-2a) \cos \theta \sin 2\theta}$$

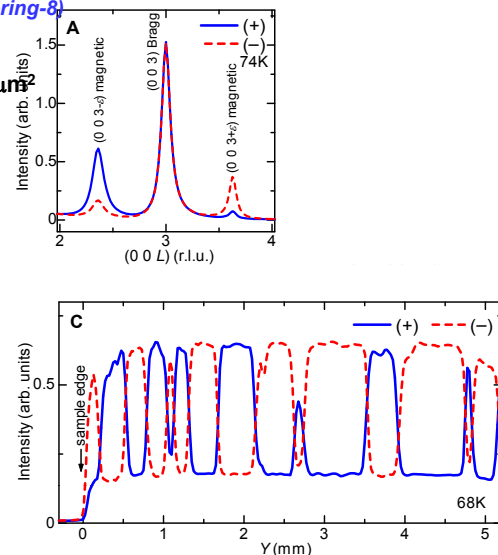
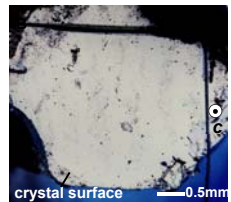
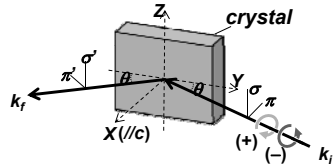
Incident polarization	(003 ⁻)		(003 ⁺)		$a = 0.77$
	Exp.	Calc.	Exp.	Calc.	
RCP	0.50	0.52	0.11	0.10	
LCP	0.24	0.25	0.25	0.23	

Imaging spin-chiral domains in Ba_{0.5}Sr_{1.5}Zn₂Fe₁₂O₂₂ by circularly polarized X-ray

Sample Ba_{0.5}Sr_{1.5}Zn₂Fe₁₂O₂₂ $T_N \sim 310$ K magnetic satellite (0,0,3n±ε)

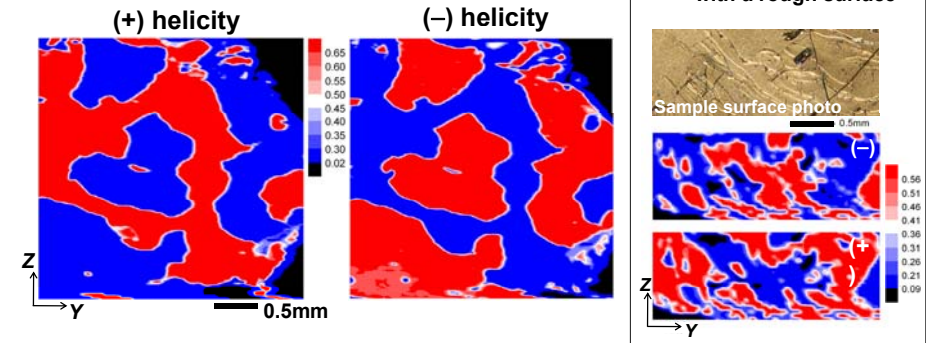
Experimental conditions (@BL17SU, Spring-8)

Incident x-ray energy 710 eV
Illuminated sample area 60 x 15 μm²
with a 25 μm step
Penetration depth ~40 nm



Spatial images of spin-chiral domain structure in Ba_{0.5}Sr_{1.5}Zn₂Fe₁₂O₂₂ at 68 K

Hiraoka et al., PRB 84, 064418 (2011).

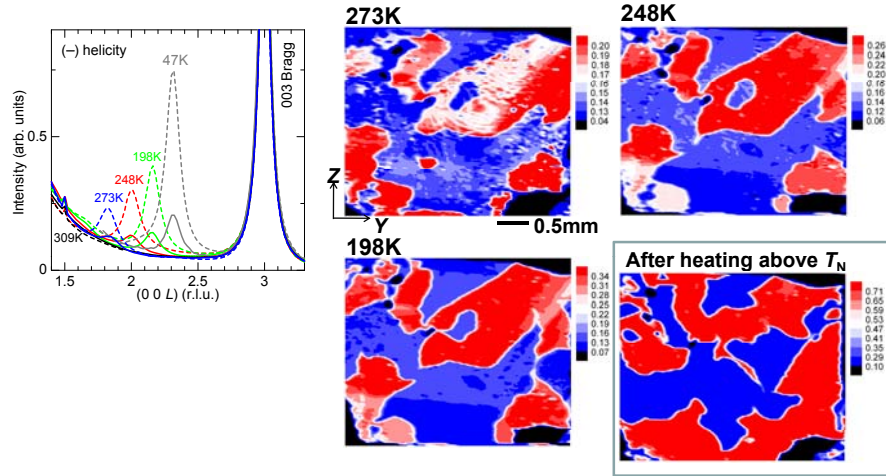


*Red and blue regions correspond to either a left- or right-handed spin-chiral monodomain.
*The observed domains are irregular in shape with a size on a submillimeter scale.

*There is a tendency that the domain boundaries are clamped at surface defects.
*The observed domains were apparently smaller in size than those on a smooth surface.

Thermal effect on the spin-chiral domain structure in $\text{Ba}_{0.5}\text{Sr}_{1.5}\text{Zn}_2\text{Fe}_{12}\text{O}_{22}$

Hiraoka et al., PRB (in press)

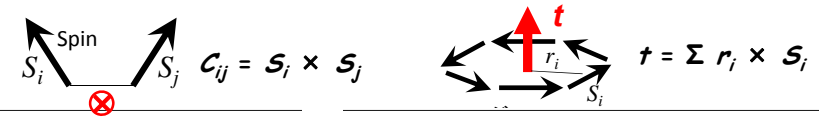


The domain structure is robust with respect to the variation of T and time once they are formed, but is not reproducible once the crystal is heated above T_N .

Outline of this lecture

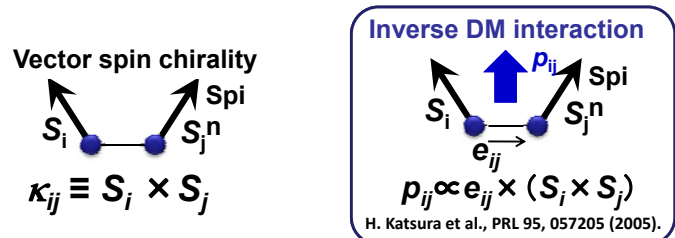
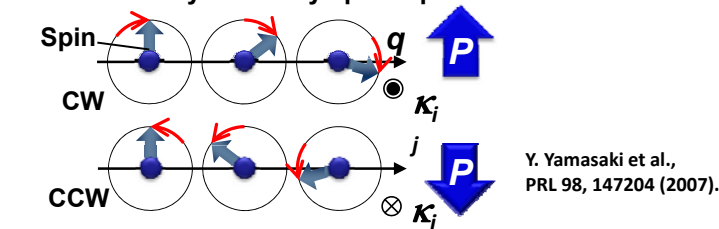
- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetoelectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites RMnO_3
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- **ME effect in magnetically-disordered system**
with Y. Yamaguchi (Osaka), T. Nakano (Osaka), Y. Nozue (Osaka)

To pursue the ME coupling owing to multi-spin variables such as spin chirality and toroidal moment in magnetically-disordered systems



Magnetically-induced ferroelectricity & Vector spin chirality

- Ferroelectricity driven by spiral spin order



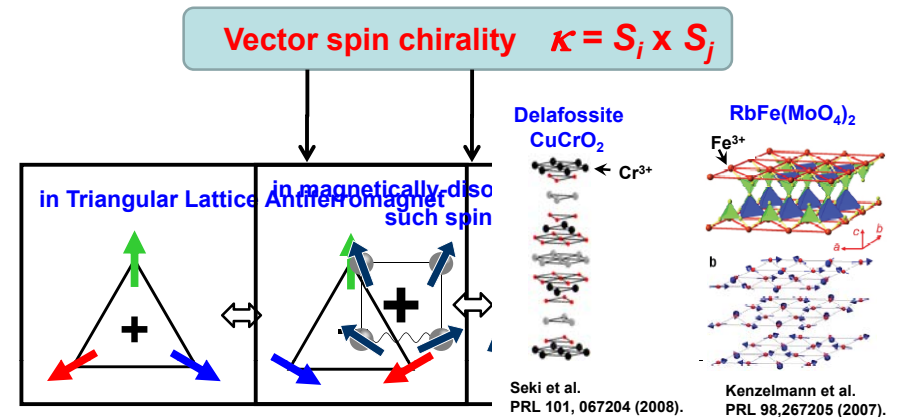
✓ Polarization $P \leftrightarrow$ Chirality κ_{ij}

Vector spin chirality can be detected as electric polarization P through ME coupling.

By recent development of multiferroics research,

Strong correlation between spin frustration & magnetoelectric coupling has been well recognized.

Magnetoelectric effect is useful to detect



Theoretically, multi-spin variables can be nonzero even in the absence of long-range magnetic order.

Chiral spin liquid phase in helimagnets

F. Cinti et al., PRL 100, 057203 (2008); PRB 83, 174414 (2011).

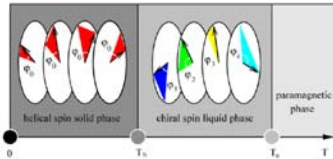


FIG. 1 (color online). Schematic representation of Villain's conjecture. In the chiral spin liquid phase, corkscrews all turning clockwise (or all anticlockwise) with in general $\varphi_i \neq \varphi_j$. In the helical spin solid phase, same angle value φ_0 for all spins.

Spin-chirality decoupling in spin-glass system

H. Kawamura, PRL 68, 3785 (2011); J. Phys. Condens. Matter 23, 164210 (2011).

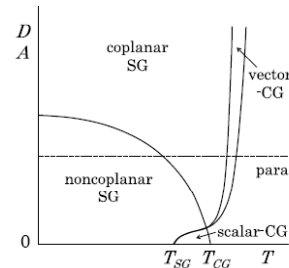


Figure 1. Phase diagram of the XY-like SG with an easy-plane-type uniaxial magnetic anisotropy in the uniaxial anisotropy versus the temperature plane. T_{CG} and T_{SG} represent the chiral-glass and the spin-glass transition temperatures of the fully isotropic Heisenberg system.

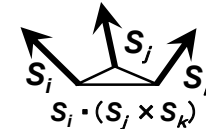
➡ It is possible that ME materials are found in magnetically-disordered phases.

Spin chirality in spin glass system

A chirality driven mechanism for spin-glass transitions

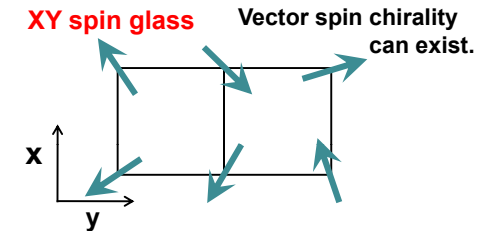
H. Kawamura, PRL 68, (1992) 3785.

Heisenberg spin glass



Anomalous Hall effect due to scalar spin chirality

T. Taniguchi, et al., PRL 93, (2004) 246605.



H. Kawamura, J. Phys. Cond. Matter 23, 164210 (2011).

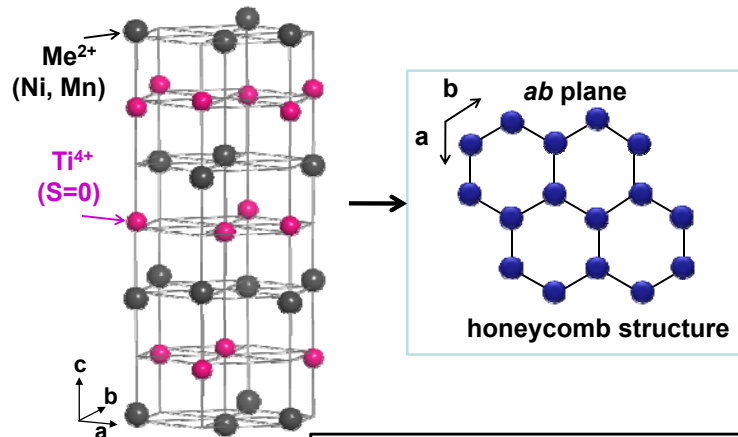
Can we detect vector spin chirality in spin glass system though magnetoelectric coupling?

Example compounds showing insulating & XY-like spin glass state

- * $\text{Rb}_2\text{Mn}_{1-x}\text{Cr}_x\text{Cl}_4$ K. Katsumata et al., PRB 25, 428 (1982).
- * $\text{Ni}_x\text{Mn}_{1-x}\text{TiO}_3$ A. Ito et al., JMMM 104, 1637 (1992).

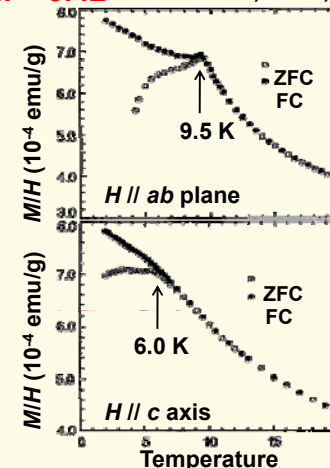
Crystal structure of $\text{Ni}_x\text{Mn}_{1-x}\text{TiO}_3$

ilmenite structure



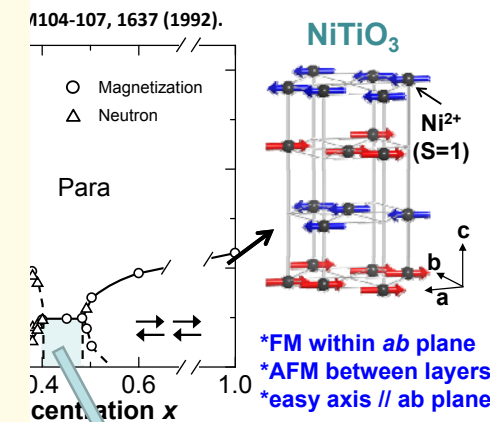
- Alternating stack of Me^{2+} & Ti^{4+}
- Only Me (Ni, Ni) ions are magnetic.
- Space group $R\bar{3}$ → centrosymmetric

Ni = 0.42 H. Kawano et al., JPSJ 62, 2575 (1993)



9.5 K : inplane spin component freezes.
6.0 K : c-axis spin component freezes.
XY-like Spin Glass
Pseudo vector spin chirality appears at 9.5 K?

Crystal structure of $\text{Ni}_x\text{Mn}_{1-x}\text{TiO}_3$



Ni = 0.4~0.5
shows spin glass phase with weak inplane anisotropy.

Our experiments

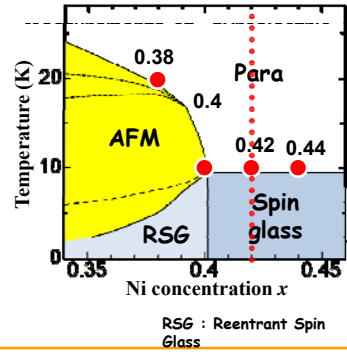
Sample $\text{Ni}_{1-x}\text{Mn}_x\text{TiO}_3$

Single crystals are grown by the floating zone method.



Phase diagram $\text{Ni}_x\text{Mn}_{1-x}\text{TiO}_3$

A. Ito et al., J. MMM 104-107, 1637 (1992).



Following measurements.

- ② Frequency dependence of ϵ
Measurements of capacitance with an LCR meter
- ③ Specific heat in magnetic fields measured with the relaxation technique (PPMS Option)
- ④ Composition dependence
 - > MnTiO_3
 - > $(\text{Ni}, \text{Mn})\text{TiO}_3$ Ni=0.38, 0.40, 0.42, 0.44

Magnetic & dielectric properties at zero magnetic fields

$\text{Ni}_{0.42}\text{Mn}_{0.58}\text{TiO}_3$

Magnetic susceptibility

Anomalies at $T_{\text{SG1}} \sim 9.5 \text{ K}$
 $T_{\text{SG2}} \sim 6.0 \text{ K}$

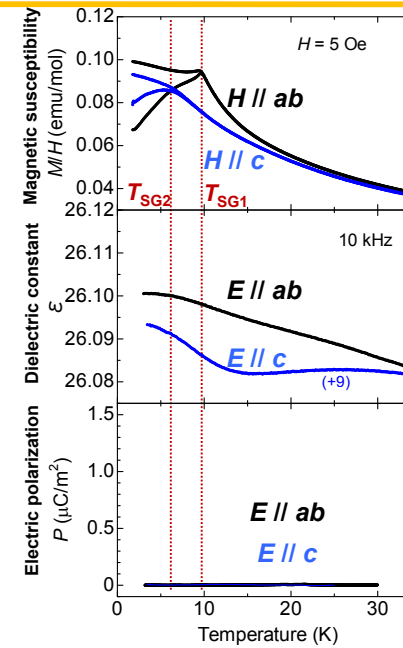
Spin glass transition

[consistent with previous study
H. Kawano et al., JPSJ 62, 2575 (1993)]

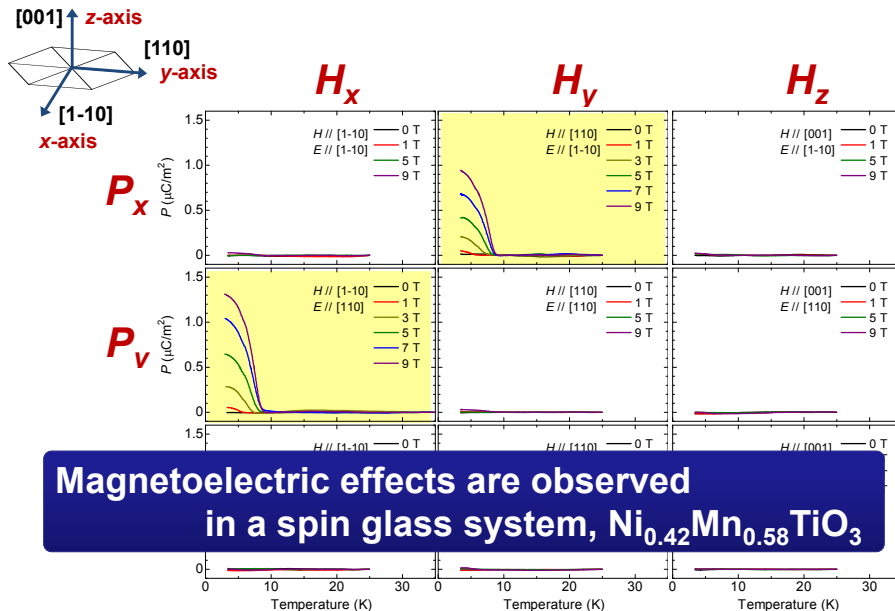
Dielectric properties

No anomaly at T_{SG1} & T_{SG2}

No correlation between magnetic & dielectric properties was observed.

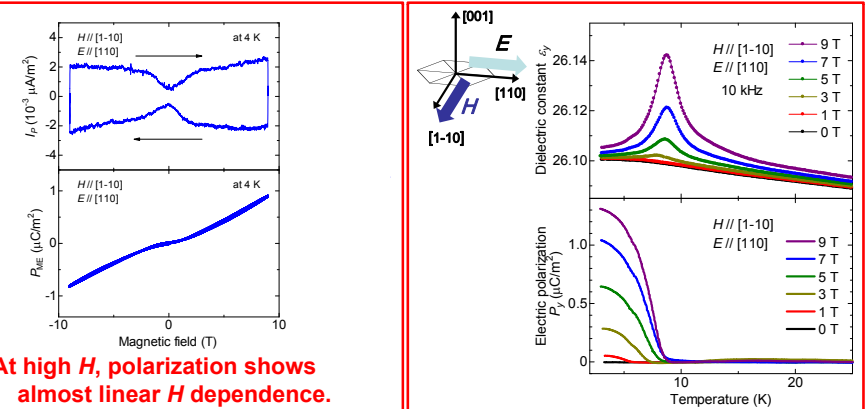


Magnetic field effect on electric polarization in $\text{Ni}_{0.42}\text{Mn}_{0.58}\text{TiO}_3$



Magnetolectric effects are observed in a spin glass system, $\text{Ni}_{0.42}\text{Mn}_{0.58}\text{TiO}_3$

Finite polarization appears only in two configurations



At high H , polarization shows almost linear H dependence.

Magnetolectric coefficient

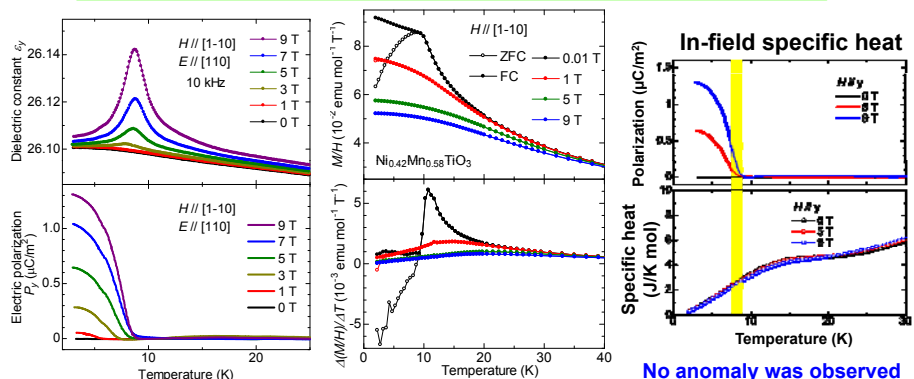
$$\begin{pmatrix} P_x \\ P_y \\ P_z \end{pmatrix} = \begin{pmatrix} 0 & \alpha_{12} & 0 \\ -\alpha_{12} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix}$$

Off-diagonal & Antisymmetric

What is the origin of the ME effect observed in $\text{Ni}_{0.42}\text{Mn}_{0.58}\text{TiO}_3$?

Proposals for possible origins

1. Magnetic-fields induce long range magnetic order which allows ME effect.



At high H , ME effect appears below ~ 9 K.

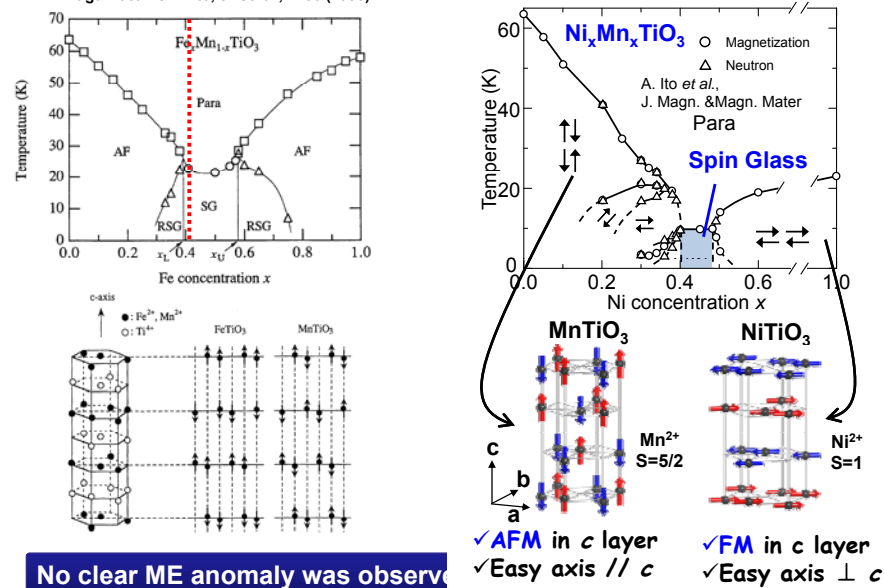
At low H , spin glass transition appears at 6.0 K & 9.5 K.

No anomaly was observed in in-field specific heat.

No corresponding anomaly was observed in magnetization & specific heat.

Comparison with an Ising-like spin glass system $-\text{Fe}_{1-x}\text{Mn}_x\text{TiO}_3-$

H. Aruga-Katori & A. Ito, JPSJ 62, 4488 (1993)



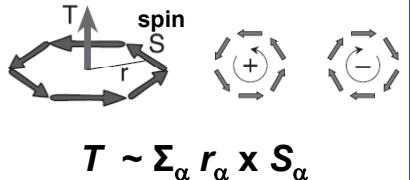
No clear ME anomaly was observed

Antisymmetric ME effect induced by toroidal moment

2. Toroidal ordering induces ME effect

Toroidal moment T

ordered arrangement of magnetic vortices



$H = 0$
 $P = 0$

$H > 0$
 $P \neq 0$

c.f. Spin current model
Katsura et al., PRL 95, 057205 (2005)

\vec{p}_{ij} : microscopic electric dipole
 \vec{e}_{ij} : unit vector
 \vec{S}_i : spin

chirality: \vec{C}

$\vec{p}_{ij} \propto \vec{e}_{ij} \times (\vec{S}_i \times \vec{S}_j)$

Delaney et al.
PRL 102, 157203 (2009).

Free energy expression including toroidal moment

$$F = -P^s_i E_i - M^s_i H_i - T^s_i (\mathbf{E} \times \mathbf{H})_i \dots - \alpha_{ij} E_i H_j \dots$$

consider $T = (0, 0, T_z)$

$$F = -P^s_i E_i - M^s_i H_i - T_z (E_x H_y - E_y H_x) \dots - \alpha_{ij} E_i H_j \dots$$

$$P_x = -\frac{\partial F}{\partial E_x} = P^s_x + T_z H_y \dots + \alpha_{xj} H_j \dots \quad P_y = -\frac{\partial F}{\partial E_y} = P^s_y - T_z H_x \dots + \alpha_{yj} H_j \dots$$

off-diagonal & antisymmetric magnetoelectric effect

A possible toroidal ordering in XY spin glass system

① XY spin glass

Spin

$\mathbf{E} \times \mathbf{H}$ induced a finite toroidal moment (spin vortex) through $-\mathbf{T}(\mathbf{E} \times \mathbf{H})$

Total $T = 0$
 $T \propto \sum \mathbf{r}_i \times \mathbf{S}_i$

“induced” $T_z \neq 0$

Direction of toroidal moment // z axis

Magnetolectric cooling procedure (cooling with \mathbf{H} & \mathbf{E})

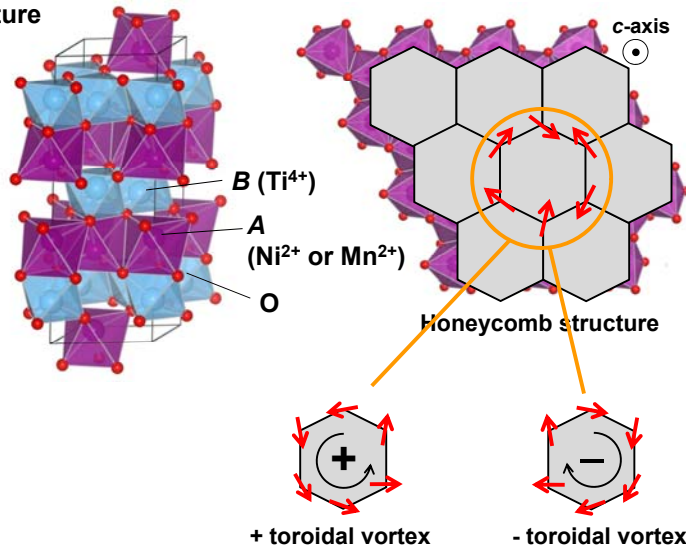
System drop into a valley with $T_z \neq 0$

$$\begin{pmatrix} P_x \\ P_y \\ P_z \end{pmatrix} = \begin{pmatrix} 0 & T_z & 0 \\ -T_z & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix}$$

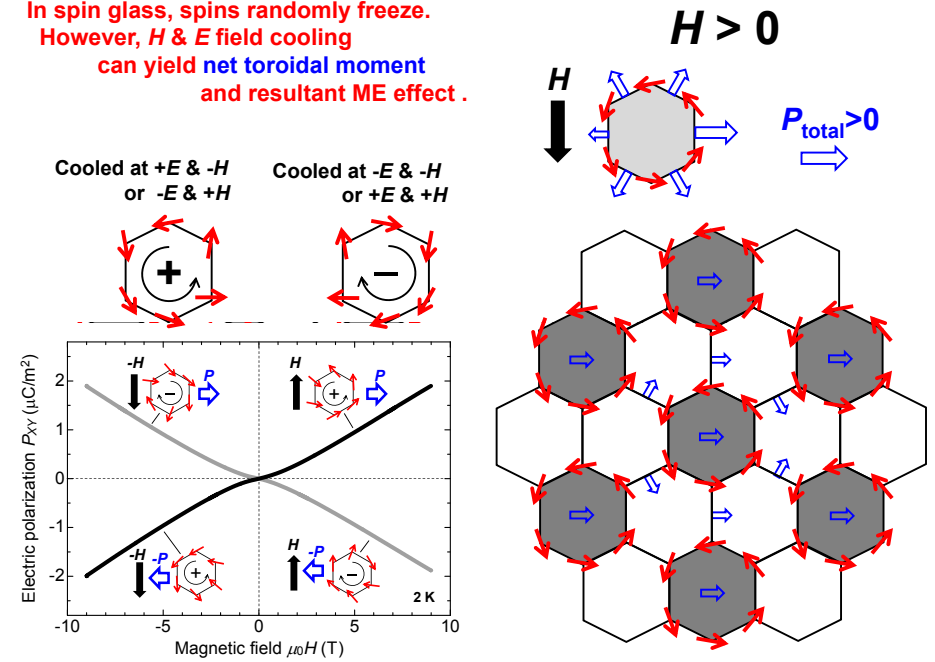
Antisymmetric ME effect are induced in XY spin glass

A possible toroidal ordering in ilmenite $\text{Ni}_{0.42}\text{Mn}_{0.58}\text{TiO}_3$

ilmenite structure
 ABO_3

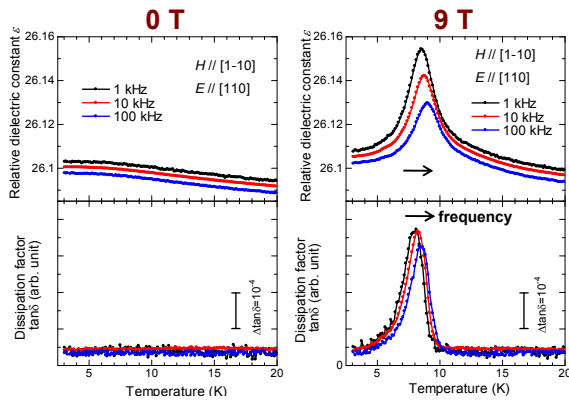


In spin glass, spins randomly freeze.
However, H & E field cooling
can yield net toroidal moment
and resultant ME effect.



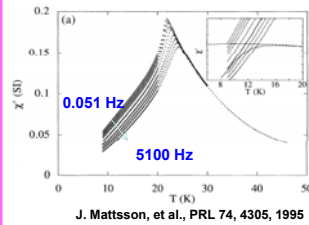
Glassy feature in dielectric constant ϵ

Frequency dependence of ϵ

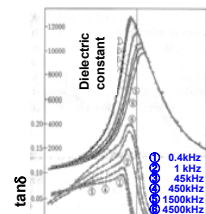


Peaks shifted toward high T as the frequency of AC electric fields increased.

c.f. AC χ in spin glass ($\text{Fe}_{0.5}\text{Mn}_{0.5}\text{TiO}_3$)



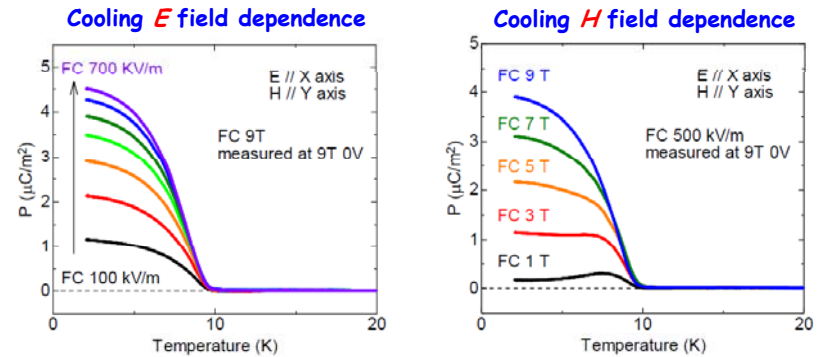
Relaxor ferroelectrics $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$



A glassy feature seems to survive in the field-induced state & contribute to the electric polarization.

Effect of ME cooling fields (E & H) on electric polarization

* measured at $H = 9\text{ T}$ & $E = 0\text{ V}/\text{m}$ in $x = 0.40$ sample



Electric polarization P monotonically increases, as cooling E & H increase.

Degree of the alignment of toroidal moments can be tuned by the ME field $E \times H$.

The behavior may reflect the SG feature in which a resulting state of frozen spins strongly depends on the cooling condition.

Summary (ME effect in a magnetically-disordered system)

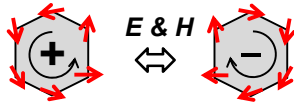
ME properties were investigated for an **XY-like spin glass**,
 $\text{Ni}_x\text{Mn}_{1-x}\text{TiO}_3$ ilmenite structure.

We observed

- ① off-diagonal & antisymmetric ME effects,
- ② frequency-dependent dielectric constant,
- ③ no anomaly in specific heat,
(indicating that long range ordering wasn't induced by H)

$$\begin{pmatrix} P_x \\ P_y \\ P_z \end{pmatrix} = \begin{pmatrix} 0 & T_z & 0 \\ -T_z & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix}$$

These results were reasonably explained by considering that
the spin-freezing process under both E & H makes **toroidal moments polarized**.



Yamaguchi et al., *PRL* 108, 057203 (2012).

Summary

- Symmetry in crystals
- Magnetic symmetry
- Conventional magnetoelectric effect
- Single crystal growth
- Spin-spiral-driven multiferroics
 - Orthorhombic perovskite manganites RMnO_3
 - Cuprates and ferrites working at room temperature
- Observation of spin-spiral domain structure
- ME effect in magnetically-disordered system